CS 420/520, Intermediate Algorithms Fall 2023

Assignment 5

due Monday, November 20, 2023

- 1. Use the pumping lemma to show that the following are not context free.
 - (a) $A = \{ 0^n 1^n 0^n 1^n \mid n \ge 0 \}$
 - (b) $B = \{ wtw^R \mid w, t \in \{0, 1\}^* \text{ and } |w| = |t| \}$
- 2. Let $\Sigma = \{a, b, c, d\}$ and $C = \{w \in \Sigma^* \mid \text{in } w, \text{ the number of a's equals the number of b's and the number of c's equals the number of d's }. Show that C is not context-free.$
- 3. Consider the PDA described by the state diagram of figure 1 below. Follow the method described the text to construct a CFG for the same language. Note:
 - follow the construction, do not just give a grammar independent of the machine
 - you can omit unnecessary variables (such as $A_{0,2}$)
 - the role of C on the stack is to satisfy feature 3 of the construction
- 4. exercise 3.2(b,c) from text [same in 1st, 2nd, 3rd editions]



Figure 1: PDA for question 3