CIS 122

Recursion Homework

Assignment 2

• Four recursion themed problems

- Triangle warmup
- Puzzling Palindromes
- Collatz Quandary
- A Shifty Problem (part 2)

1

• How many dots does it take to draw a triangle? o 1 dot on the first row o 2 dots on the second row 3 dots on the third row 0 0 ... 3

10

• How many dots does it take to draw a triangle? o 1 dot on the first row o 2 dots on the second row 3 dots on the third row 0 0 ... • • • • • 0 3 10 • How many dots in a triangle of size 1? 01

• How many dots does it take to draw a triangle? 1 dot on the first row o 2 dots on the second row 3 dots on the third row 0 0 ... • • • • • • • • 0 3 10 • How many dots in a triangle of size 2? 01 + 2 = 3

• How many dots does it take to draw a triangle? 1 dot on the first row o 2 dots on the second row 3 dots on the third row 0 0 ... 0 3 10 • How many dots in a triangle of size 3? \circ 1 + 2 + 3 = 6

• How many dots does it take to draw a triangle? 1 dot on the first row o 2 dots on the second row 3 dots on the third row 0 0 ... • 3 10 • How many dots in a triangle of size n? ○ 1 + 2 + 3 + ... + n

Write a function triangle(n)

 Calculate the nth triangle number
 1 + 2 + 3 + ... + n

What's our base case?

• What's our recursive step?

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 Calculate the nth triangle number
 1 + 2 + 3 + ... + n

What's our base case?
 triangle(0) = 0
 triangle(1) = 1 if your prefer

• What's our recursive step?

Write a function triangle(n) Calculate the nth triangle number 1 + 2 + 3 + ... + n

What's our base case? triangle(0) = 0 triangle(1) = 1 if your prefer

What's our recursive step?
 triangle(n) = n + triangle(n-1)

Write a function triangle(n) Calculate the nth triangle number 1 + 2 + 3 + ... + n

What's our base case? triangle(0) = 0 triangle(1) = 1 if your prefer

- What's our recursive step?
 triangle(n) = n + triangle(n-1)
- Very similar to factorial...

A palindrome reads the same forwards and backwards

- o pop
- \circ madam
- \circ racecar

Write a function isPalindrome(word)

 Return True if word is a palindrome
 Return False otherwise

• How do we tell if a word is a palindrome?

RACECAR

How do we tell if a word is a palindrome?
 First and last letters must match

RACECAR

How do we tell if a word is a palindrome?
 First and last letters must match
 Rest of word must be a palindrome

RACECAR

- How do we tell if a word is a palindrome?
- Base Case

Recursive Step

• How do we tell if a word is a palindrome?

Base Case

The empty string is a palindrome
If first and last letters don't match, NOT a palindrome

Recursive Step

How do we tell if a word is a palindrome?

Base Case

The empty string is a palindrome
If first and last letters don't match, NOT a palindrome

• Recursive Step

If first and last letters match...

The rest of the word must be a palindrome

HOTPO - Half Or Triple Plus One If number is even, divide it by two If number is odd, multiply by three and add one

Collatz Conjecture

- Pick any number
- Repeatedly apply HOTPO
- Eventually, it will reach 1
- You don't need to prove the Collatz Conjecture
 It's still an open problem

Write a function collatz(n)

How many steps does it take to get from n to 1?

Write a function collatz(n)

• How many steps does it take to get from n to 1?

We know what the next number in the sequence is
 If n is even, it's n/2
 If n is odd, its 3*n+1

What if we knew how long it took that number to get to 1?
 Clearly, it takes n one step more!

Write a function collatz(n)

• How many steps does it take to get from n to 1?

Base Case

Recursive Step

Write a function collatz(n)

How many steps does it take to get from n to 1?

Base Case

 collatz(1) = 0
 lt's already there!

Recursive Step

Write a function collatz(n)

• How many steps does it take to get from n to 1?

Base Case

 collatz(1) = 0
 lt's already there!

Recursive Step

 Find how many steps the number after n takes
 n takes one step more

Last week, you wrote a single character shifter

 Takes a character, and a number
 Shifts character forward by that number

Now, we'll use that work to encipher entire strings

 encipher(text, num) - Shift entire text forward by num
 decipher(text, num) - Shift entire text back by num

Before you do any work, copy over caesarShift
 Make sure it works
 You can use the solution function instead...

How can we encipher an entire string?
 We know how to encipher single characters
 Let's encipher our string in pieces

How can we encipher an entire string?
 We know how to encipher single characters
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AAAAAAA

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Recursive Step

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 The empty string can be trivially encoded

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Recursive Step

 Shift the first character
 Encode the rest of the string

How do we decode?
 Easier than it sounds

Recall that shifting forward by 26 means not shifting at all

 If we've already encoded our string
 We can "encode" it even more
 Wrap all the way around