(Calculi and Types for) Global Computing

FOUNDATIONS OF SECURITY Oregon (23.6.03)

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Overview of the Lectures

im:

Illustrate calculi which formalise these ideas and pave the ground for the development of foundations solid enough to underpin future applications.

pproach:

Present tools – essentially type systems – to guarantee safety, security and in particular resource access control.

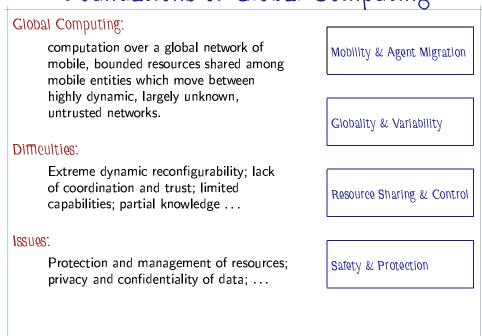
hat:

- > Name Mobility
- > Types for Safety & Control
- > Asynchrony & Distribution
- > Ambient Mobility
- Resource Control

The π Calculus:

- ➤ Basic calculus
- Variations
- Bisimulation
- ➤ Properties

Foundations of Global Computing



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What:

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Typed π Calculi:

- Sorts
- ightharpoonup Simply Typed π
- ➤ I/O Types
- Secrecy Types
- ➤ Group Types

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- ➤ Resource Control

➤ Asynchronous \approx ➤ π_L ➤ D π ➤ Join calculus

Resource Control

Interferences

Secrecy in Ambients

Sizes & Capacities

Asynchronous π Calculi:

 $\rightarrow \pi_A$

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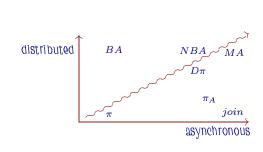
- Name Mobility
- > Types for Safety & Control
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- > Resource Control



- Mobile Ambients
- Ambient Types
- ➤ Boxed Ambients
- Types for Access Control

Roadmap

Another way to look at the plan: Start from π and move towards asynchrony and distribution.



> What will we ignore?

An enormous amount! However, what we'll do will be sufficient to be able to follow the literature and the current developments.

— Lecture I —

The π calculus

Name Mobility

The π calculus is:

- ➤ A formal model to describe and analyse systems of interacting (communicating) processes, with dynamic (re)configuration;
- Terms are processes, that is <u>computational activities</u> running in parallel with each other and possibly containing several independent subprocesses.
- Currently the canonical model of concurrent computation, as the λ-calculus for functional computation:
 - ightharpoonup computation in the λ -calculus is the result of function application; computation is the process of applying functions to arguments and yielding results:
 - ightharpoonup computation in the π -calculus arises from process interaction/reaction (based on communication).

Roadmap for Lecture I

- \triangleright The π calculus' basic mechanisms
- Examples
- Variations

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- \triangleright Polyadic π
- ➤ Summation
- ➤ Match & mismatch
- > Recursion
- ➤ Higher order
- ➤ Barbs & bisimulation
- ➤ LTS & bisimulation

Names in the π calculus

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Naming is a pervasive notion in π :

- ➤ It is a prerequisite to <code>@OMMUNiCation</code> and, therefore, interaction and computation.
- ➤ It presupposes independence: the namer and the named are independent (concurrent) entities.

Names 'name' communication channels not agents

The Syntax

- \blacktriangleright An infinite set of Names: $\mathcal{N} = \{x, y, z, \ldots\}$.
- Action prefixes:

$$\pi ::= x(y) \mid \overline{x}\langle y \rangle \mid \tau$$

Processes:

$$P ::= \sum_{i \in I} \pi_i . P_i \ | \ P \ | \ P \ | \ (\nu a) P \ | \ !P$$

where

- ➤ *I* finite;
- input x(y).P and new $(\nu y).P$ bind y in P. Terms are taken up to α -conversion. That is: for z not free in P

$$x(y).P \equiv x(z).P\{z/y\} \qquad (\nu y)P \equiv (\nu z)P\{z/y\};$$

ightharpoonup commonly used shorthands: $oldsymbol{0}$ for the empty sum $\sum_{i\in\emptyset}$; $oldsymbol{P}+P$ for binary sums; $oldsymbol{\overline{x}}$ or $oldsymbol{x}$ when the message is irrelevant

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Contexts and Congruences

rocess Contexts:

$$\mathscr{C} ::= [.] \mid \pi \mathscr{L} + P \mid (\nu a)\mathscr{C} \mid \mathscr{C} \mid P \mid \mathscr{C}$$

onguences:

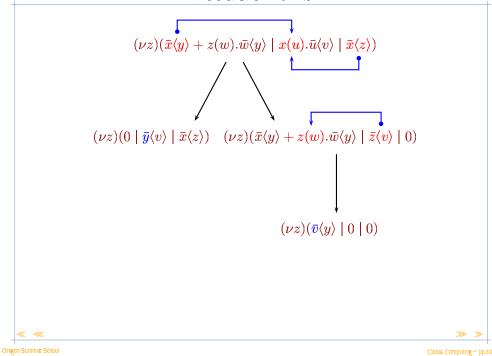
relation \bowtie is a congruence if it is preserved by all contexts, that is $P\bowtie Q$ nplies:

$$\pi.P + R \bowtie \pi.Q + R$$
 $(\nu a)P \bowtie (\nu a)Q$

$$P \mid R \bowtie Q \mid R$$
 $R \mid P \bowtie R \mid Q$

$$!P \bowtie !Q$$

Reductions



Structural Congruence

 $P \equiv Q$ if they can be transformed into each other using

- rearrangement of terms in summations;
- commutative monoidal laws for | (with 0 as unit);

$$(\nu z)(P \mid Q) \equiv (\nu z)P \mid Q,$$
 if $z \notin \mathsf{fn}(Q);$ $(\nu z)\mathbf{0} \equiv \mathbf{0};$ $(\nu x)(\nu y)P \equiv (\nu y)(\nu x)P.$

 $ightharpoonup P \equiv P \mid P$

Standard Form

process

$$(\nu \vec{a})(M_1 \mid \cdots \mid M_m \mid !Q_1 \mid \cdots \mid !Q_n)$$

in standard form if

- 1. each M_i is a sum and
- 2. each Q_i is itself in standard form.

hm: Every processes is structurally congruent to a process in standard form.

001: Easy, by structural induction.



An example

Ithough it may appear not obvious, the term

$$P = x(z).\bar{y}\langle z\rangle \mid !(\nu y)\bar{x}\langle y\rangle.Q$$

as a redex. Let us use \equiv to uncover it.

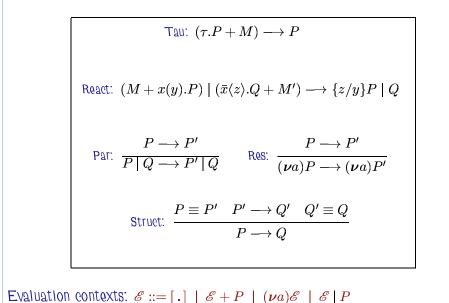
$$P \equiv x(z).\bar{y}\langle z \rangle \mid (\nu y)(\bar{x}\langle y \rangle.Q) \mid !(\nu y)\bar{x}\langle y \rangle.Q$$

$$\equiv x(z).\bar{y}\langle z \rangle \mid (\nu a)(\bar{x}\langle a \rangle.Q) \mid !(\nu y)\bar{x}\langle y \rangle.Q$$

$$\equiv (\nu a)(x(z).\bar{y}\langle z \rangle \mid \bar{x}\langle a \rangle.Q) \mid !(\nu y)\bar{x}\langle y \rangle.Q$$

$$\rightarrow (\nu a)(\bar{y}\langle a \rangle \mid Q) \mid !(\nu y)\bar{x}\langle y \rangle.Q$$

Reaction Rules



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Scope extrusion

The following rule enlarges the scope of a:

$$(\nu a)(P \mid Q) \equiv P \mid (\nu a)Q$$
 if $a \notin fn(P)$

- ➤ left-to-right reading: no surprise
- right-to-left reading: enables export of private names.

$$c(x).P \mid (\boldsymbol{\nu}a)\overline{c}\langle a\rangle.Q$$

In such form, the processes may not communicate. However:

$$c(x).P \mid (\nu a)\overline{c}\langle a \rangle.Q \equiv (\nu a)(c(x).P \mid \overline{c}\langle a \rangle.Q)$$
$$\longrightarrow (\nu a)(P\{a/x\} \mid Q)$$

the name a, private to Q, has been communicated to P.

As in the previous slide, it may be necessary to perform an α -conversion on a.

Scope extrusion, continued

he reduction

$$c(x).P \mid (\nu a)\overline{c}\langle a\rangle.Q \longrightarrow (\nu a)(P\{a/x\} \mid Q)$$

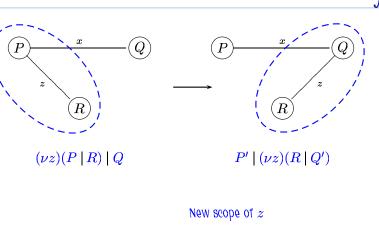
stablishes a new communication link between P and Q, viz. ${\color{red}a}$.

the new link is now private to P and Q, and will remain so until one of them communicates it to third parties.

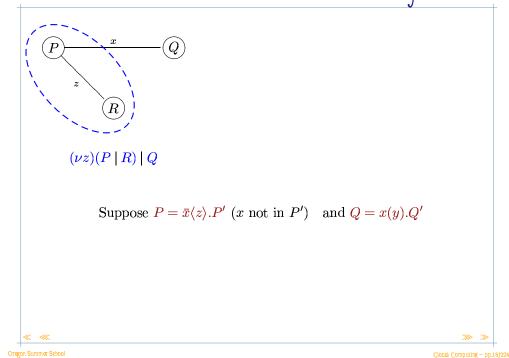
cope extrusion and channel-based communication provide an elementar, yet owerful mechanism for:

- Name mobility: dynamically changing the topological structure of a system of processes, by creating new communication links.
- Secrecy: establishing private, hence secret channels.

The essence of name mobility



I ne essence of name mobility



Name mobility and secret channels

A simple security protocol:

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- ➤ Alice and Bob want to exchange secret M, Server mediates.
- ightharpoonup A sends B a secret channel c_{AB} via S.

Msg 1: $A \rightarrow S$ c_{AB} on c_{AS}

A and B share private channels c_{AS} and c_{BS} with S

Msg 2: $S \rightarrow B$ c_{AB} on c_{BS}

Now A and B communicate via c_{AB} .

Msg 3: $A \rightarrow B$ M on c_{AB}

 π -calculus specification of the protocol

$$A \triangleq (\nu c_{AB}) \overline{c_{AS}} \langle c_{AB} \rangle. \overline{c_{AB}} \langle M \rangle$$
$$S \triangleq c_{AS}(x). \overline{c_{BS}} \langle x \rangle$$

$$B \triangleq c_{BS}(x).x(y).P\{y\}$$

 $SYS \triangleq (\boldsymbol{\nu}c_{AS})(\boldsymbol{\nu}c_{BS})(A \mid B \mid S)$

A run of the protocol

$$\begin{split} \text{SYS} &= c_{BS}(x).x(y).P\{y\} \mid c_{AS}(x).\overline{c_{BS}}\langle x \rangle \mid (\boldsymbol{\nu}c_{AB})(\overline{c_{AS}}\langle c_{AB} \rangle.\overline{c_{AB}}\langle M \rangle) \\ &\equiv c_{BS}(x).x(y).P\{y\} \mid (\boldsymbol{\nu}c_{AB})(\boldsymbol{c_{AS}}(x).\overline{c_{BS}}\langle x \rangle \mid \overline{c_{AS}}\langle c_{AB} \rangle.\overline{c_{AB}}\langle M \rangle) \\ &\longrightarrow c_{BS}(x).x(y).P\{y\} \mid (\boldsymbol{\nu}c_{AB})\overline{c_{BS}}\langle c_{AB} \rangle \mid \overline{c_{AB}}\langle M \rangle) \\ &\equiv (\boldsymbol{\nu}c_{AB})(\boldsymbol{c_{BS}}(x).x(y).P\{y\} \mid \overline{c_{BS}}\langle c_{AB} \rangle \mid \overline{c_{AB}}\langle M \rangle) \\ &\longrightarrow (\boldsymbol{\nu}c_{AB})(c_{AB}(y).P\{y\} \mid \overline{c_{AB}}\langle M \rangle) \end{split}$$

But of course ...

This is an ideal picture, as private channels are an abstraction

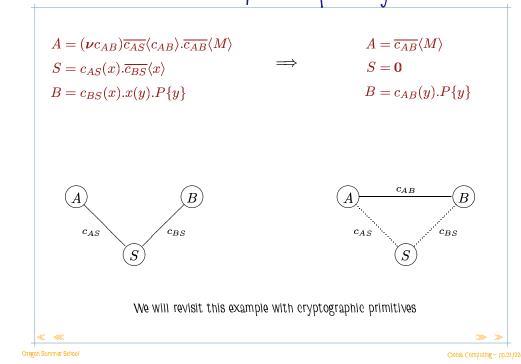
$$(\boldsymbol{\nu}n)(\overline{n}\langle a\rangle Q\mid n(x).P)$$

- What if the two processes are located at remote sites?
- In practice, one needs cryptography

$$(\nu n)(\overline{p}\langle \{a\}_n\rangle Q \mid p(y).\mathsf{decrypt}\ y \ \mathsf{as}\ \{x\}_n \ \mathsf{in}\ P)$$

that's the idea behind the spi calculus

I ne run, conceptually



Polyadie π

$$x(y_1,\ldots,y_n).P \mid \bar{x}\langle z_1,\ldots,z_n\rangle.Q \rightarrow \{\bar{z}/\bar{y}\}P \mid Q$$

Is it a more expressive paradigm? Or can it be encoded?

Right idea:

The idea:

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$$\lceil \bar{x}\langle z_1, z_2 \rangle . P \rceil = (\nu z) \bar{x}\langle z \rangle . \bar{z}\langle z_1 \rangle . \bar{z}\langle z_2 \rangle . \lceil P \rceil$$
$$\lceil x(z_1, z_2) . P \rceil = x(y) . y(y_1) . y(y_2) . \lceil P \rceil$$

Thm. The translation is 'Sound' (i.e., if $\lceil P \rceil$ behaves like $\lceil Q \rceil$, then P behaves like Q). Is it 'correct' (and therefore 'fully abstract')? (Left for exercise).

Example: memory cells

$$\begin{split} \operatorname{Cell}(n) &\triangleq (\nu s)(\overline{s}\langle n\rangle \mid \\ & \quad \operatorname{!get}(y).s(x).(\overline{s}\langle x\rangle \mid \overline{y}\langle x\rangle) \mid \\ & \quad \operatorname{!put}(y,v).s(x)(\overline{s}\langle v\rangle \mid \overline{y}\langle \rangle)) \end{split}$$

- ightharpoonup a private channel s 'stores' the value n (it represents the state of the memory cell),
- > two handlers serving the 'get' and 'put' requests.
 - ➤ both implemented as replicated processes, to serve multiple requests.
 - \blacktriangleright each request served by first spawning a fresh copy of the handler by means of the congruence $!P \equiv P \mid !P$.

Cell and User

sample user of the cell:

$$\begin{aligned} \mathsf{client}(v) &= (\pmb{\nu} \mathsf{ack})(\pmb{\nu} \mathsf{ret}) \\ & \overline{\mathsf{put}} \langle \mathsf{ack}, v \rangle. \mathsf{ack}(). \overline{\mathsf{get}} \langle \mathsf{ret} \rangle. \mathsf{ret}(x). \overline{\mathsf{print}} \langle x \rangle \end{aligned}$$

- declare private return and ack channels
- ➤ first write a new value, wait for ack, and then read the cell contents to print the returned value.

et us look at the system:

$$\operatorname{cell}(0) \mid \operatorname{client}(v) \equiv (\nu s)(\nu \operatorname{ack})(\nu \operatorname{ret})(\dots)_{cell} \mid (\dots)_{\text{USEP}}$$

Cell: put and get

$$\gcd(y).s(x).(\overline{s}\langle x\rangle \mid \overline{y}\langle x\rangle)$$

- receive on get the name y of a channel where to send back the result
- upon receiving the channel name, consume the current cell value, and then reinstate it while copying it to the channel y;

$$\operatorname{put}(y,v).s(x)(\overline{s}\langle v\rangle \mid \overline{y}\langle\rangle)$$

 \triangleright similar situation, with a further subtlety: also expect an "ack" channel (y) from the user, and use it to signal the completion of the protocol.

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Cell & user: reduction

$$\begin{split} \langle \overline{s}\langle 0 \rangle \mid & (\operatorname{put}(y,v).s(x).\ldots \mid \ldots))_{cell} \mid (\overline{\operatorname{put}}\langle \operatorname{ack}, 1 \rangle \ldots)_{user} \\ & \longrightarrow (\overline{s}\langle 0 \rangle \mid s(x).(\overline{s}\langle 1 \rangle \mid \overline{\operatorname{ack}}\langle \rangle) \mid \ldots))_{cell} \mid (\operatorname{ack}().\ldots)_{user} \\ & \longrightarrow (\overline{s}\langle 1 \rangle \mid \overline{\operatorname{ack}}\langle \rangle \mid \ldots)_{cell} \mid (\operatorname{ack}().\ldots)_{user} \\ & \longrightarrow (\overline{s}\langle 1 \rangle \mid (\operatorname{get}(y).s(x).\ldots))_{cell} \mid (\overline{\operatorname{get}}\langle \operatorname{ret} \rangle \ldots)_{user} \\ & \longrightarrow (\overline{s}\langle 1 \rangle \mid (s(x).(\overline{s}\langle x \rangle \mid \overline{\operatorname{ret}}\langle x \rangle) \ldots))_{cell} \mid \operatorname{ret}(x).\overline{\operatorname{print}}\langle x \rangle \\ & \longrightarrow (\overline{s}\langle 1 \rangle \mid \overline{\operatorname{ret}}\langle 1 \rangle \ldots)_{cell} \mid \overline{\operatorname{ret}}\langle 1 \rangle \\ & \longrightarrow (\overline{s}\langle 1 \rangle \mid \ldots)_{cell} \mid \overline{\operatorname{print}}\langle 1 \rangle \end{split}$$

Summation

he original calculus has unguarded sums:

$$P ::= \dots \mid P + P$$

his makes the theory more complex while producing little gains in expressiveness.

$$\sum_{i\in I} x_i(y).P$$

ejects things like $(\underline{x}.P + \overline{y}.Q) \mid (\overline{x}.P' + y.Q')$.

o sums at all:

till, purely internal choice $\tau.P + \tau.Q$ can be defined:

$$(\nu a)(\bar{a} \mid a.P \mid a.Q)$$



Recursive Definitions

is useful to be able to write

$$A(\vec{x}) \stackrel{def}{=} Q_A$$
, where $Q_A = \cdots A \langle \vec{w} \rangle \cdots A \langle \vec{w} \rangle \cdots$

can be obtained using replication as follows

- 1. Choose a_A to stand for A;
- 2. $\widehat{R} = \text{replace } A\langle \overrightarrow{w} \rangle \text{ with } \overline{a}_A \langle \overrightarrow{w} \rangle \text{ in } R;$
- 3. $\widehat{\widehat{P}} = (\nu a_A)(\widehat{P} \mid !a_A(\vec{x}).\widehat{Q}_A).$

In the other hand, replication can be defined from recursive defs.

$$A \stackrel{def}{=} P \mid A$$
.

Matening and Mismatening

The original calculus has

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$$\pi ::= \dots \mid [x=y]\pi \mid [x \neq y]\pi$$

$$[x=x]P \equiv P$$
 $[x \neq y]P \equiv \mathbf{0}$

Useful in programming, it has an impact on the theory, and somehow complicates it. A general encoding is impossible, but in some cases its effect can be recovered to a certain extent:

$$\Box a(x).(\sum_{i}[x=k_{i}]P_{i}) \Box = a(x).(\bar{x}\langle\rangle \mid \sum_{i}k_{i}().\Box P_{i}\Box)$$

Though this works only provided nobody 'interferes' with k_i .



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Higher Order π

A most natural suggestion for process mobility:

$$\pi ::= \cdots \mid x(X) \mid \bar{x}\langle P \rangle$$

$$P ::= \cdots \mid X$$

$$x(X).P \mid \bar{x}\langle R \rangle.Q \to \{R/X\}P \mid Q$$

Thm. Encoding 'fully abstract'. Assume a name an unused name x associated to each X.

$$[\overline{a}\langle P\rangle.Q]=(\nu p)\overline{a}\langle p\rangle.([Q]\mid !p.[P]),\ \ p \ \text{fresh}$$

$$[a(X).P]=a(x).[P])$$

$$[X] = \overline{x}$$

Other variants

- Asynchronous π : Disallow continuation on sending $\overline{a}\langle x\rangle.P$.
- \blacktriangleright Local π : Disallow inputs on x in the body of a(x).P.
- Private π : Disallow output of free names: Processes can only pass names their own private names.
- Distributed π : Several interesting calculi based on π_A : Dpi, Join, Blue, Seal, Nomadic Pict,...
- > Spi, applied pi,...

Observations and Contexts

arbed equivalence is very weak, but 'contexts' are very powerful enquirers: onsider $\mathscr{C} = (\nu a)([\]\ |\ a(x).x)$. Then

$$\mathscr{C}[\bar{a}\langle u \rangle] \to (\nu a) u \downarrow_u \qquad \mathscr{C}[\bar{a}\langle v \rangle] \to (\nu a) v \downarrow_v \qquad \mathscr{C}[(\nu u) \bar{a}\langle u \rangle] \to (\nu a u) u \not\downarrow$$

herefore $\mathscr{C}[ar{a}\langle u
angle]$ $ot\stackrel{.}{
ot}$ $\mathscr{C}[ar{a}\langle v
angle]$ $ot\stackrel{.}{
ot}$ $\mathscr{C}[(
u u)ar{a}\langle u
angle]$

arbed Congruence \cong^c : Is the largest congruence in $\stackrel{.}{\approx}$, that is

$$P \cong^c Q$$
 iff $\mathscr{C}[P] \stackrel{.}{\approx} \mathscr{C}[Q]$, for all \mathscr{C} .

Ontext Lemma: $P \cong^c Q$ iff $P\sigma \mid R \stackrel{.}{\approx} Q\sigma \mid R$, for all R and substitutions σ .

Xereise: Only non-injective substitutions are interesting here...

Observations and Bisimulation

 $P \downarrow_{\overline{a}} \triangleq P \equiv (\nu \vec{x}) (\overline{a} \langle z \rangle . P' + \cdots) \qquad \qquad a \notin \vec{x}$ $P \downarrow_{a} \triangleq P \equiv (\nu \vec{x}) (a(z) . P' + \cdots) \qquad \qquad a \notin \vec{x}$ $P \Downarrow_{\alpha} \triangleq P \Longrightarrow \downarrow_{\alpha} \qquad (\Longrightarrow \triangleq \longrightarrow^{*})$

Barbed Bisimulation $\stackrel{.}{pprox}$: is the largest equivalence relation \pitchfork s.t. for all $P \pitchfork Q$

ightharpoonup If $P\longrightarrow P'$ then $Q\Longrightarrow Q'$ for some such that $P'\pitchfork Q'$;

Observations: $P \downarrow_a$ if P can engage in action involving a

 \blacktriangleright If $P \downarrow_x$, then $Q \Downarrow_x$

Barbed bisimulation is very weak, pretty useless:

$$\overline{a}\langle u
angle \quad \dot{\overline{lpha}}\langle v
angle \quad \dot{\overline{lpha}}\langle u
angle \quad \langle oldsymbol{
u}u
angle \overline{a}\langle u
angle$$

Consider e.g. $\pitchfork = \{(\overline{a}\langle u \rangle, \overline{a}\langle v \rangle)\}$ and ...

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The problem with aliasing

Role of σ is account for aliasing occurring from rebinding of names after input.

Consider that
$$\overline{x} \mid y \stackrel{.}{\approx} \overline{x}.y + y.\overline{x}.$$

But, in $\mathscr{C} = a(y).[\,.\,] \mid \overline{a}\langle x \rangle$, since x is received for y, $\overline{x} \mid x \not\approx \overline{x}.x + x.\overline{x}$. The effect of such contexts is captured by the context lemma $\sigma(x) = \sigma(y) = z$.

Similar problems for matching:

$$[x=y]c \stackrel{.}{\approx} 0$$
 but $[x=x]c \stackrel{.}{st} 0$.

Labelled Iransition System

- ➤ Barbed bisimulation derives <code>Naturally</code> from the <code>reduction</code> rules.
- Congruences are brought about by engineering, mathematical and logical considerations.
- ➤ But barbed congruence is hard to work with.
- Desiderata: Characterise it in terms of:
 - 1. bisimulations (easy to reason with coinduction)
 - 2. labelled transition systems (describe interactions with environment explicitly, help intuition, bag of tools, \dots)

Labelled Transition System

$$(Out) \qquad (Inp) \qquad (Tau)$$

$$\overline{x}\langle y\rangle.P \xrightarrow{\overline{xy}} P \qquad \overline{x}(z).P \xrightarrow{xy} P\{y/z\} \qquad \overline{\tau}.P \xrightarrow{\tau} P$$

$$(Open) \qquad P \xrightarrow{\overline{xz}} P' \qquad x \neq z \qquad P \xrightarrow{P} P' \qquad Q \xrightarrow{xz} Q' \qquad z \notin fn(Q)$$

$$P \xrightarrow{\overline{xz}} P' \qquad Q \xrightarrow{\overline{xz}} P' \qquad P' \qquad Q \xrightarrow{T} (\nu z)(P' \mid Q') \qquad z \notin fn(Q)$$

$$P \xrightarrow{\overline{xz}} P' \qquad Q \xrightarrow{xz} Q' \qquad P \xrightarrow{P} P' \qquad P \xrightarrow{Q} P' \qquad P \xrightarrow{Q}$$

π Actions

$$\alpha ::= \tau \mid \overline{x}y \mid \nu \overline{x}y \mid xy$$

- $ightharpoonup n(\alpha)$: names in α
- ightharpoonup bn(α): names bound in α , that is bound output.

Desiderata:

Thm: Establish a compositional $\xrightarrow{\alpha}$ such that $\xrightarrow{\tau} \equiv = \longrightarrow$

Thm: Establish a proof technique for \cong^c using bisimulation on $\stackrel{\alpha}{\longrightarrow}$

An example

Let us show how to prove that

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$$x(y).P \mid (\nu a)\overline{x}\langle a \rangle.Q \xrightarrow{\tau} (\nu a)(P\{a/y\} \mid Q)$$

$$\underbrace{x(y).P \xrightarrow{xa} P\{a/y\}} \frac{\overline{x}\langle a \rangle.Q \xrightarrow{\overline{x}a} Q}{(\nu a)\overline{x}\langle a \rangle.Q \xrightarrow{\nu \overline{x}a} Q}$$

 $x(y).P \mid (\nu a)\overline{x}\langle a\rangle.Q \xrightarrow{\tau} (\nu a)(P\{a/y\} \mid Q)$

The role of Open, Close, and Comm:

$$(y).P \stackrel{x}{\longleftrightarrow} \langle a \rangle.Q = (P\{a/y\} \mid Q)$$
$$(y).P \stackrel{x}{\longleftrightarrow} (\nu a) \langle a \rangle.Q = (\nu a)(P\{a/y\} \mid Q)$$

Bisimulation

isimulation pprox: is the largest equivalence relation \pitchfork s.t. for all $P \pitchfork Q$

$$P \xrightarrow{\alpha} P'$$
 then $Q \Longrightarrow \pitchfork P'$

ote that:

in $a(x).P \approx Q$, term $P\{y/x\}$ must be matched for all y (well, almost...);

 $\nu \overline{x}z$ must be matched only for an appropriately fresh z.

gain, ≈ is not preserved by substitutions

ull Bisimulation $P \approx^c Q$ iff $P\sigma \approx Q\sigma$ for all substitutions σ (non injective).

 $hm \approx \subset \cong \mathsf{and} \approx^c \subset \cong^c.$

In finite-image processes, i.e., such all sets of α -derivated $\{P' \mid P \stackrel{\alpha}{\Longrightarrow} P'\}$ are nite, with matching $pprox^c = \cong^c$.

XQTCISQ: Prove that matching is necessary, by showing that $P \not\approx Q$, but ${}^{\circ}[P] \stackrel{.}{pprox} \mathscr{C}[Q]$ for all contexts without matching, where

$$P=\overline{a}\langle x
angle \mid !x\mid !\overline{x}\mid !y\mid !\overline{y} \quad ext{and} \quad Q=\overline{a}\langle y
angle \mid !x\mid !\overline{x}\mid !y\mid !\overline{y}$$

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Exercises

Exercises:

$$ightharpoonup$$
 Prove $\equiv \xrightarrow{\tau} = \xrightarrow{\tau} \equiv$;

 \triangleright Prove $\equiv \subset \approx$;

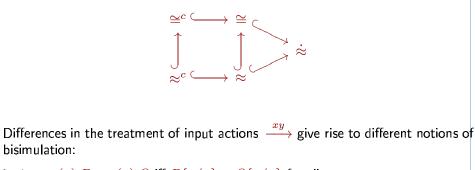
ightharpoonup Prove $\equiv \subset \stackrel{.}{\approx}$ and $\equiv \subset \cong^c$

ightharpoonup Prove $\overline{x}\langle a\rangle \not\cong^c (\nu z)\overline{x}\langle z\rangle$.

ightharpoonup Prove $\tau.P \approx^c P$.

ightharpoonup Prove $\approx \subseteq \stackrel{.}{\approx}$ and $\approx^c \subseteq \cong^c$

Comparisons and Other disimulations



► late: $a(x).P \approx a(x).Q$ iff $P\{y/x\} \approx Q\{y/x\}$ for all y;

round: $a(x).P \approx a(x).Q$ iff $P\{y/x\} \approx Q\{y/x\}$ for a fresh y;

> open: obtained using substitutions explicitly in the bisimulation game.

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bisimulation:

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Summary of Lecture I

- This lecture introduced the π calculus' mechanisms and the fundamentals of its semantic theory, ie barbed congruence and full bisimilarity.
- > Further Reading:

A complete list would be enourmous. Luckily, two references for all can take you a long way

- \triangleright Communication and Mobile Systems: the π -calculus (Milner)
- The π -calculus: A theory of mobile processes (Sangiorgi, Walker)
- ➤ The mobility home page http://lamp.epfl.ch/mobility/

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— Lecture II —

Types for Safety and Control

Why Types?

onsider the following terms of the polyadic π -calculus.

$$\overline{a}\langle b,c\rangle.P\mid a(x).Q$$
 $\overline{a}\langle {\sf true}\rangle.P\mid a(x).x(y).Q$

Both terms are ill-formed, make no sense, and must therefore be ruled out. This one of the role of types. In general, types establish invariants of computation nat we use to guarantee safety in many varieties.

- > Types protect from errors and therefore provide guarantees of consistent process interaction.
- Types convey logical structure: the untyped π -calculus is too weak to prove some expected properties of processes arising from implicit discipline of name usage.

Types bring the intended structure back into light, and enhance formal reasoning on process terms: for instance, typed behavioral equivalences are more generous, and can be easier to prove, as only typed contexts need to be looked at.

Roadmap of Lecture II

- ➤ Milner's sorting system
- \triangleright Simply typed π calculus
- ➤ IO types and subtypes
- Typed barbed congruence
- Types for secrecy
- Group types

Milner's sorting system

Memory cells $\operatorname{cell}(n) \triangleq (\nu s)(\overline{s}\langle n \rangle \mid \operatorname{!get}(y).s(x).(\overline{s}\langle x \rangle \mid \overline{y}\langle x \rangle) \mid$ $\operatorname{!put}(y,v).s(x)(\overline{s}\langle v \rangle \mid \overline{y}\langle \rangle))$

- > ret used to communicate integers,
- > get and ack used to communicate another channel

Sorting:

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«

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Sorting, formally

Sorting System

- A function $\Sigma: S \longrightarrow S^*$ describes the tuples allowed on channels of each sort. $\Sigma(\gamma)$ is the object sort of γ .
- ▶ Object sort of $\gamma \in S$ must follow the sorting discipline $\Sigma(\gamma)$.
- ightharpoonup P respects Σ if in each subterm $\overline{x}\langle \vec{y} \rangle.P'$ or $x(\vec{y}).P'$, if $x:\gamma$, then $\vec{y}:\Sigma(\gamma)$

ubject Reduction: If P respects Σ and $P\longrightarrow Q$, then Q respects Σ .

follows that $P \xrightarrow{\overline{x}\overline{y}}$ implies that $\overline{y} : \Sigma(\gamma)$, for $x : \gamma$.

herefore, these cannot happen:

$$\overline{a}\langle b,c\rangle.P\mid a(x).Q$$

$$\overline{a}\langle \mathsf{true}\rangle.P\mid a(x).x(y).Q$$

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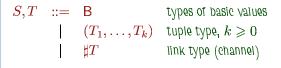
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Type system

- Initial idea: types assigned only to channels, processes are either well typed under a particular set of assumptions for their bound and free names, or they are not.
- > two judgement forms:
 - $ightharpoonup \Gamma \vdash v : T \qquad v \text{ has type } T$
 - $ightharpoonup \Gamma \vdash P$ P is well-typed
- $ightharpoonup \Gamma$ type environment: a set of type assumptions for names and variables (equivalently, a finite map from names and variables to types)

different approach possible, based on assigning more informative types to rocesses to describe various forms of process behavior.

Simply Typed π calculus



Channel types

> inform on the type of the value they carry

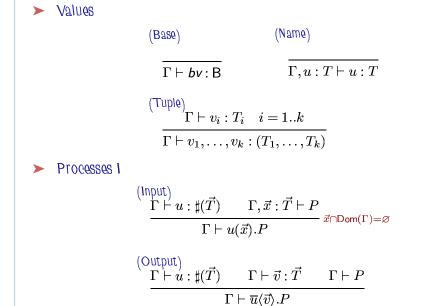
Examples

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- ➤ #(int) : channel carrying values of type int.
- \blacktriangleright \sharp (unit) : channel carrying \star , the only value of type unit.
- #(#int): channel whose values are channels carrying integers.

Typing rules: Values and Messages

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Typing rules: Process

$$\frac{(\mathsf{Zero})}{\Gamma \vdash \mathbf{0}} \qquad \qquad \frac{\overset{(\mathsf{Par})}{\Gamma \vdash P \quad \Gamma \vdash Q}}{\Gamma \vdash P \mid Q}$$

$$egin{array}{ll} (\mathsf{Repl}) & (\mathsf{Restr}) \ \Gamma \vdash P & \Gamma, a: T \vdash P \ \hline \Gamma \vdash ! \, P & \Gamma \vdash (
u a: T) P \end{array}$$

Type System Properties II

ype Safety

- > well-typed processes communicate in type-consistent ways.
- \blacktriangleright Let $\Gamma, c : \sharp (T_1, \ldots, T_n) \vdash P$. If P contains

$$\vdash c(x_1,\ldots,x_h).Q_1 \mid \overline{c}\langle v_1,\ldots,v_k\rangle.Q_2$$

then c is a name (not a basic value), k = h = n and $v_i : T_i$.

- Subject reduction guarantees that this property holds of all derivatives of P.
- We will describe richer notions of type safety that provide security guarantees

Type System Properties I

Subject Reduction:

- reduction preserves well-typedness.
- ightharpoonup if $\Gamma \vdash P$ and $P \longrightarrow Q$, then $\Gamma \vdash Q$.
- needs

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- Substitution Lemma if $\Gamma \vdash u : T$ and $\Gamma, x : T \vdash P$, then $\Gamma \vdash P\{u/x\}$.
- Subject Congruence if $\Gamma \vdash P$ and $P \equiv Q$, then $\Gamma \vdash Q$.

Why Types? II

> Types help resource access control

In the untyped $\pi\mbox{-calculus, resources}$ (channels) are protected by hiding them

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Often too coarse a policy: protection is lost when the channel name is transmitted, as no assumption can be made on how the recipient of the name will use it.

Types come to the rescue: enforce constraints on use of channels by associating them with read and/or write capabilities.

Example: printer

- \triangleright printer P and two clients C_1 and C_2 .
- \triangleright P provides a request channel p carrying data to be printed
- \rightarrow π -calculus representation:

$$(\boldsymbol{\nu}p)(P\mid C_1\mid C_2)$$

- ightharpoonup if $C_1 riangleq \overline{p}\langle j_1 \rangle.\overline{p}\langle j_2 \rangle...$, we expect that the jobs $j_1, j_2,...$ are received and processed, in that order.
- Not necessarily true: C_2 might compete with P to "Steal" the jobs sent by C_1 and throw them away: $C_2 \triangleq ! p(j).0$.
- ➤ Let's fix this with Types!

Subtyping

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he core of resource access control by typing: restrict capabilities in certain ontexts to protect channels from misuse.

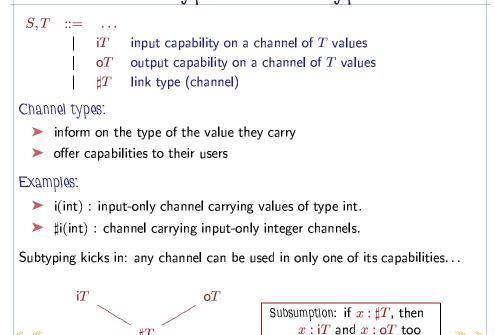
$$p: \sharp T, a: \sharp \mathsf{i} T \vdash \overline{a} \langle p \rangle. P \mid a(x). Q$$

knows p as a read/write channel. Q receives it on a and therefore knows it nly as a input-only channel. Name p can travel on a because of Subtyping ans absumption.

$$\frac{\text{(Subs Refi)}}{T\leqslant T} \qquad \frac{T\leqslant T'}{T\leqslant T'} \quad \frac{T'\leqslant T''}{T\leqslant T''}$$

(Subs IO/I)
$$\frac{\text{(Sub IO/O)}}{\sharp T\leqslant \mathrm{i}T}$$

IO Types and Subtypes



Subtyping, II

> subtyping applies also to argument types

- \blacktriangleright intuition: Assume $c: \sharp T$.
 - ightharpoonup c can safely be used to read values at type T or higher, ...
 - ightharpoonup provided that only values at type T, or lower, are written to c

As for invariance, suppose nat $\leqslant \mathsf{int} \leqslant \mathsf{real}$ and $a: \sharp (\mathsf{int}).$

If \sharp was variant, either this $P_1=\overline{a}\langle 3.5\rangle$ or $P_2=a(x).\overline{\log}\langle x\rangle$ would be typable.

Also Q=a(x).succ $x\mid \overline{a}\langle -2\rangle$ is obviously alright. But $P_1\mid Q$ and $P_2\mid Q$ are both flawed.

New typing rules

$$\frac{\Pr (\mathsf{Input})}{\Gamma \vdash u : \mathsf{i}\vec{T}} \frac{\Gamma, \vec{x} : \vec{T} \vdash P}{\Gamma \vdash u(\vec{x}).P}$$

$$\frac{ \overset{\left(\text{Output} \right)}{\Gamma \vdash u : \text{o} \vec{T}} \qquad \Gamma \vdash v_i : T_i \qquad \Gamma \vdash P}{ \Gamma \vdash \overline{u} \langle \vec{v} \rangle . P}$$

$$\frac{ \begin{pmatrix} \text{Subsumption} \end{pmatrix} }{ \Gamma \vdash u : S} \qquad S \leqslant T \\ \hline { \Gamma \vdash u : T }$$

ubject Reduction: if $\Gamma \vdash P$ and $P \longrightarrow Q$, then $\Gamma \vdash Q$.

rocesses

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Typed printer II

Tain steps of the typing derivation of $\Gamma \vdash \overline{a}\langle p \rangle.\overline{b}\langle p \rangle \mid a(x).P \mid b(y).(C_1 \mid C_2)$, where $\Gamma = \{a, b : \sharp(\sharp T), p : \sharp T\}.$

$$\Gamma \vdash a,b: \sharp (\sharp T) \qquad \sharp (\sharp T) \leqslant \mathsf{o}(\sharp T)$$

$$\sharp T \leqslant iT$$

$$\sharp (\sharp T) \leqslant i(\sharp T) \quad \overline{i(\sharp T) \leqslant i(iT)}$$

$$\frac{\Gamma \vdash a : \mathsf{i}(\mathsf{i}T) \qquad \qquad \Gamma, x : \mathsf{i}T \vdash P}{\Gamma \vdash a(x).P}$$

$$\frac{\sharp(\sharp T)\leqslant \mathsf{i}(\sharp T) \ \overline{\mathsf{i}(\sharp T)\leqslant \mathsf{i}(\sharp T)}}{\Gamma\vdash b:\mathsf{i}(\mathsf{o}T)} \frac{}{\Gamma,y:\mathsf{o}T\vdash C_1\mid C_2}$$

$$\frac{}{\Gamma\vdash b(y).(C_1\mid C_2)}$$

 $\sharp T\leqslant \mathsf{o}T$

i yped printer

- ightharpoonup use types to make sure the printer only reads from p, and the clients only write on p.
- \blacktriangleright initialize the system with two channels a and b, to send the name p to P and to C_1 and C_2 restricting the use of p.

$$S \triangleq (\boldsymbol{\nu}p: \sharp T)\overline{a}\langle p\rangle.\overline{b}\langle p\rangle|a(x:iT).P \mid b(y:oT).(C_1 \mid C_2)$$

$$\longrightarrow (\boldsymbol{\nu}p: \sharp T)P\{p/x\} \mid (C_1 \mid C_2)\{p/y\}$$

- \blacktriangleright typing ensures that P only reads, and C_i 's only write on p
- \triangleright With appropriate definitions for P and C_i 's

$$a,b:\sharp(\sharp T)\vdash S$$

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Limitations

The simply typed λ calculus has only finite computation. Not so the simply type π calculus. There however limitations, due with the fact that terms must have a finite bound on the "nesting" of channels.

Thm. No well typed term can produce a sequence of actions such as

$$x_1(x_2).x_2(x_3).x_3(x_4).x_4(x_5)...$$

'Cause, what would the type of x_1 be? $\sharp(\sharp(\sharp(\ldots)))$

The problem can be avoided with recursive types (Pierce, Sangiorgi).

Then $x_1: \mu X. \sharp X$. The untyped calculus can be encoded satisfactorily in the recursively typed π using such type.

Advanced Type Systems

he work on types has push forward towards greater refinement and control of esources. We will see examples of types for secrecy and capability types. list of things we will not see:

- linear type systems, trying to control how many times a resource is used (Pierce, Kobayashi, Yoshida,)
- > types for deadlocks avoidance (Kobayashi,...)
- Polymorphic types:
- $a: \sharp \langle X | \sharp X \times X \rangle \vdash \overline{a} \langle Int; c, s \rangle \mid a(x).$ Open x as (X; z, y) in $\overline{z} \langle y \rangle$ (Pierce, Sangiorgi)

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Typed Barbed Bisimulation

efinition: A (Γ/Δ) -context is a Γ -context with a Δ -hole. That is, $\mathscr C$ such that henever $\Delta \vdash P$, then $\Gamma \vdash \mathscr{C}(P)$.

arbed Congruence. For $\Delta \vdash P, Q$ we say $\Delta \triangleright P \cong^c Q$ if for all closed Γ and all Γ/Δ)-contexts \mathscr{C} , we have $\mathscr{C}(P) \approx \mathscr{C}(Q)$.

Yped substitutions σ is a Δ/Γ substitution if for all $x \in Dom(\Delta)$, we have $\vdash \sigma(x) : \Delta(x)$.

Vped Context Lemma $\Delta \triangleright P \cong^c Q$ if and only if all closed Γ which extend Γ , or all Δ/Γ substitutions, and all $\Gamma \vdash R$ we have $P\sigma \mid R \approx Q\sigma \mid R$.

I ne Case for Typed Benavioural Equivalences

Firstly, it makes no sense to compare processes with different types. Also, we know that

$$P = a(b).(\overline{b}\langle v\rangle \mid c(z)) \quad \not\cong^c \quad a(b).(\overline{b}\langle v\rangle.c(z) + c(z).\overline{b}\langle v\rangle) = Q$$

But what if we know, say, $\Gamma = \{a : \sharp \sharp S, c : \sharp T\} \vdash P, Q \text{ for } S \neq T$?

Then
$$\{a: \sharp\sharp S, c: \sharp T\} \triangleright P \cong^c Q$$

This is because no legit context will be able to alias b an c.

What is the effect of types on behavioural equivalences?

Example:
$$P = (\nu x)(\overline{a}\langle x \rangle \mid \overline{x}\langle b \rangle) \not\cong^c Q = (\nu x)\overline{a}\langle x \rangle$$
.

$$P$$
 and Q are distinguished by $\mathscr{C}=(\pmb{\nu}a)(a(x).x(z).\overline{c}\,|\,[.]).$ However,

$$\Delta = \{a : \sharp \mathsf{o} S, b : S\} \triangleright P_1 \cong^c P_2.$$

This is because no well-typed environment will be able to verify the presence of the output $\overline{x}(b)$. Types make equivalence coarser, as they limit the "power of observer," that is the number of contexts.

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Typed Bisimulation

Typed notions of \approx are know for most typed π calculi, but the issue can be problematic.

Consider

$$P = (\nu x y)(\overline{a}\langle x\rangle \mid \overline{a}\langle y\rangle \mid !x.Q \mid !y.Q) \qquad Q = (\nu x)(\overline{a}\langle x\rangle \mid \overline{a}\langle x\rangle \mid !x.Q).$$

These are \cong^c . A distinguishing context is $\mathscr{C} = a(z_1).a(z_2).(z_1().\overline{c} \mid \overline{z_2}).$ But if $\Gamma \vdash a$: oounit, then $\Gamma \triangleright P \cong^c Q$, because no context will be able to input

Matching actions is not trivial, though. Observe that

and, therefore, tell y apart from x.

$$P \xrightarrow{\nu \overline{a}x} \xrightarrow{\nu \overline{a}y} \xrightarrow{yv}$$

$$Q \xrightarrow{\nu \overline{a}x} \xrightarrow{\overline{a}x} \xrightarrow{xv}$$

So, they are easily too fine. Need to refine with system/environment point of view of an action.

As a proof technique sometimes the context lemma works much better.



Types for Secrecy

n application in which types guarantee that secrets are not leaked by programs. xpressed in the Spi ealculus.

emember the wide mouth frog protocol? Let's add explicit encryption:

$$A \longrightarrow S : \{K_{AB}\}_{K_{AS}}$$

 $S \longrightarrow B : \{K_{AB}\}_{K_{BS}}$
 $A \longrightarrow B : \{M\}_{K_{AB}}$

he protocol now runs as

$$A(M) \triangleq (\nu K_{AB}) \overline{c_{AS}} \langle \{K_{AB}\}_{K_{AS}} \rangle. \overline{c_{AB}} \langle \{M\}_{K_{AB}} \rangle$$

$$S \triangleq c_{AS}(x). \text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c_{SB}} \langle \{y\}_{K_{SB}} \rangle$$

$$B \triangleq c_{SB}(x). \text{case } x \text{ of } \{y\}_{K_{SB}} \text{ in } c_{AB}(z). \text{case } z \text{ of } \{w\}_y \text{ in F}(w)$$

$$\text{Inst}(M) \triangleq (\nu K_{AS}, K_{SB}) (A(M) \mid S \mid B)$$

Secrecy of M: Inst $(M)\cong ext{Inst}(M')$, for all M' . (Similar notion available for authenticity)

Spi calculus: Semantics

$$[M \text{ is } M]P \equiv P$$

$$\text{let } (x,y) = (M,N) \text{ in } P \equiv P\{M/x,N/y\}$$

$$\text{case } 0 \text{ of } 0:P \text{ succ}(x):Q \equiv P$$

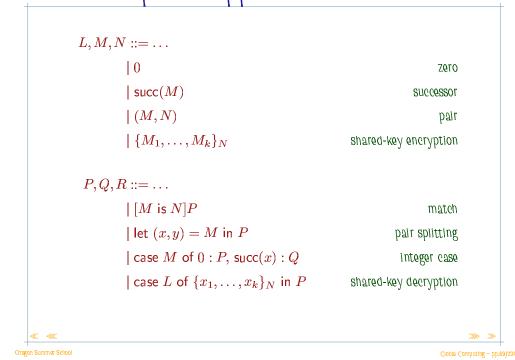
case $\operatorname{succ}(M)$ of $0:P,\ \operatorname{succ}(x):Q\equiv Q\{M/x\}$ case $\{M\}_N$ of $\{x\}_N$ in $P\equiv P\{M/x\}$

(Comm)

$$\overline{n(x_1,\ldots,x_k)P\mid \overline{n}\langle M_1,\ldots,M_k\rangle.Q\longrightarrow P\{M_1/x_1,\ldots,M_k/x_k\}}$$

$$\begin{array}{c} \text{(Par)} \\ \hline P \to P' \\ \hline P \mid Q \to P' \mid Q \end{array} \qquad \begin{array}{c} \text{(New)} \\ \hline (\nu n) P \to (\nu n) P' \end{array} \qquad \begin{array}{c} \text{(Cong)} \\ \hline P \equiv P' \quad P' \to Q' \quad Q' \equiv Q \\ \hline P \to Q \end{array}$$

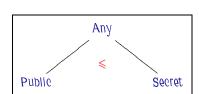
Spi: an applied π calculus



Secrecy

Data into three security classes, formalised as types:

- Public, which can be communicated
- > Secret, which should not be leaked;
- Any, which is arbitrary data



Encryption keys are data. Only the following combination are reasonable

- encrypting v with a Public key has the same level as the data encrypting v with a Secret key can be made Public;
- only public data can be sent on public channels, while all kinds of data may be sent on secret channels.

Aim: Design a type system to guarantee the secrecy of parameters of type Any.

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Messages and Contounders

o avoid confusion on the format of encrypted data, we adopt common one.

Secret_ $\{M_1, M_2, M_3, n\}_K$

Message 1 $B \rightarrow A$: N_B

Message 2 $A \rightarrow B$: $\{M, N_B\}_{K_{AB}}$

his does not guarantee the secrecy of M_{\cdot} . If an attacker sends a nonce N_{C} vice, A replies with ciphertexts $\{M,N_C\}_{K_{AB}}$ and $\{M',N_C\}_{K_{AB}}$. ttacker gets to know whether M and M' are the same message by just omparing the two ciphertexts.

Message 1 $B \rightarrow A$: N_B

Message 2 $A \rightarrow B$: $\{M, N_B, N_A\}_{K_{AB}}$

he confounder N_A is a fresh number that A creates for every encryption and revents the information flow illustrated above.

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The Types

he Types:

- \triangleright $\vdash E$ well formed
- means that environment E is well-formed.
- \triangleright $E \vdash M : T$

that term M is of level T in E. means

 \triangleright $E \vdash P$ means that process P type-checks in E.

.nyironments

$$(Env \ Empty) \qquad (Env \ Variable) \\ \vdash E \ \text{well formed} \qquad \vdash E, x : T \ \text{well formed} \qquad x \notin dom(E)$$

(Env Name)

dash E well formed $Edash M_1:T_1\ldots Edash M_k:T_k$ Edash N:R $\vdash E, n : T :: \{M_1, \ldots, M_k, n\}_N$ Well formed

The Guarantees

The confounder N_A is a fresh number for every encryption. This prevents the information flow arising from encrypting the same data repeatedly. The protocol with confounders:

> Message 1 $B \rightarrow A$: N_B Message 2 $A \rightarrow B$: $\{M, N_B, N_A\}_{K_{AB}}$

Expressed in the spi calculus, A's part of the protocol looks like this:

$$m(n_B)(\nu K)(\nu n_A)\overline{c}\langle\{n_B,x,*,n_A\}_K\rangle$$

where c is a public channel and x has level Any.

It is possible to show that this typechecks. Thus it does not leak the value of x, in the sense that A[M/x] and A[N/x] are equivalent for all closed M and N.

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Typing – Values

$$\frac{E \vdash M : T \quad T \leqslant R}{E \vdash M : R} \qquad \frac{(\text{Level Var})}{\vdash E \text{ Well formed} \quad x : T \text{ in } E}}{\vdash E \text{ Well formed} \quad x : T \text{ in } E}$$

$$\frac{(\text{Level Name})}{\vdash E \text{ Well formed}} \qquad E \vdash n : T :: \{M_1, \dots, M_k, n\}_N$$

$$E \vdash n : T$$

$$\frac{(\text{Level Zero})}{E \vdash E \text{ well formed}} \qquad \frac{(\text{Level Suce})}{E \vdash M : T} \qquad \frac{(\text{Level Pair})}{E \vdash M : T} \qquad \frac{E \vdash M : T}{E \vdash M : T} \qquad E \vdash N : T$$

I yping - Values II vel Enc Public)

$$\frac{E \vdash M_1: T \dots M_k: T \quad E \vdash N: \texttt{Public}}{E \vdash \{M_1, \dots, M_k\}_N: T} \xrightarrow{T=\texttt{Public if } k=0}$$

(Level Enc Secret)
$$E \vdash n:T :: \{M_1,M_2,M_3,n\}_N$$

$$E dash M_1:$$
 Secret $E dash M_2:$ Any $E dash M_3:$ Public $E dash N:$ Secret

$$E dash \{M_1, M_2, M_3, n\}_N$$
 : Public

Typing - Processes II

$$\underbrace{\begin{array}{ccc} \text{(Level Match)} \\ E \vdash M : T & E \vdash N : R & E \vdash P \end{array}}_{\text{(Level Match)}}$$

here and below T,R not Any

$$E dash [M ext{ is } N].P$$
 (Level Pair Split)

$$E dash M: T = E, x:T,y:T dash P$$

$$E \vdash \mathsf{let}\ (x,y) = M \mathsf{ in } P$$

(Level Int Case)

$$\frac{E \vdash M : T' \quad E \vdash P \quad E, x : T \vdash Q}{F \vdash M \quad f \cap F}$$

$$E \vdash \mathsf{ case } M \mathsf{ of } 0 : P, \mathsf{ succ}(x) : Q$$

$$rac{E dash L: T \quad E dash N: ext{Public} \quad E, x_1: T, \ldots, x_k: T dash P}{E dash ext{ case } L ext{ of } \{x_1, \ldots, x_k\}_N ext{ in } P}$$

Level Dec Secret)

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$$\frac{E \vdash L : T \quad E \vdash N : \mathsf{Secret} \quad E, x_1 : \mathsf{Public}, x_2 : \mathsf{Any}, x_3 : \mathsf{Secret}, x_4 : \mathsf{Any} \vdash P}{E \vdash \mathsf{case} \ L \ \mathsf{of} \ \{x_1, x_2, x_3, x_4\}_N \ \mathsf{in} \ P} \\ \Longrightarrow$$

Typing – Processes

(Level Output Public) $E \vdash M$: Public $E \vdash M_1$: Public, ..., $E \vdash M_k$: Public $E \vdash P$ $E \vdash \overline{M}\langle M_1, \ldots, M_k \rangle.P$ (Level Output Secret) $E \vdash M$: Secret $E \vdash M_1$: Secret $E \vdash M_2$: Any $E \vdash M_3$: Public $E \vdash P$ $E \vdash \overline{M}\langle M_1, M_2, M_3 \rangle.P$ (Level Input Public) $E \vdash M$: Public E, x_1 : Public, \dots, x_k : Public $\vdash P$ $E \vdash M(x_1, \ldots, x_k).P$ (Level Input Secret) $E \vdash M : \mathsf{Secret}$ $E, x_1: \mathsf{Secret}, x_2: \mathsf{Any}, x_3: \mathsf{Public} \vdash P$ $E \vdash M(x_1, x_2, x_3).P$ (Level Par) (Level Res) (Level Nil) (Level Rep) $E \vdash P' \quad E \vdash Q$ $E, n: T:: L \vdash P$ $\vdash E$ well formed $E \vdash P \mid Q$ $E \vdash (\nu n)P$ $E \vdash \mathbf{0}$

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Secrecy by Typing

Thm: Secrecy

Let E be an environment with only variables of level Any and names of level Public in Dom(E). Let σ, σ' be substitutions of values for the variables which respect E.

If
$$E \vdash P$$
, then $P\sigma \cong P\sigma'$

In other words, if P is well typed, then no observer that can tell $P\sigma$ apart from $P\sigma'$, so it cannot detect differences in the value of any parameter of type Any.

roups for Secrecy: Scope extrusion revisited

$$p(x).O \mid (\nu s) \ \overline{p}\langle s \rangle.P$$

- ➤ The name s is initially private to P. One step of reduction passes it over to O. This may be desirable, as we have seen.
- ▶ But we may instead want to keep s from escaping its initial scope. Eg, s could be a secret, and O an opponent.
- > How can we do that?
- ightharpoonup one could say: $\overline{p}\langle s \rangle$ should not occur in P, ie s should not be sent on a channel known to the opponent.
- ➤ But this is not easily enforced: *p* may be obtained dynamically from some other channel, and may not occur at all in *P*.



Pi Calculus with Groups

Croups can be created dynamically

$$P ::= \ldots$$
 as before $(
u G)P$ group creation

Additional reduction

$$\blacktriangleright$$
 $(\nu G)P \longrightarrow (\nu G)Q$ if $P \longrightarrow Q$

Additional congruence rules

$$(\nu G_1)(\nu G_2)P \equiv (\nu G_2)(\nu G_1)P$$

 $(\nu G)(P \mid Q) \equiv P \mid (\nu G)Q$ if $G \notin fg(P)$
 $(\nu G)(\nu a : T)P \equiv (\nu a : T)(\nu G)P$ if $G \notin fg(T)$

Controlling scope extrusion

- ➤ The problem must be approached carefully: scope extrusion is a fundamental mechanism.
- ▶ Idea: classify names into groups, and isolate a group G for names that should be secret. Then declare $(\nu s:G)\overline{p}\langle s\rangle.P$.
- ➤ Clobal groups are of no use. Leakage can be made to typecheck:

$$p(y:G).O \mid (\boldsymbol{\nu}s:G)\overline{p}\langle s \rangle.P$$

- ➤ Groups themselves should be secret, so that *P* cannot output values of group *G* on public channels.
- ➤ A scope mechanism for groups:

$$p(y:T).O \mid (\nu G)(\nu s:G)\overline{p}\langle s\rangle.P$$

This will not typecheck if one tries to imply T = G, as G has local scope.



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Groups and reduction

> Groups have no computational impact:

$$\mathit{erase}((m{
u}G)P) \triangleq \mathit{erase}(P)$$
 $\mathit{erase}(a(\vec{x}:\vec{T}).P) \triangleq a(\vec{x}).\mathit{erase}(P)$ $\mathit{erase}((m{
u}x:T)P) \triangleq (m{
u}x)\mathit{erase}(P)$ $\ldots \triangleq \ldots$

- $ightharpoonup P \longrightarrow Q$ if and only if $\mathit{erase}(P) \longrightarrow R$, for some $R \equiv \mathit{erase}(Q)$.
- > They do, however, affect typing

Types and Judgements

- ➤ Channel Types
 - $ightharpoonup T, U ::= G[T_1, \ldots, T_n]$: polyadic channel in group G
- Type Environments
 - $ightharpoonup \Gamma ::= \varnothing \mid \Gamma, G \mid \Gamma, u : T$ lists, not sets (!)
- Additional judgements
 - $ightharpoonup \Gamma \vdash \diamond$: good environments
 - $ightharpoonup \Gamma \vdash T$: good types
 - ➤ Intuition:

 $\Gamma \vdash T$ iff all group names in T are declared in Γ .

 $\Gamma \vdash \diamond$ iff all types in Γ are well-formed



Typing Rules: processes

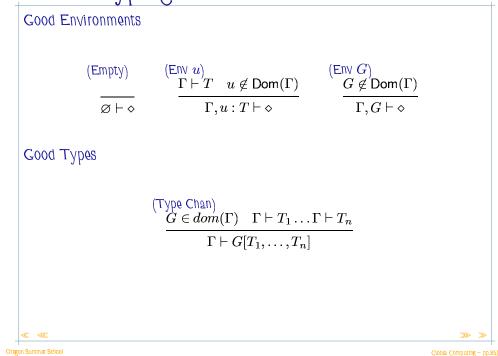
rocess typing as before, e.g.

$$\frac{\text{(Input)}}{\Gamma \vdash u : G[T_1, \dots, T_n] \quad \Gamma, x_1 : T_1, \dots, x_n : T_n \vdash P}{\Gamma \vdash u(x_1 : T_1, \dots, x_n : T_n)P}$$

ule for group creation

$$\frac{\overset{\text{(GR0S)}}{\Gamma,G\vdash P}}{\Gamma\vdash (\nu G)P}$$

Typing Rules: formation rules



Properties of the type system

- > Subject Reduction
 - If $\Gamma \vdash P : T$ and $P \longrightarrow Q$, then $\Gamma \vdash Q : T$.
- > Secrecy

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Let $S = p(y:U).O \mid (\nu G)(\nu x:G[\ldots])P$, and assume $\Gamma \vdash S$.

- \triangleright Then no process deriving from S outputs x along p.
- ightharpoonup Formally, for all processes Q, S' and S'', and contexts $\mathscr{C}[\cdot]$ such that

$$S \equiv (\nu G)(\nu x : G[\dots])S', \qquad S' \longrightarrow S'' \quad \text{ and } \quad S'' \equiv \mathscr{C}[\overline{p}\langle x \rangle . Q].$$

it is the case that p is bound by $\mathscr{C}[\cdot]$

Proof of secrecy

ssume:

$$\Gamma \vdash p(y:U).O \mid (\nu G)(\nu x:G[\dots])P$$

$$\longrightarrow (\nu G)(\nu x:G[\dots])\mathscr{C}[\overline{p}\langle x\rangle.Q]$$

vith p not bound in $\mathscr{C}[\cdot].$

- ightharpoonup By subject reduction $\Gamma, G, x : G[\dots] \vdash \mathscr{C}[\overline{p}\langle x \rangle.Q].$
- ightharpoonup This implies that $\Gamma, G, x : G[\ldots], \Gamma' \vdash \overline{p}\langle x \rangle.Q$ for some Γ'
- ightharpoonup Then $\Gamma, G, x : G[\dots], \Gamma' \vdash p : H[G[\dots]]$ for some H.
- Impossible:
 - $ightharpoonup \Gamma \vdash p(y:U).O \mid (\nu G)(\nu x:G[\ldots])P \text{ implies } p \in Dom(\Gamma)$
 - ➤ Thus we would have $\Gamma \vdash p : H[G[\dots]]$, but this judgement is not derivable because $G \not\in \mathsf{Dom}(\Gamma)$.

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Summary of Lecture II

- We studied the use of (elementary) types in the π calculus, starting simple sorts to protect tupling for programmers' errors, arriving to types to protect secrecy.
- We introduced subtyping as a natural way to manage capabilities and disclose different 'views' of the same object to different users.
- > We considered the why and how of typed equivalences.

Further Reading:

Again, the best starting points are:

- \blacktriangleright The π -calculus: A theory of mobile processes (Sangiorgi, Walker)
- ➤ The mobility home page http://lamp.epfl.ch/mobility/

Consider also

- ➤ The Spi Calculus (Abadi, Gordon)
- Secrecy by Typing in Security Protocols (Abadi)
- ➤ Secrecy and Group Creation (Cardelli, Ghelli, Gordon)

Untyped Opponents

Idea (simplified): extend the type system so that all processes type check trivially:

Secrecy Thm generalises to the case of untyped/ill-typed opponents

$$\frac{\Gamma \vdash n : \mathsf{Un} \quad \Gamma, \vec{x} : \tilde{\mathsf{Un}} \vdash P}{\Gamma \vdash n (\vec{x} : \tilde{\mathsf{Un}}) . P} \quad \frac{\Gamma \vdash n : \mathsf{Un} \quad \Gamma \vdash M_i : \mathsf{Un} \quad \Gamma \vdash P}{\Gamma \vdash \overline{n} \langle M_1, \dots, M_k \rangle P}$$

- Untyped opponents can be made to typecheck by annotating all their free/bound names/variables with the type Un.
- Prove subject reduction for the new system
- Derive generalized secrecy

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— Lecture III —

Asynchrony and Distribution

The Case for Asynchrony

et us move a step towards realistic networks, trying to embed <code>locations</code> in our alculi. As a first step, let us build a case for:

Synchrony. Channels in π are 'global' high-level, somehow unrealistic. Everybody an send and receive on them, regardless of location. The handshaking

$$\overline{x}.P \longleftrightarrow x.Q$$

epresents an instantaneous action at a distance unfeasible in distributed etworks, where localities, delays, and failures play a fundamental role distributed consensus (Lynch).

Iso summation can be criticised especially in 'mixed' forms like

$$x.P + \overline{x}.Q \mid \overline{x}.Q + x.P' + k$$

ynchronised choice at a distance very hard to implement.

lso, $\overline{x}\langle z
angle + y(z)$ makes little sense in general.

et us abandon synchronous remote communication...

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Asynchronous π

o continuation on output: $ar{x}\langle y
angle \mathcal{K}$

ontinuations can be simulated as: $\tau.(\bar{x}\langle y\rangle \mid P)$.

ow can ${\it P}$ know when and if the output is received? Well, in general it can't.

ut explicit continuations:

sender:
$$\tau.(\bar{x}\langle y\rangle\mid c_x.P')$$
 receiver: $x(y).(Q'\mid \bar{c}_x)$.

he synchronisation is now much looser, and widely accepted to be a better base or distributed systems

$$ightharpoonup$$
 Action prefixes $\pi := \overline{x} / x(y) \mid x(y)$

$$\blacktriangleright \ \, \text{Processes} \,\, P ::= \overline{x} \langle y \rangle \,\, | \,\, \sum_{i \in I} \pi_i.P_i \,\, | \,\, P \,\, | \,\, P \,\, | \,\, (\nu a)P \,\, | \,\, !P$$

synchronous calculi often do not consider sums nor au.

Roadmap of Lecture III

- \triangleright The asynchronous π calculus
- \triangleright The localised π calculus
- \triangleright The distributed π calculus
- The join calculus

π_A : Expressiveness

Polyadie π :

$$\{\overline{x}\langle y_1, y_2 \rangle\} \triangleq (\nu w) (\overline{x}\langle w \rangle \mid w(v).(\overline{v}\langle y_1 \rangle \mid w(v).\overline{v}\langle y_2 \rangle))$$
$$\{x(z_1, z_2).P\} \triangleq x(w)(\nu v)(\overline{w}\langle v \rangle \mid v(z_1)(\overline{w}\langle v \rangle \mid v(z_2).\{P\}))$$

Synchronisation:

$$[\overline{x}\langle y\rangle.P] \triangleq (\nu a)\overline{x}\langle y, a\rangle \mid a.[P]$$
$$[x(z).P] \triangleq x(z, a).(\overline{a} \mid [P])$$

EXECCISE: Compose $\{\ \cdot\ \}$ and $[\ \cdot\]$ above. Prove that it takes 2n+5 monadic asynchronous communications to exchange one n-pla.

 π_A : Expressiveness, II

ummation

OK
$$riangleq l(p,f).\overline{p}$$
 Fail $riangleq l(p,f).\overline{f}$

erms in the summation will compete to grab \overline{p} from OK. The loosers will either ang forever, or grab \overline{f} from Fall.

$$\begin{split} [x_1(y_1).P_1 + x_2(y_2).P_2] \triangleq \\ (\nu l) (\text{OK} \mid_{i=1,2} x_i(z).(\nu p f)(\overline{l}\langle p,f\rangle \mid p.(\text{Fall} \mid [P_i]) \mid f.(\text{Fall} \mid \overline{x_i}\langle z\rangle))) \end{split}$$

lixed choice cannot be encoded (satisfactorily).

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On Asynchronous Bisimulation

Vill the hypothesis of asynchrony bear consequences on bisimulation?

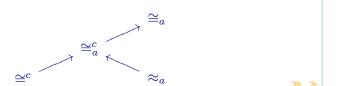
$$x(z).\overline{x}\langle z\rangle \stackrel{?}{=} \mathbf{0}$$

Matter of fact, with only asynchronous contexts, $\pi_A \triangleright !x(z).\overline{x}\langle z\rangle \cong^c \mathbf{0}$ his can be captured a LTS definition.

Synchronous Bisimulation
$$pprox_a$$
: the largest equivalence s.t. for all $Ppprox_a Q$ $P \xrightarrow{lpha} P'$ for $lpha \in \{\overline{x}u,
u\overline{x}z, au\}$ then $Q \stackrel{\hat{lpha}}{\Longrightarrow} pprox_a P'$

$$P \xrightarrow{xy} P'$$
then $Q \Longrightarrow \approx_a P'$ or $Q \Longrightarrow Q'$ for $P' \approx_a Q' \mid \overline{x}\langle y \rangle$

Ote: Alternatively the 2nd clause: if $P\!\downarrow_x$, then $P\mid \overline{x}\langle y\rangle \approx_a Q\mid \overline{x}\langle y\rangle$ for all y.



π_L : The Local π calculus

Only the Output capability can be received on names (either by typing or by syntactic restrictions). It makes a lot of sense in practice (eg printer, objects, distributed environment, ...). As a consequence, all the 'receivers' for a channel are local to the scope. One of the semantics consequence:

$$\pi_L \triangleright (\nu z) \overline{x} \langle z \rangle \cong^c (\nu z) (\overline{x} \langle z \rangle \mid \overline{z} \langle y \rangle)$$

Simulating read capabilities.

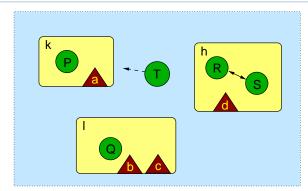
We represent a name x of π_A with a pair $\langle x^o, x \rangle$ of π_L , whose first component represent the (lost) read capability on x.

$$\begin{split} x^o &\hookrightarrow x \triangleq ! x^o(z).x(s,t).\overline{z}\langle s,t\rangle \\ & [\overline{a}\langle x\rangle]_{\mathscr{E}} \triangleq (\nu x^o)(\overline{a}\langle x^o,x\rangle \mid x^o \hookrightarrow x) \\ & [a(x).P]_{\mathscr{E}} \triangleq \left\{ \begin{array}{l} a(z^o,z).[P]_{\mathscr{E} \cup \{z\}} & \text{if } a \not \in \mathscr{E} \\ (\nu w)(\overline{a}^o\langle w\rangle \mid w(z^o,z).[P]_{\mathscr{E} \cup \{z\}} \end{array} \right. \end{split}$$

We will see later the Join Calculus, which originated the idea of unique receptors.

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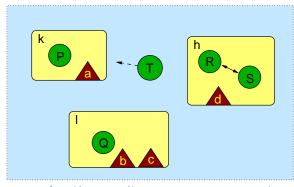
The Case for Distribution



Distributed Systems consist of:

- ➤ A collection of independent distributed sites offering Services / resources to migrating agents.
 - Resources: All sort of things a agent may long for (CPU time, space, printers, ...); we will model them as π -calculus channels for now.
- Agents: mobile processes of general nature; we will model them by augmented π -calculus processes.

The Case for Distribution



lore precisely... Add locations or sites, remove direct remote communication.

he basic elements are:

- \blacktriangleright Locations are sites containing processes: l[P]
- ightharpoonup Communication is only local: $l[\overline{x}\langle z\rangle.P \mid x(y).Q]] \longrightarrow l[P \mid Q\{z/y\}]$
- ightharpoonup Agents travel between locations $l[\![\![\![\!]\!]\!]$ goto k . $P\mid Q]\!]\mid k[\![\![\![\!]\!]\!]\mid k[\![\![\![\!]\!]\!]\!] \to l[\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\mid k[\![\![\![\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\mid k[\![\![\![\![\!]\!]\!]\mid k[\![\![\![\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\![\![\!]\!]\mid k[\![\![\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\!]\!]\mid k[\![\![\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\![\![\!]\!]\mid k[\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\!]\!]\mid k[\![\!]\!]\mid k[\![\![\!]\!]\mid k[\![\!]\!]\mid k[\!$

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The distributed π calculus

- ightharpoonup Values: $V::=l\mid c\mid c$ @l
- ➤ Sites: $M ::= 0 \mid l \llbracket P \rrbracket \mid M \mid M \mid (\nu e @ l : T) M$

Example: $h[P] \mid (\nu a @l)(k[\ldots a @l \ldots] \mid l[\ldots a \ldots])$

Threads:

 $u(\vec{x}:\vec{T})Q$ local input on channel u $\overline{u}\langle V\rangle Q$ local output on channel u

goto uP code movement to site u

[u=v]P; Q testing of names

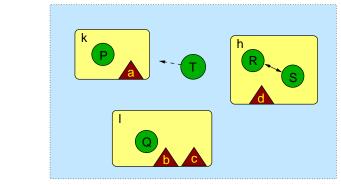
 $(\nu e:T)P$ generation of new names (channels or locations)

 $P \mid Q$ composition

!P replicationfinished

Example: $l\llbracket d(x@z)P \rrbracket \mid k\llbracket (\nu a) \operatorname{goto} l.\overline{d}\langle a@k \rangle \rrbracket$

The Case for Distribution



Agent Migration

This opens a lot of interesting "global" issues

- ➤ Which resource are available at a given location?
- ➤ How do we make sure their are used accordingly?

The use of types to control resource access and usage is an important current topic.

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Semantics

Structural congruence

- $ightharpoonup l[\![P]\!] = l[\![P]\!] \mid k[\![Q]\!]$

Reduction Semantics

- $ightharpoonup k \llbracket \overline{c}\langle v \rangle.Q \mid c(x:T)P \rrbracket \longrightarrow k \llbracket Q \mid P\{v/x\} \rrbracket$
- $ightharpoonup k \llbracket \operatorname{goto} \operatorname{l} P \rrbracket \longrightarrow \operatorname{l} \llbracket P \rrbracket$

The famous Cell (yet again)

et us reconsider the the cell and write a distributed version.

 \triangleright g – inputs a location; the location MUST have a channel called ret on which to return value

ightharpoonup p – inputs a location and new value; location must have a channel ack on which to send acknowledgement.

$$\begin{aligned} \operatorname{Cell}(n) &\triangleq (\boldsymbol{\nu}s)(\overline{s}\langle n\rangle \mid \boldsymbol{!}g(y).s(x).(\overline{s}\langle x\rangle \mid \operatorname{goto} y.\overline{\operatorname{ret}}\langle x\rangle) \\ & \quad | \boldsymbol{!}p(y,v).s(x)(\overline{s}\langle v\rangle \mid \operatorname{goto} y.\overline{\operatorname{ack}}\langle\rangle) \end{aligned}$$
 User $\triangleq \operatorname{goto} l.\overline{p}\langle h,0\rangle \mid \operatorname{ack}().\operatorname{goto} l.\overline{g}\langle h\rangle \mid \operatorname{ret}(x) \overline{\operatorname{print}}\langle x\rangle$

System $\triangleq l[Cell(v)] \mid h[User]$

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A Cell Factory

ere is a (final) version, where a new private cell is created for each user.

$$\operatorname{System} \triangleq s \llbracket \mathbf{S} \rrbracket \mid h_1 \llbracket \mathbf{U} \mathbf{Ser}_1 \rrbracket \mid h_2 \llbracket \mathbf{U} \mathbf{Ser}_2 \rrbracket$$

$$\mathbf{S}\triangleq \operatorname{!req}(z\mathbf{@}y).\ (\boldsymbol{\nu}c)(y::\overline{z}\langle c\rangle\ |\ \operatorname{goto}\ c\,.\mathsf{Cell}(0))$$

$$\mathsf{USer}_i \triangleq (\boldsymbol{\nu}r)(s::\overline{\mathsf{req}}\langle r\mathbf{@}h_i\rangle \mid r(z).\mathsf{USer}_i(z))$$

Evolution of the System

$$s\llbracket \mathtt{S} \rrbracket \mid h_1\llbracket \mathtt{USer}_1 \rrbracket \mid h_2\llbracket \mathtt{USer}_2 \rrbracket$$

$$\longrightarrow s\llbracket \mathbb{S} \rrbracket \ (\nu c_1)(c_1\llbracket \mathsf{Cell}(0) \rrbracket \ | \ h_1\llbracket \mathsf{User}_1 \rrbracket) \ | \ h_2\llbracket \mathsf{User}_2 \rrbracket$$

$$\longrightarrow s\llbracket \mathbb{S} \rrbracket \left(\nu c_1 \right) \left(c_1 \llbracket \mathsf{Cell}(0) \rrbracket \mid h_1 \llbracket \mathsf{USer}_1 \rrbracket \right) \mid \left(\nu c_2 \right) \left(c_2 \llbracket \mathsf{Cell}(0) \rrbracket \mid h_2 \llbracket \mathsf{USer}_2 \rrbracket \right) \\ \longrightarrow \dots$$

Exercise:

Program a remote channel creation and a newloc construct.

 \triangleright Program a forwarder from in@a to out@b

A refined cell

In order to use the cell, users have to have a ack and a reply channel. Here is a version where these are generated on purpose and communicated from the client to the cell.

```
System \triangleq l[Cell(v)] \mid h[User]
```

$$\mathsf{USer} \triangleq (\boldsymbol{\nu}ar)\,l :: \overline{p}\langle a@h, 0\rangle \mid a()(l :: \overline{g}\langle r@h\rangle \mid r(x).\overline{\mathsf{print}}\langle x\rangle)$$

$$\begin{aligned} \mathsf{Cell}(n) &\triangleq (\boldsymbol{\nu}s)(\overline{s}\langle n\rangle \mid !g(z@y).s(x).(\overline{s}\langle x\rangle \mid y :: \overline{z}\langle x\rangle) \\ & |!p(z@y,v).s(x).(\overline{s}\langle v\rangle \mid y :: \overline{z}\langle \rangle) \end{aligned}$$

Notation: calling a method at a location: $l:: \overline{a}(v)$ shorthand for goto $l.\overline{a}(v).0$.



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Types for Resource Access Control

Location types: Key notion: describe the services available at a site.

$$\mathsf{loc}[s_1:T_1,\ldots,s_n:T_n]$$

The purpose of the type system is to guarantee that incoming agents access only the resources granted to them, in the way granted to them. This is called

Resource Access Control.

Example: comp $f[req(x : int, ret@l : \sharp(int)@loc).l :: \overline{ret}\langle fx \rangle]]$. Then,

comp_f : loc[req : i(int, \pmu(int) @loc)]

Suptyping:

ubtyping plays a central role in access control policies:

$$\frac{\left(\text{Sub Loe}\right)}{\text{loc}[\vec{s}:\vec{S},s_k:S_k]\leqslant \text{loc}[\vec{s}:\vec{T}]}$$

The receiver gains capabilities according to the type of the location. Using abtyping the sender can control this.

Or instance, a receiver of I over a channel carrying loc[a:iV,h:oW] will be

or instance, a receiver of l over a channel carrying loc[a:iV,b:oW] will be able to read V-values over a and write W-values to b, but not to use any other esource possibly present at l (and hidded by subtyping).

$$\frac{A \leqslant A' \quad L \leqslant L'}{A@L \leqslant A'@L'}$$

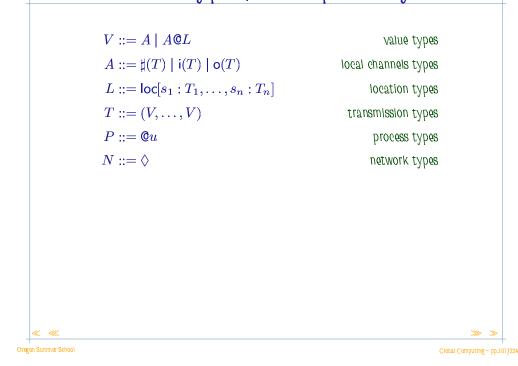
et us study the types of the previous examples, and unveil some of the issues evolved.

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A feel for the rules

The Types, more precisely



Typing the cell

```
The simple cell  \begin{aligned} \operatorname{Cell}(n) &\triangleq (\nu s: \sharp V)(\overline{s}\langle n\rangle \,|\, !g(z@y: oV@loc).s(x:V).(\overline{s}\langle x\rangle \,|\, y:: \overline{z}\langle x\rangle) \\ &\quad |\, !p(z@y: o(\operatorname{unit})@c, v:V).s(x:V).(\overline{s}\langle v\rangle \,|\, y:: \overline{z}\langle \rangle) \end{aligned}  cell : CELL = \operatorname{loc}[g: \sharp(oV@loc), p: \sharp(o(\operatorname{unit})@loc, V)] The cell factory  \mathbf{S} &\triangleq !\operatorname{req}(z@y: o(\operatorname{CELL})@loc). \ (\nu c: \operatorname{CELL})(y:: \overline{z}\langle c\rangle \,|\, \operatorname{goto} c.\operatorname{Cell}(0))   \mathbf{S} : \operatorname{loc}[\operatorname{req}: \sharp(o(\operatorname{CELL})@loc)]
```

Dynamic Types

```
onsider a generic system
```

```
\mathsf{server}\llbracket \dots | \ !\mathsf{quest}(v:V,x@l:\mathsf{o}(\mathsf{ANSW})@\mathsf{loc})\dots l :: \overline{x}\langle \mathsf{answ}\rangle \rrbracket
```

The type of server:

$$Serv \triangleq loc[quest : \sharp(V, o(ANSW)@loc), \ldots]$$

low, suppose that ellent wants to setup a 'private' service, so that answers to lest's can reach only it.

```
\begin{split} \text{client} & [\hspace{-0.1em}[\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}|\hspace{-0.1em}
```

The move capability

dd a new component of types which allows to control movements. Consider

$$M ::= \dots \log[\mathsf{move}_{\ell}, \vec{x} : \vec{T}]$$

he obvious typing rule is

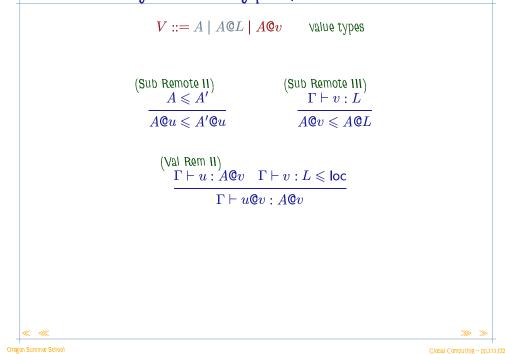
$$\frac{\overset{\mathsf{(MOVe)}}{\Gamma \vdash k} : \mathsf{loc}[\mathsf{move}_\ell] \qquad \Gamma \vdash P : @k}{\Gamma \vdash \mathsf{goto}\, k \,.P : @\ell}$$

imilarly, one can add a capability new_ℓ to allow processes from ℓ to create new hannels at a given location k. And more.

xample: A confidential account

$$\begin{aligned} & \textbf{bank} [\![\texttt{!new account}(y @ z : \sharp W @ \texttt{loc}, _ @ a : \texttt{i}() @ \texttt{Agent}) \\ & (\textbf{ν} \texttt{loc} : [\texttt{move}_a, \texttt{withdraw} : \ldots, \texttt{deposit} : \ldots]) \ldots]\!] \end{aligned}$$

Dynamic Types, Resolved



Location Typed Bisimulation

Question: Does this affect the behavioural equivalences?

$$k \llbracket \overline{b} \langle \rangle \rrbracket \stackrel{?}{\cong^c} k \llbracket \mathbf{0} \rrbracket$$

Of course. The impact of types with locations is even greater than before. Whether the equivalence above holds depends on Γ . Precisely, can we move to k to observe b?

Consider

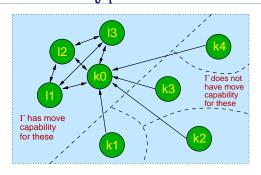
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$$(\boldsymbol{\nu}\boldsymbol{k}: \mathsf{loc}[\boldsymbol{a}:\sharp(),\mathsf{move}_{h_1}])\,h_1[\![\overline{\boldsymbol{d}}\langle\boldsymbol{k}\rangle]\!]\,|\,h_2[\![\overline{\boldsymbol{c}}\langle\boldsymbol{k}\rangle]\!]\,|\,k[\![\overline{\boldsymbol{a}}\langle\rangle]\!]$$

$$(\boldsymbol{\nu}\boldsymbol{k}: \mathsf{loc}[\boldsymbol{a}:\sharp(),\mathsf{move}_{h_1}])\,h_1[\![\overline{\boldsymbol{d}}\langle\boldsymbol{k}\rangle]\!]\,|\,h_2[\![\overline{\boldsymbol{c}}\langle\boldsymbol{k}\rangle]\!]\,|\,k[\![\boldsymbol{0}]\!]$$

They are equivalent if Γ contains: $d: \mathsf{i}(\mathsf{loc}[\mathsf{move}])$ and $c: \mathsf{i}(\mathsf{loc}[a:\sharp()])$ and it is not possible to move between h_1 and h_2 .

rocation Typed Risimulation



et \mathcal{T} be the collection of locations (e.g. $\{k1, k2, k3, k4\}$) for which Γ does not ave move capability but the environment may a priori have code running at.

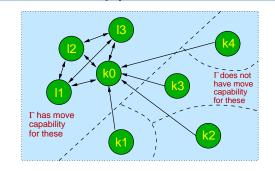
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Labelled transition system example rules

- $ightharpoonup \Gamma_{k0}$ contains move capability for l
- \blacktriangleright and Γ_{k0} contains read capability for a at l for values of type T
- $\qquad \text{then } (\overline{\Gamma}\rhd l[\![\overline{a}\langle v\rangle.P]\!]) \xrightarrow{l::\overline{a}v} (\overline{\Gamma}\sqcap_{\pmb{k}0}v:T@l\rhd P)$
- $ightharpoonup \Gamma_{k0}$ does not contain move capability at $k \in \mathscr{T}$
- \triangleright and Γ_k contains read capability for a at k for values of type T
- $\rightarrow \text{ then } (\overline{\Gamma} \rhd k \llbracket \overline{a} \langle v \rangle. P \rrbracket) \xrightarrow{k:: \overline{a} v} (\overline{\Gamma} \sqcap_k v : T@l \sqcap_{k0} v : T@l \rhd P)$

rocation Typed Bisimulation



Transition of the form: $(\overline{\Gamma}\rhd M)\stackrel{\alpha}{\longrightarrow} (\overline{\Gamma}'\rhd M')$ where $\overline{\Gamma}$ is of the form $(\Gamma_{k0},\Gamma_{k1},\ldots,\Gamma_{kn})$ for $\mathscr{T}=\{k1,\ldots,kn\}$ such that

$$\Gamma_{k0}\leqslant\Gamma_{ki}$$
 for each $ki\in\mathscr{T}$

- Knowledge gained at any li is learned in Γ_{k0}
- \blacktriangleright Knowledge gained at ki is learned in Γ_{ki} and Γ_{k0}

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Full abstraction

Thm

With the simplifying assumption in place that all move capabilities are of the form $move_*$ (that is everybody is allowed in, or nobody is) then, for all systems of $D\pi$ and all $\mathscr T$ we have

$$\Gamma \rhd M \cong^c N \quad \text{iff} \quad \overline{\Gamma}_{\nabla} \rhd M \approx^{\mathscr{T}} N$$

where $\overline{\Gamma}_{\nabla}=(\Gamma,\Gamma,\ldots,\Gamma)$ and $\approx^{\mathscr{T}}$ is the bisimulation equivalence induced by the labelled transition system.

Open issues:

- Remove the simplifying assumption about move capabilities
- Other capabilities: permission to exit, permission to create new channels,

The Join Calculus

he Join Calculus (aka the Reflexive Chemical Abstract Machine): a version of synchronous π combining restriction, reception, and replication in one construct:

Join receptor: $J \triangleright P$.

or example the definition

$$\texttt{def apply} \langle \texttt{f}, \texttt{x} \rangle \triangleright \texttt{f} \langle \texttt{x} \rangle$$

efines apply that receives two arguments and applies the first to the second, as

nown by the reduction:

$$\mathsf{def}\;\mathsf{apply}\langle \mathtt{f},\mathtt{x}\rangle\, \triangleright\, \mathtt{f}\langle\mathtt{x}\rangle\;\mathsf{in}\;\mathsf{apply}\langle \mathtt{g},\mathtt{y}\rangle \quad \longrightarrow \quad \mathsf{def}\;\mathsf{apply}\langle \mathtt{f},\mathtt{x}\rangle\, \triangleright\, \mathtt{f}\langle\mathtt{x}\rangle\;\mathsf{in}\;\mathsf{g}\langle\mathtt{y}\rangle$$

Notice:

This is very similar to $(\nu \text{apply})(!\text{apply}(x,y).\overline{x}\langle y\rangle \mid \overline{\text{apply}}\langle g,y\rangle)$ in π_A . In general, def D in P corresponds to a π form of the kind $(\nu \vec{d})(! \lceil D \rceil | \lceil P \rceil)$

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(red)

The RCHAM Semantics

effexive Chemical Abstract Machine: Structural rules \rightleftharpoons plus reduction \rightarrow : tates of the RCHAM are expression of the form $D \models P$, where P are the unning processes and D are the (chemical) reactions.

$$(\text{str-join}) \qquad \qquad \models P \mid Q \qquad \qquad \rightleftharpoons \qquad \qquad \models P, Q$$

$$\begin{array}{lll} (\text{str-join}) & & \models P \mid Q & \; \rightleftharpoons & \; \models P,Q \\ \\ (\text{str-def}) & & \models \det D \text{ in } P & \; \rightleftharpoons & \; D_{\sigma_{dv}} \models P_{\sigma_{dv}} & \sigma_{dv} \text{ instantiates } dv(D) \text{ freshly} \end{array}$$

 $J \triangleright P \models J_{\sigma_{rv}} \qquad \qquad \rightarrow \quad J \triangleright P \models P_{\sigma_{rv}} \quad \sigma_{rv} \text{ substitutes for } rv(J)$

$$\models \mathsf{def}\ x\langle z\rangle \triangleright x\langle z,z\rangle\ \mathsf{in}\ x\langle a\rangle\ |\ \mathsf{def}\ x\langle z\rangle \triangleright x\langle x,z,z\rangle\ \mathsf{in}\ x\langle b\rangle$$

$$\Longrightarrow k\langle z \rangle \rhd k\langle z,z \rangle \models k\langle a \rangle, \text{def } x\langle z \rangle \rhd x\langle x,z,z \rangle \text{ in} x\langle b \rangle$$

$$\rightleftharpoons k\langle z\rangle \triangleright k\langle z,z\rangle, r\langle z\rangle \triangleright r\langle r,z,z\rangle \models k\langle a\rangle, r\langle b\rangle$$

$$\rightarrow k\langle z\rangle \triangleright k\langle z, z\rangle, r\langle z\rangle \triangleright r\langle r, z, z\rangle \models k\langle a, a\rangle, r\langle b\rangle$$

$$\rightarrow k\langle z\rangle \triangleright k\langle z,z\rangle, r\langle z\rangle \triangleright r\langle r,z,z\rangle \models k\langle a,a\rangle, r\langle r,b,b\rangle$$

$$\begin{tabular}{l} \rightleftharpoons & \end{tabular} \begin{tabular}{l} \rightleftharpoons & \end{tabular} \begin{tabular}{l} \deg x\langle z\rangle \rhd x\langle z,z\rangle \ \mbox{in} \ x\langle x,b,b\rangle \\ & \end{tabular} \begin{tabular}{l} \rightleftharpoons & \end{tabular} \begin{tabular}{l} \bowtie & \end{tabular} \begin{tabular}{l} \rightleftharpoons & \end{tabular} \begin{tabular}{l} \bowtie & \end{tabular} \be$$

I ue syntax

P,Q ::= $x\langle \widetilde{V} \rangle$ Processes Asynchronous message on xdef D in PDefinition of D in P $P \mid Q$ Parallel Composition **Empty Process** Join patterns J,J' ::= $x\langle \tilde{y} \rangle$ Asynchronous reception on x $J \mid J'$ Joining messages Definition $D, E ::= J \triangleright P$ Elementary clause $D \wedge E$ Simultaneous definition $V, V' ::= \tilde{x}$ Values Names The only synchronisation primitive is the Join pattern: $\operatorname{def} x\langle z_1 \rangle \mid y\langle z_2 \rangle \triangleright Q \text{ in } P$

Example: Join pattern

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def ready(printer) | print(file) > printer(file) in Preduces only in the presence of messages on both ready and print, concurrently def ready(printer) | print(file) > printer(file) in ready(gutenberg) | print("slides.ps") | Q→ def ready(printer) | print(file) > printer(file) gutenberg("slides.ps") | Q

The same behavior is obtained by composing the definitions of apply and printer

 $\mathsf{def} \; \mathsf{apply} \langle \mathsf{f}, \mathsf{x} \rangle \triangleright \mathsf{f} \langle \mathsf{x} \rangle \; \wedge \; \mathsf{ready} \langle p \rangle \; | \; \mathsf{print} \langle f \rangle \triangleright \mathsf{apply} \langle p, f \rangle$

Derived constructs

$$P,Q ::= f(\widetilde{V}); P \qquad \text{Sequential Composition}$$

$$\text{let } \widetilde{x} = \widetilde{V} \text{ in } P \qquad \text{Named Values}$$

$$\text{reply } \widetilde{V} \Rightarrow f \qquad \text{Implicit Continuation}$$

$$J,J' ::= f(\widetilde{x}) \qquad \text{Synchronous reception on } f$$

$$V,V' ::= f(\widetilde{V}) \qquad \text{Synchronous Call}$$

$$\lfloor f(\widetilde{u}) \rfloor \qquad \triangleq f(\widetilde{v}), \kappa_f \rangle \qquad \text{(join pattern)}$$

$$\lfloor \text{reply } \widetilde{V} \Rightarrow f \rfloor \qquad \triangleq \kappa_f \langle \widetilde{V} \rangle \qquad \text{(process)}$$

$$\lfloor x \langle \widetilde{V} \rangle \rfloor \qquad \triangleq \text{let } \widetilde{u} = \widetilde{V} \text{ in } x \langle \widetilde{u} \rangle \qquad \text{(asynchronous call)}$$

$$\lfloor \text{let } \widetilde{u} = f(\widetilde{V}) \text{ in } P \rfloor \qquad \triangleq \text{def } \kappa \langle \widetilde{u} \rangle \triangleright P \text{ in } f \langle \widetilde{V}, \kappa \rangle \qquad \text{(synchronous call)}$$

$$\lfloor \text{let } \widetilde{u} = \widetilde{v} \text{ in } P \rfloor \qquad \triangleq \text{def } \kappa \langle \rangle \triangleright P \text{ in } f \langle \widetilde{V}, \kappa \rangle \qquad \text{(sequencing)}$$

The cell in Join

$$\models \operatorname{def} \operatorname{cell}[s\langle x\rangle \mid \operatorname{get}\langle r\rangle \rhd r\langle x\rangle \mid s\langle x\rangle \land \\ s\langle x\rangle \mid \operatorname{put}\langle v\rangle \rhd s\langle v\rangle : s\langle 0\rangle] \text{ in } \operatorname{get}\langle x\rangle; \operatorname{put}\langle 2\rangle \\ \longrightarrow \operatorname{cell}[D:s\langle 0\rangle] \models \operatorname{get}\langle x\rangle; \operatorname{put}\langle 2\rangle \longrightarrow D \models_{\operatorname{cell}} s\langle 0\rangle \parallel \models \operatorname{get}\langle x\rangle; \operatorname{put}\langle 2\rangle \\ \longrightarrow D \models_{\operatorname{cell}} s\langle 0\rangle \mid \operatorname{get}\langle x\rangle \parallel \models \operatorname{put}\langle 2\rangle \longrightarrow D \models_{\operatorname{cell}} s\langle 0\rangle \mid x\langle 0\rangle \parallel \models \operatorname{put}\langle 2\rangle \\ \longrightarrow D \models_{\operatorname{cell}} s\langle 0\rangle \mid x\langle 0\rangle \mid \operatorname{put}\langle 2\rangle \longrightarrow D \models_{\operatorname{cell}} s\langle 2\rangle \mid x\langle 0\rangle \longrightarrow \\ \models \operatorname{def} \operatorname{cell}[s\langle x\rangle \mid \operatorname{get}\langle r\rangle \rhd r\langle x\rangle \mid s\langle x\rangle \land \\ s\langle x\rangle \mid \operatorname{put}\langle v\rangle \rhd s\langle v\rangle : s\langle 2\rangle] \text{ in } x\langle 0\rangle$$

Xercise: Program a mobile cell.

Distributed Join Calculus

The distributed reflexive chemical abstract machine (DRCHAM) is a multiset of "located" RCHAMs $D_1 \models_{\rho_1} P_1 \| \cdots \| D_k \models_{\rho_k} P_k$ Each of these is a running location, and they are related to each other by a sublocation relation: $\models_{\phi} \text{ is a sublocation of } \models_{\rho} \text{ if } \rho \text{ is a prefix of } \phi.$ $(\text{str-loc}) \qquad a[D:P] \models_{\rho} \qquad \models_{\rho} \| D \models_{\rho a} P \qquad (a \text{ frozen})$ $(\text{comm}) \qquad \models_{\phi} x \langle \tilde{v} \rangle \parallel J \triangleright P \models \qquad \models_{\phi} \parallel J \triangleright P \models x \langle \tilde{v} \rangle \qquad (x \in dv(J))$ $(\text{move}) \ a[D:P|go\langle b,\kappa\rangle] \models_{\phi} \parallel \models_{\psi b} \qquad \models_{\phi} \parallel a[D:P|\kappa\langle\rangle] \models_{\psi b}$ Notice: $\blacktriangleright \text{ Remove messages are forwarded to the unique solution where they are}$

Summary of Lecture III

- We studied asynchrony in the π calculus and its consequences on behavioural equivalences.
- ightharpoonup We considered a distributed π calculus and a notion of typed equivalence.
- We introduced the distributed join calculus.

defined. There the usual (red) applies.

The entire location moves, not the thread.

> Further Reading:

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Again, the best starting points are:

- \blacktriangleright The π -calculus: A theory of mobile processes (Sangiorgi, Walker)
- ➤ The mobility home page http://lamp.epfl.ch/mobility/

Consider also

- \blacktriangleright Asynchronous π (Boudol), (Honda, Tokoro)
- \blacktriangleright Comparing Synchronous and Asynchronous π (Palamidessi)
- ➤ Decoding Choice Encodings (Pierce, Nestmann)
- ➤ On Asynchronous Bisimulation (Amadio, Castellani, Sangiorgi)
- > Access and Mobility Control in Distributed Systems (Hennessy, Rathke, et al)
- Join Calculus (Fournet, Conthier, et al) http://pauillac.inria.fr

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— Lecture VI —

Ambient Mobility

The roadmap

- ➤ Mobile Ambients
- ➤ Typing ambients
- Boxed Ambients
- > Types for access control in ambients

Open networks and mobile agents

- Distribution over wide-area networks introduces new issues and breaks many of assumptions usually made in concurrent systems. We have already discussed asynchrony.
- > Other examples:
 - existence of explicit physical locations determines latency in communication,
 - ➤ existence of virtual locations enforcing security policies that can restrict access to resources or even the visibility of locations.
- Mobile Ambients: a calculus of locations with migration primitives sufficiently expressive to encode the π-calculus, and presenting a new idea:

Modelling Environment Mobility



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Overview

Mobile Ambients:

- \blacktriangleright Are named agents: n[P]
- ➤ Represent computational environments, containing data and live computations: $n[P \mid \langle M \rangle]$
- \triangleright Can be nested: n[m[P] | k[Q]]
- Move under the control of their enclosed processes: $n[\text{in } m.P] \mid m[Q]$ This is dubbed (subjective mobility).

Provide a direct representation of the structured nature of physical or administrative domains as well as of mobile computational environments.

The Essence of Mobile Ambients

Subjective movements

$$\begin{array}{c} n[\text{ in } m.P \mid Q \] \mid m[\ R \] \longrightarrow m[\ n[\ P \mid Q \] \mid R \] \\ m[\ n[\text{ out } m.P \mid Q \] \mid R \] \longrightarrow n[\ P \mid Q \] \mid m[\ R \] \end{array}$$

Process interaction

$$n[\ \langle M \rangle.P\ |\ (x).Q\] \longrightarrow n[\ P\ |\ Q\{M/x\}\],$$

Boundary dissolver

open
$$n.P \mid n[Q] \longrightarrow P \mid Q$$
.

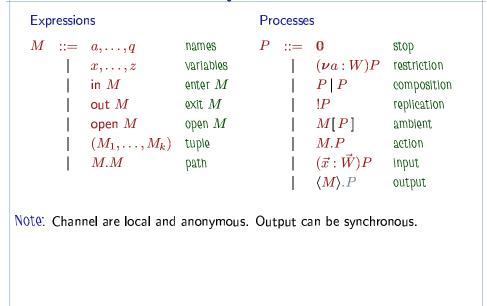
Structural Congruence

- \blacktriangleright $(M.M').P \equiv M.(M'.P)$
- $\blacktriangleright (\nu a: W)b[P] \equiv b[(\nu a: W)P]$ for $a \neq b$
- $\triangleright (\nu a: W)\mathbf{0} \equiv \mathbf{0}$

 $Q \equiv Q$

- $(\boldsymbol{\nu}a:W)a[\mathbf{0}] \equiv \mathbf{0}$
- \blacktriangleright $(\nu a:W)(\nu b:W')P \equiv (\nu b:W')(\nu a:W)P$ for $a \neq b$
- \triangleright $(\nu a; W)(P \mid Q) \equiv P \mid (\nu a : W)Q$ for $a \notin fn(P)$
- \triangleright ! $P \equiv !P \mid P$,
- usual rules for symmetricity, associativity and identity

Syntax



Mobility: An example

Firewalls

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An agent crosses a firewall by means of passwords k, k_1 and k_2 . The firewall, with secret name w, sends out the pilot ambient k to guide the agent inside.

Firewall
$$\triangleq (\nu w)w[k[$$
 out $w.$ in $k_1.$ in $w]$ $|$ open $k_1.$ open $k_2.P]$
Agent $\triangleq k_1[$ open $k.k_2[Q]$ $]$

- ightharpoonup Agent exhibits the passwd k_1 using k_1 as wrapper ambient
- \triangleright Firewall verifies that agent knows the passwd with in k_1
- \triangleright in w carries the agent into the firewall
- $ightharpoonup k_2$ prevents Q from interfering with the protocol

A run of the protogol

Firewall $\triangleq (\nu w)w[k]$ out w in k_1 in w | open k_1 open k_2 .P | Agent $\triangleq k_1$ [open $k.k_2$ [Q]]

Firewall Agent

- $\longrightarrow (\nu w)k[\text{in } k_1.\text{in } w] \mid w[\text{open } k_1.\text{open } k_2.P] \mid k_1[\text{open } k.k_2[Q]]$
- $\longrightarrow (\nu w)w[\text{open }k_1.\text{open }k_2.P] \mid k_1[k[\text{in }w] \mid \text{open }k.k_2[Q]]$
- $\longrightarrow (\nu w)w[\text{open }k_1.\text{open }k_2.P] \mid k_1[\text{in }w \mid k_2[Q]]$
- $\rightarrow (\nu w)w[\text{open } k_1.\text{open } k_2.P \mid k_1[k_2[Q]]]$
- $\longrightarrow (\nu w)w[\text{open } k_2.P \mid k_2[Q]]$
- $\longrightarrow (\nu w)w[P \mid Q]$

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Reduction: structural rules

o surprises ...

$$\frac{P \longrightarrow P'}{P \mid Q \longrightarrow P' \mid Q} \qquad \frac{P \longrightarrow P'}{(\nu a : W)P \longrightarrow (\nu a : W)P'}$$

$$\frac{(\mathsf{Amb})}{a[\,P\,] \longrightarrow a[\,P'\,]} \qquad \frac{(\mathsf{Cong})}{P \equiv P' \quad P' \longrightarrow Q' \quad Q' \equiv Q}{P \longrightarrow Q}$$

. but note that processes inside ambients reduce

ambients are active while moving

Reduction: communication

(Comm) $(x)P \mid \langle M \rangle \longrightarrow P\{M/x\}$ local, asynchronous and anonymous Remote communication must be encoded. ➤ To realise: $a[\text{send } M \text{ to } b \mid P] \mid b[\text{get}(x) \text{ from } a.Q \mid R]$ we use a 'taxi' ambient to transport a packet with M: $(\nu n)(a[n[\text{out }a.\text{in }b \mid \langle M \rangle] \mid P] \mid b[\text{open }n \mid (x)Q \mid R])$ $\longrightarrow (\nu n)(a[P] \mid n[\text{in } b \mid \langle M \rangle] \mid b[\text{open } n \mid (x)Q \mid R])$ $\longrightarrow (\nu n)(a[P] | b[\text{open } n | n[\langle M \rangle] | (x)Q | R])$ $\longrightarrow a[P] | b[\langle M \rangle | (x)Q | R]$ $\longrightarrow a[P] \mid b[Q\{M/x\} \mid R]$ Oregon Summer School

Types: overview

- Idea: ambients are places of conversation
- > multiple processes within an ambient can freely execute input and output actions:

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since messages are not directed to a particular channel, it is possible for a process to output a message that is not appropriate for the receivers active inside the current ambient.

$$(x:W)x[P] | \langle \operatorname{in} n \rangle$$

> type systems must statically detect such errors, keeping track of the

topic of conversation

appropriate within a given ambient

Exchange Types

Expression Types

$$W \quad ::= \quad \mathsf{B} \qquad \qquad \mathsf{type} \ \mathsf{constants} \\ | \quad \mathsf{Amb}[E] \qquad \qquad \mathsf{ambient:} \ \mathsf{allow} \ E \ \mathsf{exchanges} \\ | \quad \mathsf{Cap}[E] \qquad \qquad \mathsf{capability:} \ \mathsf{when} \ \mathsf{exercised} \ \mathsf{unleash} \ E$$

Exchange Types

$$E,F$$
 ::= Shh no exchange (W_1,\ldots,W_n) tuple $n\geq 0$

Process Types

$$T \quad ::= \quad [E] \qquad \qquad \mathsf{process} \; \mathsf{exchanging} \; E$$

Typing Processes I

put-Output

- $\Gamma, x: W \vdash P: [W]$ $\Gamma \vdash (x:W)P:[W]$
- \blacktriangleright if x:W, and P also exchanges W, then (x:W).P exchanges W.
- Only one topic of conversation.
- $\Gamma \vdash M : W$ $\Gamma \vdash \langle M \rangle : [W]$
 - \blacktriangleright M is an expression of type W: hence a process that outputs M exchanges W, i.e. has type [W].

Typing Rules

Type Judgements

Note: processes have types, describing effects (i.e. their exchanges)

Typing Processes II

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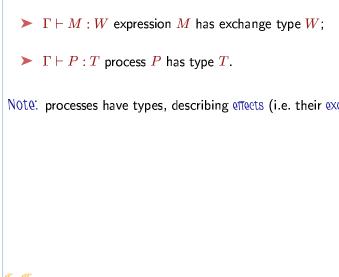
Ambients

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$$\qquad \qquad \frac{\Gamma \vdash a : \mathsf{Amb}[E] \quad \Gamma \vdash P : [E]}{\Gamma \vdash a[P] : T}$$

- ➤ an ambient exchanges nothing at its own level, hence it may be thought of as potentially exchanging any type.
- \triangleright Type safety requires consistency between the type that a declares and the type of exchanges held by P inside a.
- ➤ We can check that processes inside that ambient behave consistently.
- Further consequence: can tell what types are exchanged with ambient is opened ... useful for typing open



Typing Expressions I

 $\Gamma dash M : \mathsf{Amb}[E]$

pen

 $\Gamma \vdash \mathsf{open}\ M : \mathsf{Cap}[E]$

- if n : Amb[E], opening n unleashes processes enclosed in n, which have exchanges of type E.
- lacksquare by our intended interpretation of ${
 m Cap}[E]$, this implies open $n:{
 m Cap}[E].$
- Further consequence: process exercises open $n: {\rm Cap}[E]$ may end-up running in parallel with processes which exchange E.
- \blacktriangleright any such process must be itself prepared to exchange E that types ... useful for typing M.P

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Typing Processes III

 $\qquad \qquad \frac{\Pr(\Pr(\exists X)}{\Gamma \vdash M : \mathsf{Cap}[E] \quad \Gamma \vdash P : [E]}{\Gamma \vdash M.P : [E]}$

Explained earlier

- Remember: just one topic of conversation
- Remaining rules present no difficulties

Typing Expressions II

 $ightharpoonup \Gamma dash M: {
m Amb}[F]$

In and Out

 $\overline{\Gamma dash \mathsf{in} \ M : \mathsf{Cap}[E]}$

 $\qquad \frac{\Gamma \vdash M : \mathsf{Amb}[F]}{\Gamma \vdash \mathsf{out}\ M : \mathsf{Cap}[E]}$

- > need not track type information
- ➤ all the required consistency checks on the local exchanges within an ambient are already accounted for by the typing of open.

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Mobility Types

- Exchange types are effective in imposing a discipline on the exchanges within ambients.
- but communication is just one aspect of the computation of the ambient calculus, and not the core one.
- basic properties of mobile ambients are those related to their mobility, to the possibility of opening an ambient and exposing its contents,
- want a type system to control/characterize these aspects of ambient behavior.

Boxing Ambients

- The Open capability is
 - > essential for communication, but
 - potentially dangerous

 $\langle V \rangle^{\eta}.P$

 $(\nu G)P$

XS

```
a [ \ {
m in \ Safe\_amb.NastyCode} \ ] \ | \ {
m Safe\_amb} [ \ {
m open} \ a.Q \ ]
```

 $\longrightarrow \longrightarrow$ safe_amb[NastyCode | Q]

- complicates the typing of mobility
- Drop the open capability of Mobile Ambients
- Provide new constructs for communication across boundaries
 - \blacktriangleright exchanges towards children: $(x)^n.P$, $\langle M \rangle^n.P$
 - \blacktriangleright exchanges towards parent: $(x)^{\uparrow}.P$, $\langle M \rangle^{\uparrow}.P$

output

group creation



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Typed Boxed Ambients: Syntax

```
names
::=
                         enclosing amb
XS
 XS \star
                         local
        0
                         nil process
                                            V,U
::=
                                                    ::= n
                                                                      name
|XS P_1|P_2
                         composition
                                                    XS in V
                                                                      may enter V
 XS \quad (\nu n:A)P
                                                    \mid XS \mid out V
                                                                     may exit \,V\,
                         restriction
 XS !P
                                                    |XS| = \frac{1}{1} \frac{V}{V} = \frac{V}{V}
                         replication
       V[P]
                                                    XS V_1.V_2
                                                                      path
                         ambient
 XS
       V.P
                         prefixing
       (\boldsymbol{x}:\boldsymbol{W})^{\eta}.P
                         input
```

Boxed Ambients: overview

➤ Mobile Ambients \ open + parent-child I/O

Communication primitives

- \blacktriangleright $(\vec{x})^{\eta}P$: input from ambient η
- $ightharpoonup \langle M \rangle^{\eta} P$: output to ambiet η
- $\eta=$ the location where the communication happens
 - $\eta = \star$: local, as in Mobile Ambients
 - $\rightarrow \eta = n$: from parent to child
 - $\rightarrow \eta = \uparrow$: from child to parend

Remote communication, between siblings, still requires mobility

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(Comm Local)

(Comm Output n)

Reduction Semantics

Mobility:

$$n[\operatorname{in} m.P|Q] \mid m[R] \to m[n[P|Q]|R] \tag{In}$$

$$m[n[\operatorname{out} m.P|Q]|R] \to n[P|Q]|m[R] \tag{Out}$$

Communication:

$$(m{x})^n.P \mid n[\langle m{V}
angle.Q \mid R]
ightarrow P\{m{V} / m{x}\} \mid n[Q \mid R]$$
 (Comm Input n)

 $(x).P \mid \langle V \rangle.Q \rightarrow P\{V/x\} \mid Q$

 $\langle V \rangle^n P \mid n[(x).Q \mid R] \rightarrow P \mid n[Q\{V/x\} \mid R]$

$$(x).P \mid n[\langle V \rangle^{\uparrow}.Q \mid R] \rightarrow P\{V/x\} \mid n[Q|R]$$
 (Comm Output \uparrow)

$$\langle V \rangle . P \mid n[(x)^{\uparrow}.Q \mid R] \rightarrow P \mid n[Q\{V/x\} \mid R]$$
 (Comm Input \uparrow)

+

Discussion

- Reductions yield clear notions of resources and access requests
 - each ambient has an allocated resource, its local (anonymous) channel;
 - $ightharpoonup \langle M
 angle^{\eta} pprox$ write access to the ambient η towards which the request is directed (equivalently, its anonymous channel).
 - $ightharpoonup (x)^{\eta} \approx \text{read access}$
- > Resource access control policies expressed easily and directly
- > Static analysis, by typing, eased and more accurate, given the absence of open

till, we will criticise it tomorrow. For now let us look at access control.



Indirect Border Crossing in MA

royan Horses: The system

Odysseus[in Horse.out Horse.Destroy] | Horse[in Troy] | Troy[Trojans]

well-typed under assumptions:

Odysseus: amb[Achaean, cross(Toy)]

Horse : amb[Toy, cross(City)]

Troy: amb[City, _]

OWQVQT, the system may evolve to

Troy[Trojans | Horse[_] | Odysseus[Destroy]]

there Odysseus got inside Troy's Walls taking by surprise the *Trojans*.

Group Types for Modility

Aim: Resource Access Control

- Detect and prevent unwanted access to resources.
- ➤ We focus on Static approaches based on enforcing type disciplines.

 ${\tt Groups:} \ \, {\tt Sets \ of \ processes \ with \ common \ access \ rights.} \ \, ({\tt Cardelli-Gordon})$

Constraints like k: CanEnter(n) are modelled as:

n holongs to group O

n belongs to group ${\tt G}$

k may cross the border of any ambient of group ${\tt G}.$

For instance, the system:

$$k[\operatorname{in} n \mid l[\operatorname{out} k]] \mid n[_]$$

is Well-typed under assumptions of the form:

k: amb[K, eross(N)]

l: amb[L, cross(K)] n: amb[N, ...]

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Types

Groups: G,H,...

Sets of groups: $\mathscr{G}, \mathscr{D}, \mathscr{S}, \dots$ \mathscr{U} Th

W The universal set of groups

Ambients types:

nielim ryben

 $A\quad ::=\quad \mathrm{amb}_{\chi}[\mathbf{G},M,C]$

amb of group G, good for actions $\chi\subseteq\{i,o,c,r,w\},$ with mobility type M, and communication type C

Process types:

 $\Pi ::= \operatorname{proe}[G, M, C]$

process that can be enclosed in an ambient of group ${ t G},$ may drive to ambients whose groups are in ${ t M},$ and communicates as described by type ${ t C}$

Capability types:

 $K\quad ::= \quad \operatorname{cap}[{\tt G},M,F]$

capability that can appear in an ambient of group ${f G},$ may drive it to ambients whose groups are in ${f M},$ with exchange type ${f F}$ for local communication

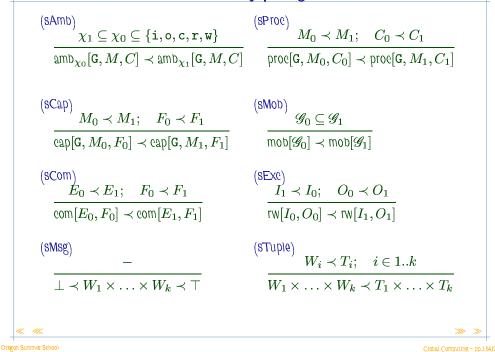
IVDS (COUT)lobility types: mobility specs $M ::= mob[\mathscr{G}]$ ommunication types: $C ::= \operatorname{com}[E, F]$ $oldsymbol{E}$ for local and $oldsymbol{F}$ for upward $oldsymbol{e}$: xchange types: E,F ::= rw[I,O]read/write values (valid if $O \prec$ lessage types: I,O ::= $\bot \mid XS \mid W_1 \times ... \times W_k \mid XS \mid T$ bottom, tuple, top alue types: W,Y ::= Aambient name XS Kcapability Global Computing - pp.153/224

Good Values

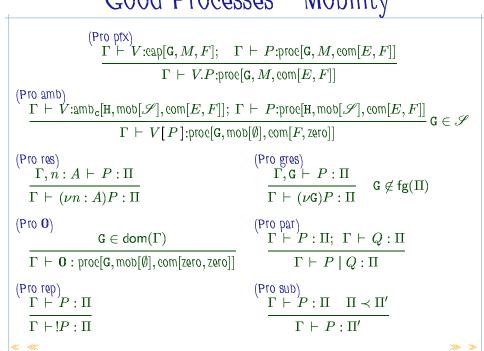
$$\frac{(\text{Val n})}{\Gamma, n: W, \Gamma' \, \vdash \, \diamond} \\ \frac{\Gamma, n: W, \Gamma' \, \vdash \, \alpha: W}{\Gamma, n: W, \Gamma' \, \vdash \, n: W}$$

$$\begin{array}{ll} \frac{(\mathsf{Val}\;\mathsf{pfx})}{\Gamma \vdash V_0:K;\;\;\Gamma \vdash V_1:K} & \frac{(\mathsf{Val}\;\mathsf{in})}{\Gamma \vdash V:\mathsf{amb}_\mathtt{i}[\mathsf{G},M,\mathsf{com}[E,F]]} \, \mathtt{H} \in \Gamma \\ \\ \frac{(\mathsf{Val}\;\mathsf{Sub})}{\Gamma \vdash V:W;\;\;W \prec W'} & \frac{\Gamma \vdash V:\mathsf{amb}_\mathtt{o}[\mathsf{G},M,\mathsf{com}[E,F]]}{\Gamma \vdash V:\mathsf{amb}_\mathtt{o}[\mathsf{G},M,\mathsf{com}[E,F]]} \, \mathtt{H} \in \Gamma \\ \\ \frac{(\mathsf{Val}\;\mathsf{Sub})}{\Gamma \vdash V:W'} & \frac{\Gamma \vdash V:\mathsf{amb}_\mathtt{o}[\mathsf{G},M,\mathsf{com}[E,F]]}{\Gamma \vdash \mathsf{out}\;V:\mathsf{cap}[\mathtt{H},M,F]} \, \mathtt{H} \in \Gamma \\ \end{array}$$

Subtyping



Good Processes - Mobility



Good Processes – Communication

```
\frac{\Pr(\mathbf{x}, \boldsymbol{x}: \boldsymbol{W} \vdash P: \mathsf{proe}[\mathbf{G}, M, \mathsf{com}[\mathsf{rw}[I, O], F]]}{\Gamma \vdash (\boldsymbol{x}: \boldsymbol{W}).P: \mathsf{proe}[\mathbf{G}, M, \mathsf{com}[\mathsf{rw}[I, O], F]]} \ I \prec \boldsymbol{W}
   \Gamma \vdash \langle \boldsymbol{V} \rangle.P : \mathsf{proe}[\mathsf{G}, M, \mathsf{com}[\mathsf{rw}[I, \boldsymbol{W}], F]]
\frac{\overset{\text{(inp }\uparrow)}{\Gamma, \boldsymbol{x}: \boldsymbol{W} \, \vdash \, P: \operatorname{proe}[\mathsf{G}, M, \operatorname{com}[E, \operatorname{rw}[I, O]]]}}{\Gamma \, \vdash \, (\boldsymbol{x}: \boldsymbol{W}_k)^{\uparrow}.P: \operatorname{proe}[\mathsf{G}, M, \operatorname{com}[E, \operatorname{rw}[I, O]]]} \, I \prec \boldsymbol{W}}
   \Gamma \vdash \langle \boldsymbol{V} \rangle^{\uparrow}.P : \mathsf{proe}[\mathsf{G}, M, \mathsf{com}[E, \mathsf{rw}[I, \boldsymbol{W}]]]
                                                     ...and so on analogously
```

Detecting Odysseus' intentions

low, in order to assign a type to

Odysseus[in Horse.out Horse.Destroy] | Horse[in Troy] | Troy[Trojans]

e need assumptions of the form:

Odysseus: ambc[Achaean, mob[{Ground, Toy, City}], _] Horse: ambioc[Toy, mob[{Ground, City}], _] Troy: ambioc[City, -, -]

representing that Odysseus is an Achaean intentioned to move into a City! In the other hand, under assumptions of the form

Odysseus: ambc[Achaean, mob[{Ground, Toy}], _]

ne Trojans should not fear any attack from Odysseus.

ut what if Odysseus is lying about his intentions (i.e. type)?

Properties

Communication properties:

▶ If $\Gamma \vdash (x : W).P \mid \langle V \rangle.Q : \Pi$ then $\Gamma \vdash V : Y$ with $Y \prec W$.

Mobility properties:

ightharpoonup If $\Gamma \vdash n[\inf m.P \mid Q] \mid m[R] : \Pi$, then

$$\Gamma \vdash m : \mathsf{amb}_{\chi_0}[\mathtt{M},_,_] \quad \mathrm{and} \quad \Gamma \vdash n : \mathsf{amb}_{\chi_1}[_,\mathsf{mob}[\mathscr{S}],_]$$

with $M \in \mathcal{S}$, i, $c \in \chi_0$ and $c \in \chi_1$.

ightharpoonup If $\Gamma \vdash m[n[$ out $m.P \mid Q] \mid R] : \Pi$, then

with $o, c \in \chi_0$, $c \in \chi_1$, $M \in \mathcal{S}_n$ and $\mathcal{S}_m \subseteq \mathcal{S}_n$.

Subject reduction:

ightharpoonup If $\Gamma \vdash P : \Pi$ and $P \equiv Q$ or $P \rightarrow Q$, then there exist groups $G_0, \dots G_k$ such that $G_0, \ldots, G_k, \Gamma \vdash Q : \Pi$.

 $\Gamma \vdash m : \operatorname{amb}_{\gamma_0}[M, \operatorname{mob}[\mathscr{S}_m], _] \text{ and } \Gamma \vdash n : \operatorname{amb}_{\gamma_1}[N, \operatorname{mob}[\mathscr{S}_n], _]$

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Adding co-capabilities

Reduction Semantics:

 $n[\operatorname{in} m.P \mid Q] \mid m[\operatorname{\overline{in}} \alpha.R \mid S] \ \to m[n[P \mid Q] \mid R \mid S] \quad \text{ for } \alpha \in \{\star, n\}$

 $m[n[\text{out } m.P \mid Q] \mid R] \mid \overline{\text{out }} \alpha.S \rightarrow n[P \mid Q] \mid m[R] \mid S$ for $\alpha \in \{\star, n\}$

 $M ::= mob[\mathscr{S},\mathscr{C}]$

Subtyping Relation: (extended)

 $\frac{(\mathrm{SMOD})}{\mathscr{G}_0\subseteq\mathscr{G}_1,\quad\mathscr{C}_0\subseteq\mathscr{C}_1}{\mathrm{mob}[\mathscr{G}_0,\mathscr{C}_0]\prec\mathrm{mob}[\mathscr{G}_1,\mathscr{C}_1]}$

Good Values in BSA

```
(Val in)
                                                                                         (Val out)
                                                                                              \Gamma \vdash V: \mathsf{amb}_{\mathsf{o}}[\mathsf{G}, \mathsf{mob}[\mathscr{S}, \mathscr{C}], \mathsf{com}[E, F]]
      \Gamma \vdash V: \operatorname{amb_i}[G, M, \operatorname{com}[E, F]]
   \Gamma \vdash \text{in } V:\text{eap}[\mathtt{H}, \text{mob}[\{G\}, \emptyset], E]
                                                                                                     \Gamma \vdash \mathsf{out} \ V : \mathsf{eap}[\mathtt{H}, \mathsf{mob}[\mathscr{S}, \emptyset], F]
(Val coin)
     \Gamma \vdash V: amb_i[G, M, com[E, F]]
                                                                                                  \Gamma \vdash V: amb_{\mathbf{G}}[\mathbf{G}, M, com[E, F]]
   \Gamma \vdash \overline{\operatorname{in}} V : \operatorname{cap}[H, \operatorname{mob}[\emptyset, \{G\}], F]
                                                                                             \Gamma \vdash \overline{\mathsf{out}} \, V : \mathsf{eap}[\mathtt{H}, \mathsf{mob}[\emptyset, \{\mathtt{G}\}], F]
(Val coin *)
                                                                                          (Val coout ⋆)
                                                                                                                        \mathtt{G}\in\mathsf{dom}(\Gamma)
                            G \in dom(\Gamma)
   \Gamma \vdash \overline{\mathsf{in}} \star :\mathsf{eap}[\mathsf{G},\mathsf{mob}[\emptyset,\mathscr{U}],\mathsf{zero}]
                                                                                             \Gamma \vdash \overline{\mathtt{out}} \star : eap[\mathtt{G}, mob[\emptyset, \mathscr{U}], zero]
                               In (Val in), (Val out), (Val coin), (Val coin), assume H \in \Gamma
```

Control Properties in BSA

ecess Control Theorem:

Whenever

$$\Gamma \vdash m[\overline{\operatorname{in}} \alpha.P \mid Q] : \Pi \quad \text{or} \quad \Gamma \vdash m[\overline{\operatorname{out}} \alpha.P \mid Q] : \Pi,$$

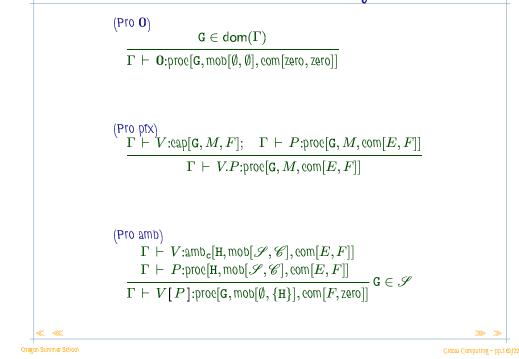
with $\alpha \in \{\star, n\}$, then

$$ightharpoonup \Gamma \vdash m : \operatorname{amb}_{\chi_0}[-, \operatorname{mob}[-, \mathscr{C}], _], \text{ and}$$

$$\blacktriangleright$$
 either $\alpha = \star$ and $\mathscr{C} = \mathscr{U}$,

$$ightharpoonup$$
 or $lpha=n$ with $\Gamma\vdash n$: $\mathrm{amb}_{\chi_1}[\mathtt{N},\mathtt{-},\mathtt{-}]$ and $\mathtt{N}\in\mathscr{C}.$

Good Processes - Modility in BSA



Using co-capabilities to defend Troy

```
Our running example in BSA:
```

```
The Trojan War \triangleq Odysseus[inHorse.outHorse.Destroy]
```

| Horse[in *.inTroy]

| Troy[in Horse. Trojans | out Odysseus. Sinon]

which can be Well-typed only if

 $\Gamma \vdash \mathsf{Troy} : \mathsf{amb}_{\mathsf{ioc}}[\mathsf{City}, \mathsf{Mob}[_, \{\mathsf{Toy}, \mathsf{Achaean}\}], _]$

That is if Troy (in suicidal mood) allowed Achaeans in.

Using co-capabilities to detend I roy (ctd)

onsider now the system:

```
The Trojan Trap \triangleq Odysseus [in Horse.out Horse.Destroy]
                         Horse [in \star .in Troy]
                         Troy [in Horse. Trojans]
```

his situation would be perfectly safe for Troy (but dangerous for Odysseus!) rovided we can type it under the assumptions of the form

```
Odysseus: ambc[Achaean, _, _]
    Horse: amb_{ioc}[Toy, -, com[E, 0]]
    Troy: amb_{ioc}[City, mob[\emptyset, \mathscr{C}], \_]
```

with Achaean $otin \mathscr{C}$.

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Global Computing

— Lecture V —

Towards Ambient Resource Control

Summary of Lecture IV

We focused on ambient mobility, introducing ambients and their exchange types, boxed ambients and their mobility types.

Further Reading

Mobile Ambients, a "hot topic": lots of papers. References for this lecture are:

- Mobile ambients (Cardelli, Gordon)
- Mobility types (Cardelli, Ghelli, Gordon)
- Polymorphic Typing (Amtoft, Kfoury, Pericas)
- Safe Ambients (Levi, Sangiorgi)
- Boxed Ambients (Bugliesi, Crafa, Castagna)
- Typing and Subtyping Mobility (Merro, Sassone)
- ... a long list, ...

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The Case for Resource Usage Control

Global Computing involve scenarios where mobile devices enter and exit domains and networks.

Typical Devices:

Today: Smart Cards, Embedded devs (e.g. in cars), Mobile phones, PDAs, Sat navigators, ...

Tomorrow: PAN, VAN, D-ME, P-COM, ...

Requirements:

- Security: Authentication, Privacy, Non Repudiation
- Trust Formation and Management
- Context (e.g. Location) Awareness
- Dynamic Learning and Adaptability
- Policies of Access Control and their Enforcement
- Negotiation of Access, Access Rights, Resource Acquisition
- Protection of Resource Bounds ...

Central Notion:

Resource Usage







Roadmap for Lecture V

- Control of Interference in Mobile Ambients: manageable vs expressive: how do you want your calculus?
- Secrecy in Untrusted Networks: crypto-primitives for mobile agents
- Ambients with Bounded Capacity: make realistic hypothesis on ambient capacities and processes' space consumption.

Mobile Boxed Ambients

open's nature of ambient dissolver is a potential source of problems.

Direct communication as alternative source of expressiveness: Mobile Boxed mbients. Perform I/O on a subambient n's local channel (viz. $(x)^n$) as well as om the parent's local channel (viz. $(x)^{\uparrow}$)

$$(x)^n \cdot P \mid n[\langle M \rangle \cdot Q \mid R] \longrightarrow P\{M/x\} \mid n[Q \mid R]$$

 $\langle M \rangle \cdot P \mid n[(x)^{\uparrow} \cdot Q \mid R] \longrightarrow P \mid n[Q\{M/x\} \mid R].$

But it is a great source of non-local nondeterminism and communication terference.

$$m[\ (x)^n.P \mid n[\ \langle M \rangle \mid (x).Q \mid k[\ (x)^{\uparrow}.R\]\]\]$$

Interferences in Mobile Ambients

The inherent nondeterminism of movement may go wild: Grave Interferences.

 $k[n[in m.P \mid out k.R] \mid m[Q]]$

$$k[n]$$
 in $m.P$ [out $k.R$] [$m[Q]$

➤ Introducing Safe Ambients

$$n[\text{ in } m.P \mid Q] \mid m[\overline{\text{ in }} m.R \mid S] \longrightarrow m[n[P \mid Q] \mid R \mid S]$$

➤ Co-capabilities and single-threadedness rule out grave interferences

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Introducing NBA: Communication

NBA: a fresh foundation based on: each ambient comes equipped with two mutually non-interfering channels, for local and upward communications.

$$(x)^{n}.P \mid n[\langle M \rangle^{\hat{}}.Q \mid R] \longrightarrow P\{M/x\} \mid n[Q \mid R]$$
$$\langle M \rangle^{n}_{\mid}.P \mid n[(x)^{\hat{}}.Q \mid R] \longrightarrow P \mid n[Q\{M/x\} \mid R]$$

> Expressiveness??

 \blacktriangleright Hmm, rather poor: n[P] cannot, for instance, communicate with children it doesn't know statically. It can never learn about incoming ambients, and will never be able to talk to them.

introducing NBA: Mobility

Let us introduce co-actions of the form $\overline{\text{enter}}(x)$ which have the effect of inding the variable x.

Such a purely binding mechanism does not provide a way control of access, ut only to registers it. As a (realistic) access protocol where newly arrived gents must register themselves to be granted access to local resources.

Need a finer mechanism of access control:

$$a[\, \operatorname{enter} \langle b, \overset{\downarrow}{k} \rangle . P \mid R \,] \mid b[\, \overline{\operatorname{enter}}(x, \overset{\downarrow}{k}) . Q \mid S \,] \longrightarrow b[\, a[\, P \mid R \,] \mid Q\{a/x\} \mid S \,]$$

This represent an access protocol where the credentials of incoming processes (k) the rule above) are controlled, as a preliminary step to the registration protocol.

NBA: Reduction Semantics

mobility

$$n[\operatorname{enter}\langle m,k\rangle.P\mid R]\mid m[\overline{\operatorname{enter}}(x,k).Q\mid S] \quad \longrightarrow \quad m[\,n[\,P\mid R]\mid Q\{n/x\}\mid S]$$

$$n[\,m[\,\operatorname{exit}\langle n,k\rangle.P\mid R]\mid S]\mid \overline{\operatorname{exit}}(x,k).Q \quad \longrightarrow \quad m[\,P\mid R]\mid n[\,S]\mid Q\{m/x\}$$

communication

$$\begin{array}{ccc} (\vec{x}).P \mid \langle \vec{M} \rangle.Q & \longrightarrow & P\{\vec{M}/\vec{x}\} \mid Q \\ \\ (\vec{x})^n.P \mid n[\langle \vec{M} \rangle \hat{} .Q \mid R] & \longrightarrow & P\{\vec{M}/\vec{x}\} \mid n[Q \mid R] \\ \\ \langle \vec{M} \rangle^n.P \mid n[\langle \vec{x} \rangle \hat{} .Q \mid R] & \longrightarrow & P \mid n[Q\{\vec{M}/\vec{x}\} \mid R] \end{array}$$

structural congruence

$$P \equiv Q, \ Q \quad \longrightarrow \quad R, \ R \equiv S \Longrightarrow P \longrightarrow S$$

NRA: Syntax

name

may ent

may exit

message

input

output

allow eu

allow ex

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path

Names : $a, b, \ldots n, x, y, \ldots \in \mathbb{N}$ Locations: Messages: M,N::= anested names ::=XSenclosing amb XS enter $\langle M, N \rangle$ $XS \star$ $XS = \text{exit}\langle M, N \rangle$ local XS M.NPrefixes: Processes: := 0Mnil process ::= $|XS|(x_1,\ldots,x_k)^{\eta}$ $|XS P_1|P_2$ composition $|XS | \langle M_1, \ldots, M_k \rangle^{\eta}$ $|XS|(\nu n)P$ restriction $XS = \overline{\text{enter}}(x, M)$ XS $!\pi.P$ replication XS M[P] $XS = \overline{\text{exit}}(x, M)$ ambient $XS \pi.P$ prefixing

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A one-to-one communication server

ightharpoonup Let ${\sf w}(k)$ be a bidirectional forwarder for any pair of incoming ambients.

$$\mathsf{w}(k) \triangleq \mathsf{w}[\ \overline{\mathsf{enter}}(x,k).\overline{\mathsf{enter}}(y,k).(!(z)^x.\langle z\rangle^y|!(z)^y.\langle z\rangle^x) \]$$

An agent can be defined as: $A(a,k,P,Q) \triangleq a[\operatorname{enter}\langle \mathbf{w},k\rangle.P \mid \operatorname{exit}\langle \mathbf{w},k\rangle.Q]$ and a communication server as:

o2o(k) =
$$(\nu r) (r[\langle \rangle^{\hat{}}]!!()^r.(w(k)|\overline{\text{exit}}(\underline{},k).\overline{\text{exit}}(\underline{},k).r[\langle \rangle^{\hat{}}]))$$

 \blacktriangleright It can be proved that once two agents engage in communication no other agent knowing the key k can interfere with their completing the exchange. In formulas:

$$\begin{split} (\nu k) (\ \mathsf{o2o}(k) \ | \ A(k, a_1, \langle M \rangle^{\hat{\cdot}}.P_1, Q_1) \ | \ A(k, a_2, (x)^{\hat{\cdot}}.P_2\{x\}, Q_2) \ | \ \Pi_{i \in I} A(K, a_i, R_i, S_i) \) \\ \Longrightarrow & \cong^c \ (\nu k) (\ \mathsf{o2o}(k) \ | \ a_1[P_1 \ | \ Q_1] \ | \ a_2[P_1\{M/x\} \ | \ Q_2] \ | \ \Pi_{i \in I} A(K, a_i, R_i, S_i) \) \end{split}$$

A print server

The following process assigns a progressive number to incoming jobs.

$$\mathsf{enqueue}_k \triangleq \ (\boldsymbol{\nu}c) \ (\ c[\langle 1 \rangle ^{\hat{}}\] \ |\ !(n)^c.\overline{\mathsf{enter}}(x,k).\langle n \rangle^x.c[\langle n+1 \rangle ^{\hat{}}\])$$

- We can turn it into a print server (which consumes such numbers).

print
$$\triangleq (\nu c) \left(c[\langle 1 \rangle^{\hat{}}] \right] | !(n)^c.\overline{\text{exit}}(x,n).(dat)^x.(P\{dat\} | c[\langle n+1 \rangle^{\hat{}}])$$

 $prtsrv(k) \triangleq k[enqueue_k|print]$

 $\mathsf{iob}(M,k) \triangleq (\boldsymbol{\nu}p)p[\mathsf{enter}\langle k,k\rangle.(n)^{\hat{}}.(\boldsymbol{\nu}q)q[\mathsf{exit}\langle p,n\rangle.\langle M\rangle^{\hat{}}]]$

enters the server
$$prtsrv(k)$$
 (using enqueue), it is assigned a number that it uses

s a password to carry job M to print (which eventually will bind it to dat in P.

Dynamic name discovery and passwords are fundamental here.)

Some Equational Laws

arbage Collection laws

 $l[(\vec{x}_i)^n . P | (\vec{x}) . Q | \langle \vec{M} \rangle^m . R] \cong^c \mathbf{0}$

$$[(\vec{x}_i)^n.P \mid (\vec{x}).Q \mid \langle M \rangle^m.R] \cong^c \mathbf{0}$$

$$l[(\vec{x})^n . P \mid \langle \vec{M} \rangle . P \mid \langle \vec{M} \rangle^m . P] \cong^c \mathbf{0}$$

ommunication laws

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$$-l[\langle ilde{M_0}
angle^{\hat{}} | \langle ilde{M_1}
angle^{\hat{}}] \, \cong^c \, l[\langle ilde{M_0}
angle^{\hat{}}] | \, l[\langle ilde{M_1}
angle^{\hat{}}]$$

$$l[\langle \vec{x} \rangle.P \mid \langle \vec{M} \rangle.Q] \cong^{c} l[P\{\vec{M}/\vec{x}\} \mid Q]$$

$$(\nu l)((\vec{x})^l \cdot P \mid l[\langle \vec{M} \rangle \hat{} \cdot Q]) \cong^c (\nu l)(P\{\vec{M}/\vec{x}\} \mid l[Q])$$

$$m[(\vec{x})^l . P \mid l[\langle \vec{M} \rangle \hat{} . Q]] \cong^c m[P\{\vec{M}/\vec{x}\} \mid l[Q]]$$

lobility laws

$$\begin{array}{l} (\boldsymbol{\nu}p)(m[\operatorname{enter}\langle n,p\rangle.P] \mid n[\overline{\operatorname{enter}}(x,p).Q]) \; \cong^c \; (\boldsymbol{\nu}p)(n[Q\{m/x\} \mid m[P]]) \\ \\ \vdash l[m[\operatorname{enter}\langle n,p\rangle.P] \mid n[\overline{\operatorname{enter}}(x,p).Q]] \; \cong^c \; l[n[Q\{m/x\} \mid m[P]]] \end{array}$$

Goodies of NBA over BA

- ➤ A good set of equational laws
- A simpler type system
- ➤ A sound LTS characterisation of barbed congruence.
- No significant loss of expressive power

A Type System for NBA

> Types

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Message Types

W

Exchange Types E, F ::= Shh

:= N[E]

C[E]capability

no exchange

ambient/password

 $W_1 \times \ldots \times W_k$ tuples $(k \ge 0)$ Process Types := [E, F]

local/upward exchange TN[E] types both ambients and passwords; Shh is the Silent type; N[Shh] is an

ambient with no upward exchanges or a password that reveal the visitor's name.

> Type Environments

(Env Empty) $\Gamma \vdash \diamond \quad a \notin \mathsf{Dom}(\Gamma)$ $\Gamma, a: W \vdash \diamond$ Ø F O

```
Typing Rules
                                                                                                  \Gamma \vdash M_1 : \mathsf{C}[E_1] \quad \Gamma \vdash M_2 : \mathsf{C}[E_2]
     \Gamma, a: W, \Gamma' \vdash \diamond
\Gamma, a: W, \Gamma' \vdash a: W
                                                                                                          \Gamma \vdash M_1.M_2 : \mathsf{C}[E_1 \sqcup E_2]
\Gamma \vdash M : N[E] \quad \Gamma \vdash N : N[F] \quad (F \leqslant G)
                                                                                                  \Gamma \vdash M : \mathsf{N}[E] \quad \Gamma \vdash N : \mathsf{N}[F] \quad (F \leqslant G)
                 \Gamma \vdash \mathsf{enter}\langle M, N \rangle : \mathsf{C}[G]
                                                                                                                    \Gamma \vdash \mathsf{exit}\langle M, N \rangle : \mathsf{C}[G]
                                                                                          \Gamma \vdash P : [E, F]
                                                                                                                                             \Gamma \vdash \diamond
              \Gamma \vdash P : [E, F] \quad \Gamma \vdash Q : [E, F]
                                                                                         \Gamma \vdash !P : [E, F]
                                                                                                                                     \Gamma \vdash \mathbf{0} : [E, F]
                           \Gamma \vdash P \mid Q : [E, F]
                                                                 \Gamma, n: \mathbb{N}[G] \vdash P: [E, F]
                                                                \Gamma \vdash (\boldsymbol{\nu} n: \mathbb{N}[G])P: [E, F]
```

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Typing Rules: II

```
Processes: I/O
\Gamma, \vec{x} : \vec{W} \vdash P : [\vec{W}, E]
                                                                                            \Gamma, \vec{x} : \vec{W} \vdash P : [E, \vec{W}]
\Gamma \vdash (\vec{x} : \vec{W}) . P : [\vec{W}, E]
                                                                                          \Gamma \vdash (\vec{x}:\vec{W})^{\hat{}}.P:[E,\vec{W}]
```

Messages

Processes

(Par)

Projection)

$$\frac{\overset{\cdot}{\Gamma} \vdash \overset{\cdot}{M} : \mathsf{N}[\vec{W}] \quad \Gamma, \vec{x} : \vec{W} \vdash P : [G, H]}{\Gamma \vdash (\vec{x} : \vec{W})^M . P : [G, H]} \qquad \frac{\overset{\cdot}{\Gamma} \vdash \overset{\cdot}{M} : \vec{W} \quad \Gamma \vdash P : [\vec{W}, E]}{\Gamma \vdash \langle \vec{M} \rangle . P : [\vec{W}, E]}$$

$$\frac{\overset{\cdot}{\Gamma} \vdash \vec{M} : \vec{W} \quad \Gamma \vdash P : [E, \vec{W}]}{\Gamma \vdash (\vec{M})^{\hat{\Gamma}} . P : [E, \vec{W}]} \qquad \frac{\overset{\cdot}{\Gamma} \vdash N : \mathsf{N}[\vec{W}] \quad \Gamma \vdash \vec{M} : \vec{W} \quad \Gamma \vdash P : [G, H]}{\Gamma \vdash \langle \vec{M} \rangle^N . P : [G, H]}$$

Subject Reduction. If $\Gamma \vdash P : T$ and $P \longrightarrow Q$, then $\Gamma \vdash Q : T$.

Typing Rules: II

```
> Processes: mobility
        (Amb)
                                                                                                 (Prefix)
            \Gamma \vdash M : \mathsf{N}[E] \quad \Gamma \vdash P : [F, E]
                                                                                                     \Gamma \vdash M : \mathsf{C}[F] \quad \Gamma \vdash P : [E,G] \quad (F \leqslant G)
                     \Gamma \vdash M[P] : [G, H]
                                                                                                                           \Gamma \vdash M.P : [E,G]
        (Co-enter)
                                                                                                 (Co-exit)
            \Gamma \vdash M : \mathsf{N}[\tilde{W}] \quad \Gamma, x : \mathsf{N}[\tilde{W}] \vdash P : [E, F]
                                                                                                     \Gamma \vdash M : \mathsf{N}[	ilde{W}] \quad \Gamma, x : \mathsf{N}[	ilde{W}] \vdash P : [E, F]
                                                                                                                   \Gamma \vdash \overline{\mathsf{exit}}(x, M).P : [E, F]
                         \Gamma \vdash \overline{\mathsf{enter}}(x, M).P : [E, F]
        (Co-enter-silent)
                                                                                                 (Co-exit-silent)
            \Gamma \vdash M : N[Shh] \quad \Gamma \vdash P : [E, F] \quad x \not\in fv(P)
                                                                                                     \Gamma \vdash M : \mathsf{N[Shh]} \quad \Gamma \vdash P : [E, F] \quad x \not\in \mathsf{fv}(P)
                           \Gamma \vdash \overline{\mathsf{enter}}(x, M).P : [E, F]
                                                                                                                     \Gamma \vdash \overline{\mathsf{exit}}(x, M).P : [E, F]
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                                                                                                                                                                Global Computing - pp.182/2
```

Encoding: BA in NBA

We can encode BA into NBA enriched with a focused form of nondeterminism.

```
\{P\}_n
                                                 = \overline{\text{Cross}} | \langle P \rangle_n
              \langle m[P] \rangle_n = m[\{P\}_m]
              \langle (x)^a P \rangle_n = (x)^a \langle P \rangle_n
              \langle (x)P \rangle_n = (x) \langle P \rangle_n + (x)^{\hat{}} \langle P \rangle_n + \overline{\text{exit}}(y, pw)(x)^y \langle P \rangle_n
              \langle (x)^{\uparrow}P \rangle_n = (\nu p)p[\operatorname{exit}\langle n, \operatorname{pr}\rangle.(x)^{\hat{}}.\operatorname{enter}\langle n, p \rangle.\langle x \rangle^{\hat{}}] | \overline{\operatorname{enter}}(y, p)(x)^y \langle P \rangle_n
              \langle \langle M \rangle^a P \rangle_n = \langle M \rangle^a \langle P \rangle_n
                                                = \langle M \rangle \langle P \rangle_n + \langle M \rangle^{\hat{n}} \langle P \rangle_n + \overline{\text{exit}}(y, \text{pr}) \langle M \rangle^y \langle P \rangle_n
              \langle\!\langle M \rangle P \rangle\!\rangle_n
              \langle \langle M \rangle^{\uparrow} P \rangle_n = (\nu p) p [\operatorname{exit}\langle n, \operatorname{pw}\rangle \cdot \langle M \rangle^{\hat{n}} \cdot \operatorname{enter}\langle n, p \rangle \cdot \langle \cdot \rangle^{\hat{n}}] | \overline{\operatorname{enter}}(y, p) (_)^y \langle P \rangle_n
where \overline{\text{cross}} = |\overline{\text{enter}}(x, mv)| |\overline{\text{exit}}(x, mv), in n = \text{enter}\langle n, mv \rangle, and out n = \text{exit}\langle n, mv \rangle
and p, y \notin \operatorname{fn}(P).
\triangleright Thm. The encoding is operationally sound. If P and Q are Single-threaded,
```

then it is equationally sound, that is $\{P\}_n \cong^c \{Q\}_n \text{ implies } P \cong^c Q$.

Secreey in the pi calculus

- exchange messages over private channels
 - $(\boldsymbol{\nu}n)(\ \overline{n}\langle m\rangle\ |\ n(x).P\)$
- No third process can
 - \blacktriangleright discover m by interacting with the process
 - ightharpoonup cause a different message to be sent on n
- ➤ Or is it?

Secrecy in the Mobile Ambients

ames \approx Cryptokeys: Carrying messages inside private ambients preserves nessage integrity and privacy. Or, does it?

$$(\nu n)(a[n[\text{out }a.\text{in }b.\langle M\rangle]]|b[\text{open }n.(x)P])$$

t actually offers poor guarantees, as \emph{n} must be revealed along the move.

- ow to provide stronger protection?
- ➤ Commit to agents their own security, with <code>00-0apabilities</code>

$$(\nu n)(a[n[\text{out }a.\text{in }b.\overline{\text{open }}n.\langle M\rangle]]|b[\overline{\text{in }}b.\text{open }n.(x)P])$$

- No one can open n and read M before n reaches b.
- ➤ Protect ambients by @ncapsulating them

$$(\nu n)(a[p[\mathsf{out}\ a.\mathsf{in}\ b\mid n[\langle M\rangle]]]\mid b[\mathsf{open}\ p.\mathsf{open}\ n.(x)P])$$

A public ambient p carries a private ambient n, which need not reveal its name to move.

Secrecy in the spi calculus

Not the spi calculus way, as we saw. In a distributed system

 $(\nu n)(\underbrace{\overline{n}\langle m\rangle}_{\text{at site A}}|\underbrace{n(x).P}_{\text{at site B}})$ $\blacktriangleright \text{ Link between } A \text{ and } B \text{ may be physically insecure, regardless of the privacy of } n$ $\blacktriangleright \text{ use private keys to encrypt connections over public channels}$ $(\nu n)(\overline{p}\langle\{m\}_n\rangle \mid p(y).\text{case } y \text{ of } \{x\}_n \text{ in } P)$ $\blacktriangleright \text{ anybody can read on } p$

only the intended recipients know n and will read m

Secrecy: Need new primitives?

Case 1: Physical devices:

> the first proposal is all we need: physical devices can easily perform access control, such as that encompassed by co-capabilities

Case II: Soft agents

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the first proposal is pointless in "untrusted" networks. Similarly, the second proposal presupposes encryption for data and code and applies only partially to active agents, which may not move autonomously when encrypted.

A ${\it crypt0-primitive:}$ subjective access control using co-capabilities + data encryption to preserve secrecy of data while agents move autonomously

$$n[\operatorname{seal} k.P \mid Q] \quad \longrightarrow \quad n\{\!\!\mid P \mid Q \,\}\!\!\mid_k \qquad \qquad \text{crypto-key}$$

Effects:

- ➤ blocks message exchanges and encrypts their contents;
- > the Sealed ambient cannot communicate, but it may move.

Sealed Ambients

The mechanism to resume to a fully operational state is associated to novements and co-capabilities containing keys

$$n\{\mid \text{in } m.P \mid Q \}_k \mid m\{\mid \overline{\text{in}} \{x\}_k.R \mid R'\} \longrightarrow m\{n[P \mid Q] \mid R\{n/x\} \mid R'\}$$

xample:

$$(\nu k)a[n[\text{seal }k.\text{out }a.\text{in }b.\langle M\rangle^{\hat{a}}]]|b[\overline{\text{in}}\{x\}_k.(y)^x.P]$$

$$\longrightarrow (\nu k) a[n \{ \text{out } a.\text{in } b.\langle M \rangle^{\hat{a}} \}_k] | b[\overline{\text{in}} \{x\}_k.(y)^x.P]$$

$$\longrightarrow (\nu k)a[\quad] \mid n\{\mid \text{in } b.\langle M\rangle^{\hat{}}\}\}_k \mid b[\overline{\text{in}} \{x\}_k.(y)^x.P]$$

$$\longrightarrow (\nu k)a[\] |b[n[\langle M\rangle^{\hat{}}]|(y)^n.P\{n/x\}]$$

Silent Reduction

ilent Evaluation Context: $SE ::= [-] \mid (\boldsymbol{\nu} n) SE \mid SE \mid P \mid n \mid SE \mid \mid n \mid \mid SE \mid \mid_{L}$ lobility I

$$n\{ \text{ in } m.P \mid Q \} \mid m\{ \overline{\text{in}} .R \mid S \} \xrightarrow{\text{shh}} m\{ n\{P \mid Q \} \mid R \mid S \} \quad \text{(enter)}$$

$$m\{ \text{ in } m.P \mid Q \} \mid m\{ \text{ in } .R \mid S \} \longrightarrow m\{ n\{P \mid Q \} \mid R \mid S \}$$
 (exit)
$$m\{ n\{ \text{ out } m.P \mid Q \} \mid R \} \mid \overline{\text{out }} .S \xrightarrow{\text{shh}} n\{P \mid Q \} \mid m\{R\} \mid S$$
 (exit)

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$$n\{\inf m.P \mid Q[\}_k \mid m\{\overline{\inf}\{x\}_k.R \mid S\} \xrightarrow{\sinh} m\{n[P \mid Q] \mid R\{n/x\} \mid S\}$$
 (K-enter)

$$m\{P \mid n\{\} \text{ out } m.Q \mid R\}\}_k\} \mid \overline{\text{out}} \{x\}_k.S \xrightarrow{\text{shh}} m\{P\} \mid n[Q \mid R] \mid S\{n/x\}$$
 (K-exit)
$$n[\text{seal } k.P \mid Q] \xrightarrow{\text{shh}} n\{\}P \mid Q\}\}_k$$
 (Seal)

Structural Rules

$$P \equiv Q, \ Q \xrightarrow{\mathsf{shh}} R, \ R \equiv S \Longrightarrow P \xrightarrow{\mathsf{shh}} S$$
 (struct)
$$P \xrightarrow{\mathsf{shh}} Q \Longrightarrow SE[P] \xrightarrow{\mathsf{shh}} SE[Q]$$
 (context)

CBA: Syntax

			<i>U</i>					
Expressions				Locat	ions			
M,N ::=	k,\dots,q n	ames		η	::=	a	child	
	x,\ldots,z V	ariable	2 S			\uparrow	parent	
İ	in M $^{ m e}$	in M enter M			ĺ	*	local	
į	out M	xit M	r		•			
İ	in \(let enter						
İ	out \	et exit						
į	M.M p	ath						
Prefixes		Processes						
π ::=	M		path	P	::=	0		
	(x_1,\ldots,x_k)	$)^{\eta}$	input		ĺ	↑ parent * local	P	
$egin{array}{cccc} & \langle M_1, \ldots, N_m \rangle & & \overline{in} & \{x\}_M, \end{array}$	$\langle M_1,\ldots,M_n\rangle$	$I_k angle^\eta$	output		ĺ	(u	n)P	
		let in & unseal			P	P		
ĺ	$\overline{out}\ \{x\}_M$		let out & unseal			$!\pi$	P	
	seal M		sealing			M	[P]	
			-		ĺ	M	$\{P\}_{M}$	

Reduction

Communication

 $\langle \vec{M} \rangle^n P \mid n[(\vec{x})^{\uparrow} Q \mid R] \longrightarrow P \mid n[Q\{\vec{M}/\vec{x}\} \mid R]$

Evaluation Context $E ::= [-] | (\nu n) E | P | E | E | P | n [E]$

$$\begin{array}{cccc} \text{(local)} & (\vec{x})P \mid \langle \vec{M} \rangle Q & \longrightarrow & P\{\vec{M}/\vec{x}\} \mid Q \\ \text{(input } n) & (\vec{x})^n P \mid n[\langle \vec{M} \rangle^\uparrow Q \mid R] & \longrightarrow & P\{\vec{M}/\vec{x}\} \mid n[Q \mid R] \end{array}$$

Structural Rules

(output n)

$$(\text{Silent}) \qquad \qquad P \xrightarrow{\text{shh}} Q \quad \Rightarrow \quad P \longrightarrow Q$$

$$(\text{struct}) \qquad P \equiv Q, Q \ \longrightarrow \ R, \ R \equiv S \quad \Rightarrow \quad P \ \longrightarrow \ S$$

$$(\text{context}) \hspace{1cm} P \hspace{1cm} \longrightarrow \hspace{1cm} Q \hspace{1cm} \Rightarrow \hspace{1cm} E[P] \hspace{1cm} \longrightarrow \hspace{1cm} E[Q]$$

Remarks

- No explicit data encryption (delegate it to implementation).
- ➤ At most one level of sealing.
- > Silent reductions do not apply under prefix.
- > Reductions do not apply under prefix and sealed ambients.
- No computation, except mobility, for sealed ambients

mm er Sehool

Encoding of spi

The encoding (monadic case)

$$\langle a \rangle_p \triangleq a, \langle \{M\}_k \rangle_p \triangleq p$$

$$\llbracket a \rrbracket_p \triangleq \mathbf{0}$$

$$\llbracket \{M\}_k \rrbracket_p \triangleq (\nu q)(\llbracket M \rrbracket_q \mid p \llbracket (x) \hat{\ }.\mathsf{seal} \ k.\mathsf{in} \ x. \langle \left\langle\!\left\langle M \right\rangle\!\right\rangle_q \rangle \hat{\ }])$$

$$\llbracket \mathbf{0} \rrbracket \triangleq \mathbf{0}, \ \llbracket (\boldsymbol{\nu}n)P \rrbracket \triangleq (\boldsymbol{\nu}n)\llbracket P \rrbracket, \ \llbracket P \mid Q \rrbracket \triangleq \llbracket P \rrbracket \mid \llbracket Q \rrbracket$$

$$[\![\overline{b}\langle M\rangle]\!] \triangleq (\nu q)([\![M]\!]_q \mid b[\langle \langle\!\langle M \rangle\!\rangle_q \rangle^{\hat{n}}])$$

$$\llbracket b(x)P \rrbracket \triangleq (x)^b \llbracket P \rrbracket$$

[Case
$$M$$
 of $\{x\}_k$ in P] \triangleq let $z = \langle\!\langle M \rangle\!\rangle_p$ in
$$(\nu p) ([\![M]\!]_n \mid (\nu c) (\langle c \rangle^z \mid c[\overline{\operatorname{in}} \mid \{y\}_k.(x)^y \langle x \rangle^{\hat{\gamma}}] \mid (x)^c P))$$

➤ Thm. The encoding is equationally sound.

Encoding of spi

> Idea: represent an encrypted message with a sealed ambient which contains the message.

Communicating the encrypted messages is communicating the name of the corresponding ambient.

▶ Use three translation maps, with $\llbracket \cdot \rrbracket$ leading (and p a name):

$$\langle\!\!\langle \,\cdot \,\rangle\!\!\rangle_p$$
: Expressions \longmapsto Expressions

$$\llbracket \cdot \rrbracket_p : \mathsf{Expressions} \longmapsto \mathsf{Processes}$$

$$\llbracket \cdot \rrbracket$$
: Processes \longmapsto Processes

 \backslash $M \rangle_p$ returns p, the name of the ambient that stores M. Correspondingly, $[\![M]\!]_p$ stores M into an ambient named p.

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Secrecy, by typing

Typing System: Secrecy is captured by a type system \vdash which may classify processes as <code>Untrusted</code> and data as <code>public</code> if it can be exchanged with untrusted process.

➤ Types split the world in two: TRUSTED vs UNTRUSTED.

	TRUSTED	UNTRUSTED	
Message types W	N[E], Key $[E]$	Public	
Exchange types E	(W_1,\ldots,W_k) , Shh		
Process Types T	[E,F]	Un	

- The type system
 - ➤ allows interactions between the two components
 - > preserves the desired secrecy invariants on the trusted components.

Types for Secreey

lessage Types

- **Public:** messages that may be exchanged with untrusted processes. Includes movement (co-)capabilities
- \triangleright N[E]: ambients with upward E exchanges (as usual)
- \triangleright Key[E]: keys that may apply to ambients of type N[E]

rocess Types

- Un: unknown processes
- [E,F]: processes with local E exchanges + upward F exchanges

(Co-In Key)

(Amb Seal)

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Sample typing rules

 $\Gamma \vdash M : \mathsf{Kev}[E]$ $\Gamma, x: \mathsf{N}[E] \vdash P : [G, H]$

 $\Gamma \vdash \overline{\mathsf{in}} \{x\}_M.P : [G, H]$

 $\Gamma \vdash N : \mathsf{Key}[E]$ $\Gamma \vdash M : \mathsf{N}[E]$ $\Gamma \vdash P : [F, E]$ $\overline{\Gamma \vdash M\{\!\!\mid\! P\,\!\!\mid\!\}_N:T}$

(Input M Amb) $\Gamma \vdash M : \mathsf{N}[W_1, \ldots, W_n]$ $\Gamma, x_1: W_1, \ldots, x_n: W_n \vdash P: [E, F]$ $\Gamma \vdash (x_1, \ldots, x_n)^M P : [E, F]$

(Untrusted Co-In) $\Gamma \vdash M : Public$ Γ, x :Public $\vdash P$: Un $\overline{\Gamma} \vdash \overline{\mathsf{in}} \ \{x\}_M.P : \mathsf{Un}$

> (Untrusted Amb Seal) $\Gamma \vdash N : \mathsf{Public}$

(Untrusted Input M)

 $\Gamma \vdash M$: Public $\Gamma \vdash P : \mathsf{Un}$

 $\Gamma \vdash M \{\mid P \mid\}_N : T$

 $\Gamma \vdash M : \mathsf{Public}$ $\Gamma, x_i : \mathsf{Public} \vdash P : \mathsf{Un}$ $\Gamma \vdash (x_1,\ldots,x_k)^M P : \mathsf{Un}$

Trusted and Untrusted

The rules of the game. How do TRUSTED and UNTRUSTED interact?

- mobility for free: (un)trusted ambients may traverse (un)trusted sites;
- NO local exchanges between trusted and untrusted processes;
- YES hierarchical exchanges of public values allowed between trusted and untrusted processes.

Typing Rules: A Manichean view of the world.

- > Each process form has two typing rules, depending on whether is trusted or untrusted .
- Trusted systems exchanging public values with the untrusted components become themselves untrusted

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Properties of the Type System

Subject Reduction If $\Gamma \vdash P : T$ and $P \longrightarrow Q$, then $\Gamma \vdash Q : T$.

Typability

Let $\{a_1,...,a_n\} = \text{fn}(P)$ and $\{x_1,...,x_m\} = \text{fv}(P)$ then

 $a_1: \mathsf{Public}, \ldots, a_n: \mathsf{Public}, x_1: \mathsf{Public}, \ldots, x_m: \mathsf{Public} \vdash P: \mathsf{Un}$

> and Secrecy...

Secreey and Adversaries

ituitively:

A process preserves the secrecy of a piece of data M if it does not publish M, or anything that would permit the computation of M.

-Adversary: A context A(-) which initially knows all names in S.

evealing Names: P may reveal n to S if there exists an S-adversary A(-), a context C(-), and a name $c \in S$ not bound by C(-) such that:

$$\mathbf{A}(P) \Longrightarrow \mathbf{C}(c[\langle n \rangle^{\hat{}} | Q]).$$

his captures two kinds of attacks

- \triangleright an hostile context enclosing a trusted process, as in $a[Q \mid (-)]$,
- ▶ a malicious agent mounting an attack to a remote host, as in $a[in \ p.in \ q.Q \ | \ Q'] \ | \ (-).$

In example: $P = c[\langle a \rangle^{\hat{}}] \mid a[\langle k \rangle^{\hat{}}]$ may reveal k to $\{c\}$. In fact, for $\mathbf{A}(-)$ the c-adversary $(x)^c.(y)^x.c[\langle y \rangle^{\hat{}}] \mid (-)$, we have $\mathbf{A}(P) \Longrightarrow c[\langle k \rangle^{\hat{}}] \mid c[] \mid a[]$.

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Questions

- Sealing/unsealing is a rather flexible mechanism.
- ➤ How and how efficiently can the underlying mechanism of selective encryption be implemented ?
- Sealing provides for secrecy of messages. It would be nice to have more, eg hiding part of the agent structure.
- ➤ Can guarantees of data integrity be established along similar lines.

Secreey and Adversaries

Intuitively:

A process preserves the secrecy of a piece of data M if it does not publish M, or anything that would permit the computation of M.

S-Adversary: A context A(-) which initially knows all names in S.

Revealing Names: P may reveal n to S if there exists an S-adversary A(-), a context C(-), and a name $c \in S$ not bound by C(-) such that:

$$\mathbf{A}(P) \Longrightarrow \mathbf{C}(c[\langle n \rangle^{\hat{n}} | Q]).$$

This captures two kinds of attacks

- \triangleright an hostile context enclosing a trusted process, as in $a[Q \mid (-)]$,
- ▶ a malicious agent mounting an attack to a remote host, as in $a[in \ p.in \ q.Q \ | \ Q'] \ | \ (-).$

Secrecy Theorem: Well-typed processes do not reveal their secrets publicly. Formally, if $\Gamma \vdash P$: Un and $\Gamma \vdash s : W \neq \mathsf{Public}$, then P preserves the secrecy of s from all public channels, i.e. from $\{a \mid \Gamma \vdash a : \mathsf{Public}\}$.

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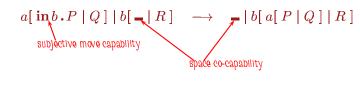
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Dimensions, Capacities, Mobility

Focus: Capacity Bounds Awareness.

BoCa: Bounded Capacities

- Subjective Mobility
- Bounded Capacity Ambients
- Space as a linear co-capability.
- > Fine control of capacity.



Minimal Desiderata

➤ Realistic about space occupation. Bigger processes take more space.

$$n[\;{
m in}\,m$$
 . big and fat P $]\mid m[\;{
m lue{-}}\;]\mid n[\;{
m in}\,m$. small and slim P $]$

> Replication must be handled appropriately

$$a[\ !P\] = a[\ !P\ |\ P\] = a[\ !P\ |\ P\ |\ P\] = a[\ !P\ |\ P\ |\ P\ |\ P\] = \dots$$

Allow an analisys of variation in space occupation

More precisely, control process spawning.

Computation takes space, dynamically, and we'd like to model it.

Term Well-formedness

undamentals: Space Conscious Movement

But the SIZE of travellers matters!

$$a^{k \text{ times}} \qquad \qquad b \text{ times} \qquad \qquad k \text{ times} \qquad \qquad k \text{ times} \qquad \qquad a^{k \text{ times}}$$

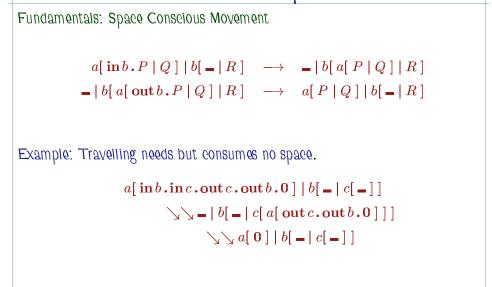
/hat is the a^k ? A well-formedness annotation measuring the size of P.

counts spaces: Weight(ullet) = 1, Weight($a^k[P]$) = k if Weight(P) = k, $oldsymbol{\perp}$ otherwise.

eduction only for Well-formed terms: (1) weights appear as conditions on eductions; (2) the calculus' operators make only sense with type annotations.

Otation. We use $_^k$ as a shorthand for $_ | \dots | _$

A Calculus of Bounded Capacities: Movement



A Calculus of Bounded Capacities: Open

 $\operatorname{opn} a \cdot P \mid a^k [\overline{\operatorname{opn}} \cdot Q \mid R] \longrightarrow P \mid Q \mid R$

Example: Recovering Mobile Ambients.

Fundamentals: Space Conscious Opening

$$\llbracket a \llbracket P \rrbracket \rrbracket \triangleq a^0 \llbracket \cdot \overline{\mathbf{opn}} \mid \llbracket P \rrbracket \end{bmatrix}$$
$$\llbracket (\nu a) P \rrbracket \triangleq (\nu a^0) \llbracket P \rrbracket$$
$$\dots$$

Calculus of Bounded Capacities: Spawning

undamentals: Space Conscious Process Activation

passive process:
$$P = k$$
weighs 0

P weighs k

xample: Replication: $!^k \triangleq ! \triangleright^k$

$$! \triangleright^k P \mid \underline{\quad}^k \quad \longrightarrow \quad ! \triangleright^k P \mid P$$

ypes ensure only 0-Weighted processes are replicable: One must use spawning, that replication needs space proportional to the process' weight.

xample: Recursion (well, almost):

$$\operatorname{rec}(X^k)P \triangleq (\nu X^k)(\operatorname{!opn} X . \triangleright^k \widehat{P} \mid X[_^k]), \quad \text{ where } \widehat{P} \triangleq P\{X[_^k]/X\}$$

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Calculus of Bounded Capacities: Transfer

undamentals: Space Acquisition and Release

$$a \hat{\;\;} .P \mid \textbf{_} \mid a^k [\stackrel{*}{\cdot} .Q \mid R \,] \quad \longrightarrow \quad P \mid a^{k+1} [\mid Q \mid \textbf{_} \mid R \,]$$

 $a^{k+1}[\ll P \mid - \mid S \mid \mid b^h[a \gg Q \mid R \mid \longrightarrow a^k[P \mid S \mid \mid b^{k+1}[Q \mid - \mid R \mid]]$

ransfer from Child:

get_from_child
$$a \cdot P \triangleq (\nu n)(\text{opn } n \cdot P \mid n[a \cdot \cdot \overline{\text{opn}}])$$

xample: A Memory Module

$$\begin{split} \text{memMod} &\triangleq \text{mem}[\ _^{256MB} \mid ! \ll \mid ! \text{free} \rangle \] \\ \text{malloc} &\triangleq \text{m}[\text{!mem} \rangle \text{.free}[\text{out m.m} \rangle . \ll] \mid ! \ll] \end{split}$$

memMod | malloc \longrightarrow ^{256MB} mem[!«|!free»] | m[\blacksquare ^{256MB} | ...] \longrightarrow ^{2×256MB} mem[!«|!free»] | malloc | free ^{256MB}[\blacksquare | «] \longrightarrow ^{256MB} memMod | malloc | ...

Boca: Exambies (Oben)

 $\operatorname{spw}^k b[\ P\] \triangleq \exp^0[\ \mathbf{out}\ a \cdot \overline{\mathbf{opn}} \cdot \triangleright^k b[\ P\]\]$ Then,

 $a[\operatorname{spw}^k b[\ P\]\ |\ Q\]\ |\ _^k\ |\ \operatorname{\mathbf{opn}} \exp \quad \longrightarrow \quad a[\ Q\]\ |\ b[\ P\].$

The father must provide enough space for the activation, of course.

Example: Ambient Renaming

Example: Ambient Spawning

a_be_b
k
. $P \triangleq \operatorname{spw}_a^k b[-^k \mid \operatorname{opn} a] \mid \operatorname{in} b.\overline{\operatorname{opn}}.P.$

Ambient a needs to <code>DOTTOW</code> space to rename itself.

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On the nature of space

An economic vehicle for multiple concepts

- \blacktriangleright Available space: a[| P]
- ightharpoonup Occupied space: M. \blacksquare . (Notation: M. \blacktriangle .)
- \blacktriangleright Lost space: $(\nu a)a^k[-k]$. (Notation: 0^k .)

$$\operatorname{destroy}^k \triangleq (\nu a)(\underbrace{a^{\hat{}} \cdot \dots \cdot a^{\hat{}}}_{k \text{ times}}.\mathbf{0} \mid a^0[\underbrace{\ \overset{\circ}{\underbrace{}} \cdot \dots \cdot \overset{\circ}{\underbrace{}}}_{k \text{ times}}.\mathbf{0}\])$$

 $\operatorname{destrov}^k \mid \underline{\hspace{1em}}^k \longrightarrow^k \mathbf{0}^k$

« ««

.....

```
P ::= - |\mathbf{0}| M \cdot P |P| P |M| P ||P| ||\mathbf{b}^{\mathbf{k}} P |(\nu n : \pi) P |(x : \chi) P |\langle M \rangle P
C ::= \mathbf{in} \, M \mid \mathbf{out} \, M \mid \mathbf{opn} \, M \mid M^{\hat{\mathbf{n}}} \mid \ll
\overline{C} ::= \overline{\operatorname{opn}} \mid {}^{*} \mid M \rangle
M ::= \varepsilon \mid x \mid C \mid \overline{C} \mid M \cdot M
tructural Congruence:
                             (|,0) is a commutative monoid.
                (\boldsymbol{\nu}a)(P \mid Q) \equiv (\boldsymbol{\nu}a)P \mid Q
                                                                                                              if a \notin \mathsf{fn}(Q)
                            (\boldsymbol{\nu}a)\mathbf{0} \equiv \mathbf{0}
                  (\nu a)\langle M\rangle P \equiv \langle M\rangle (\nu a)P
                                                                                                              if a \notin fn(P)
                  (\boldsymbol{\nu}a)(\boldsymbol{\nu}b)P \equiv (\boldsymbol{\nu}b)(\boldsymbol{\nu}a)P
                   a[(\boldsymbol{\nu}b)P] \equiv (\boldsymbol{\nu}b)a[P]
                                                                                                                      if a \neq b
                                  !P \equiv !P \mid P
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                                                                                                                                   Global Computing - pp.212/224
                      A System of Capacity Types
```

Calculus of Bounded Capabilities: Syntax

apacity Types: ϕ,\ldots are pairs of nats [n,N], with $n\leq N$.

ffect Types \mathcal{E},\ldots are pairs of nats (d,i), representing dees and ines.

 $\text{Xchange Types: } \chi ::= \text{Shh} \mid \text{Amb}\langle \sigma, \chi \rangle \mid \text{Cap}\langle \mathcal{E}, \chi \rangle$

rocess and Ambient and Capability Types:

 $C: \operatorname{Cap}\langle \mathcal{E}, \chi \rangle$

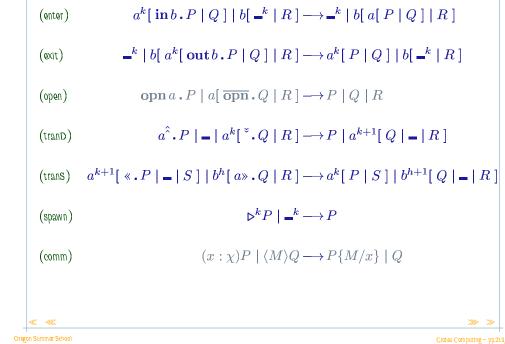
$$a: \mathsf{Amb}\langle \phi, \chi \rangle$$
 a has no less than ϕ_{m} and no more than ϕ_{M} spaces $P: \mathsf{Proe}\langle k, \mathcal{E}, \chi \rangle$ P weighs k and produces the effect \mathcal{E} on ambients

C transforms processes adding ${\mathcal E}$ to their effects

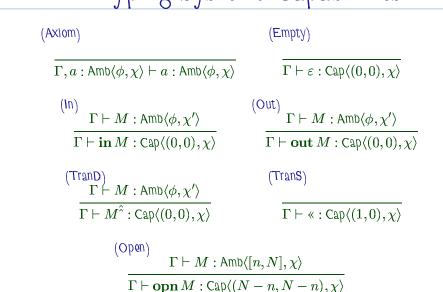
ffects and capacities componentwise and are ordered as follows:

$$\sigma \lessdot \phi \equiv \phi_{\mathsf{m}} \le \sigma_{\mathsf{m}} \text{ and } \sigma_{\mathsf{M}} \le \phi_{\mathsf{M}},$$

BoCa: Reduction Semantics



A Typing System: Capabilities



(coTranD) $\Gamma \vdash' M : \mathsf{Amb}\langle \phi, \chi' \rangle$ $\Gamma \vdash \stackrel{\circ}{}: \operatorname{Cap}\langle (0,1), \chi \rangle$ $\Gamma \vdash M \gg : \operatorname{Cap}\langle (0,1), \chi \rangle$ (coOpen) (Composition) $\Gamma \vdash M : \mathsf{Cap}\langle \mathcal{E}, \chi \rangle \quad \Gamma \vdash M' : \mathsf{Cap}\langle \mathcal{E}', \chi \rangle$ $\Gamma \vdash M.M' : \operatorname{Cap}\langle \mathcal{E} + \mathcal{E}', \chi \rangle$ $\Gamma \vdash \overline{\mathbf{opn}} : \mathsf{Cap}\langle (0,0), \chi \rangle$ (Slot) (Zero) $\Gamma \vdash \mathbf{0} : \text{Proc}\langle 0, (0,0), \chi \rangle$ $\Gamma \vdash \blacksquare : \text{Proe}\langle 1, (0,0), \chi \rangle$ $\Pr_{\Gamma,\,x:\,\chi \vdash P: \operatorname{Proc}\langle k,\mathcal{E},\chi\rangle}$ $\begin{array}{c} \text{(Output)} \\ \Gamma \vdash M : \chi \quad \Gamma \vdash P : \operatorname{Proc}\langle k, \mathcal{E}, \chi \rangle \end{array}$ $\Gamma \vdash (x : \chi)P : \text{Proc}\langle k, \mathcal{E}, \chi \rangle$ $\Gamma \vdash \langle M \rangle P : \text{Proc}\langle k, \mathcal{E}, \chi \rangle$ A Calculus of Bounded Capabilities

yping System: CoCapabilities and Processe

hm: Subject Reduction

$$\Gamma \vdash P : \operatorname{Proc}\langle k, \mathcal{E}, \chi \rangle \text{ and } P \longrightarrow Q \text{ then } \Gamma \vdash Q : \operatorname{Proc}\langle k, \mathcal{E}', \chi \rangle \text{ for some } \mathcal{E}' \lessdot \mathcal{E}.$$

he missing bit:

Grave interferences in the use of spaces

$$a[\operatorname{in} b] | b[\triangleright P | \frac{1}{\uparrow} | a[c[\operatorname{out} a]]]$$

$$\begin{split} \operatorname{rec}(X^k)P &\triangleq (\nu X^k)(\operatorname{!opn} X . \triangleright^k \widehat{P} \mid X[\ _^k \]) \\ &\longrightarrow (\nu X^k)(\operatorname{!opn} X . \triangleright^k \widehat{P} \mid \operatorname{opn} X . \triangleright^k \widehat{P} \mid X[\ _^k \]) \\ &\longrightarrow (\nu X^k)(\operatorname{!opn} X . \triangleright^k \widehat{P} \mid \triangleright^k \widehat{P}) \mid _^k \quad \operatorname{Oocops} \end{split}$$

A Typing System: Processes

```
\Gamma \vdash M : \operatorname{Cap}\langle \mathcal{E}, \chi \rangle \quad \Gamma \vdash P : \operatorname{Proe}\langle k, \mathcal{E}', \chi \rangle
                                                                                                                           \Gamma \vdash P : \text{Proc}(0,(0,0),\chi)
                   \Gamma \vdash M \cdot P : \text{Proc}\langle k, \mathcal{E} + \mathcal{E}', \chi \rangle
                                                                                                                          \Gamma \vdash !P : \text{Proc}(0,(0,0),\chi)
                                                                                                                       \Gamma \vdash P : \operatorname{Proc}\langle k, \mathcal{E}, \chi 
angle
            \Gamma, a : Amb(\phi, \chi) \vdash P : Proc(k, \mathcal{E}, \chi')
                                                                                                                             \Gamma \vdash \triangleright^k P : \text{Proc}(0, \mathcal{E}, \chi)
         \Gamma \vdash (\nu a : Amb\langle \phi, \chi \rangle) P : Proc\langle k, \mathcal{E}, \chi' \rangle
                                          \Gamma \vdash P : \text{Proc}\langle k, \mathcal{E}, \chi \rangle \quad \Gamma \vdash Q : \text{Proc}\langle k', \mathcal{E}', \chi \rangle
                                                     \Gamma \vdash P \mid Q : \text{Proc}(k + k', \mathcal{E} + \mathcal{E}', \gamma)
(Ambient)
     \Gamma \vdash M : \mathsf{Amb}\langle [n,N],\chi \rangle \quad \Gamma \vdash P : \mathsf{Proc}\langle k,(d,i),\chi \rangle \quad n \leq k-d \quad k+i \leq N
                                                         \Gamma \vdash M^k[P] : \text{Proc}\langle k, (0,0), \chi' \rangle
```

Control Space Usage: Named Slots

 $\{x/y\}_k \cdot P \triangleq y \triangleright^k(\underline{\hspace{1em}}_x^k \mid P)$

$$P ::= \underline{\hspace{1cm}}_a \mid a \triangleright^k P \mid \cdots \qquad (\text{spawn}) \quad a \triangleright^k P \mid \underline{\hspace{1cm}}_a^k \quad \longrightarrow \quad P$$

Then, $\blacksquare_{y}^{k} \mid \{x/y\}_{k} \cdot P \longrightarrow \blacksquare_{x}^{k} \mid P$

 $\operatorname{rec}(X^k)P \triangleq (\nu X)(!X\triangleright^k \widehat{P} \mid \mathbb{I}_Y^k), \quad \text{where } \widehat{P} \triangleq P\{\mathbb{I}_Y^k/X\}$

$$=_{a} \triangleq a[\ \ \ | \ =]$$

$$a \triangleright^{k} P \triangleq (\nu n)(n[\ a^{k} \rangle \cdot \triangleright^{k} \overline{\text{opn}} \cdot P \] \ | \ \text{opn} \ n)$$

Discussion

his is just a start.

et to be done:

- In the large: Develop a theory a resources, including quantitative bounds negotiation and enforcement in GC, which goes beyond space.

 Develop languages and logics to express policies and properties. . . .
- In the small: Expressiveness of BoCa; Equational theory; Smarter types; . . .
- In general: A lot to be done...

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Drawing conclusions

- Global Computing is about computation over a global, highly distributed, swiftly changing network of bounded resources.
- Central problems are (third-party) resource usage, usage analysis, and protection.
- These lectures have focused on foundational calculi (arising also from work on concurrency), useful to represent and understand issues in GC, and on types systems which guarantee properties of relevance.
- What we discussed:
 - Name Mobility
 - ➤ Types for Safety & Control
 - > Asynchrony & Distribution
 - ➤ Ambient Mobility
 - > Resource Control
- GC is a moving target, and very much alive and kicking. There are many open issues and challenging problems, spanning (almost) all grades from theoretical to practical.

Certainly a good topic for a PhD...



Summary of Lecture V

We illustrated some initial ideas about resource control in ambient-like environment. In particular, access control based on passwords and dynamic learning about the environment; data secrecy data for migrating agents; control of space usage for mobile mobile ambients.

Further Reading: This lecture was based on

- ➤ Safe Ambients (Levi, Sangiorgi).
- Boxed Ambients (Bugliesi, Castagna, Crafa)
- NBA (Bugliesi, Crafa, Sassone)
- Secrecy in Untrusted Networks (Bugliesi, Crafa, Sassone)
- Calculus of Bounded Capacities (Barbanera, Bugliesi, Dezani, Sassone)

Related work include

- > Finite Control Ambients (Gordon et al)
- ➤ Resource Control in the Ambient Calculus (Teller et al)
- Resource Usage Analysis (Igarashi, Kobayashi)
- ➤ Typed Assembly Languages (Morrisett) ... and many more...



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