# The Real/Ideal Paradigm Lecture 3

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**Boston University** 

- Our second example of the Real/Ideal Paradigm is concerned with the security of a three party private count retrieval protocol
- We'll start this third lecture by reviewing where we got to on this example in Lecture 2

# **Example 2: Private Count Retrieval (Review)**



- The Private Count Retrieval (PCR) Protocol involves three parties:
  - a Server, which holds a database
  - a Client, which makes queries about the database
  - an untrusted Third Party (TP), which mediates between the Server and Client
- A database is one-dimensional: it consists of a list of elements
- Each query is also an element, and is a request for the count of the number of times it occurs in the database

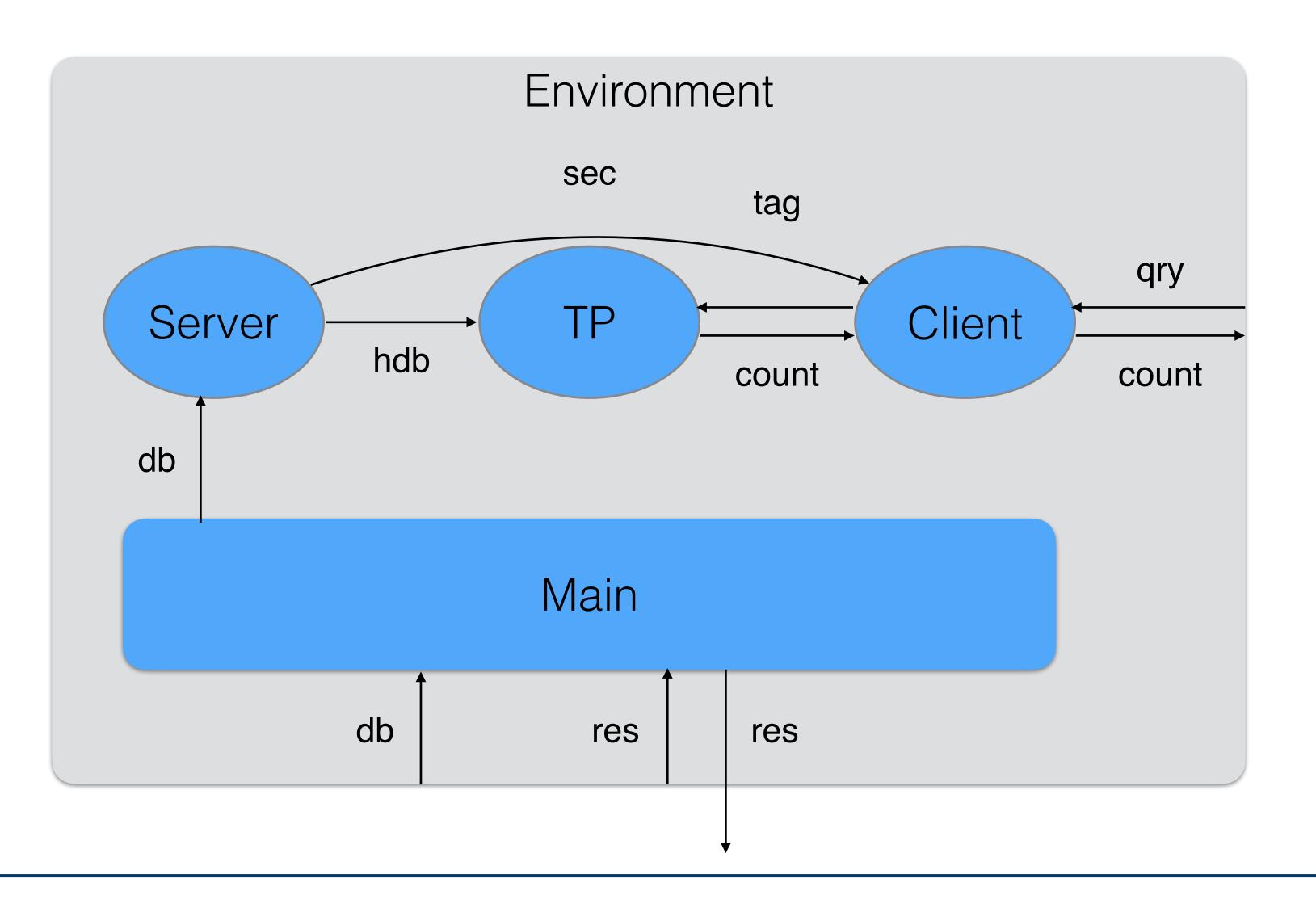
### **Private Count Retrieval Protocol**



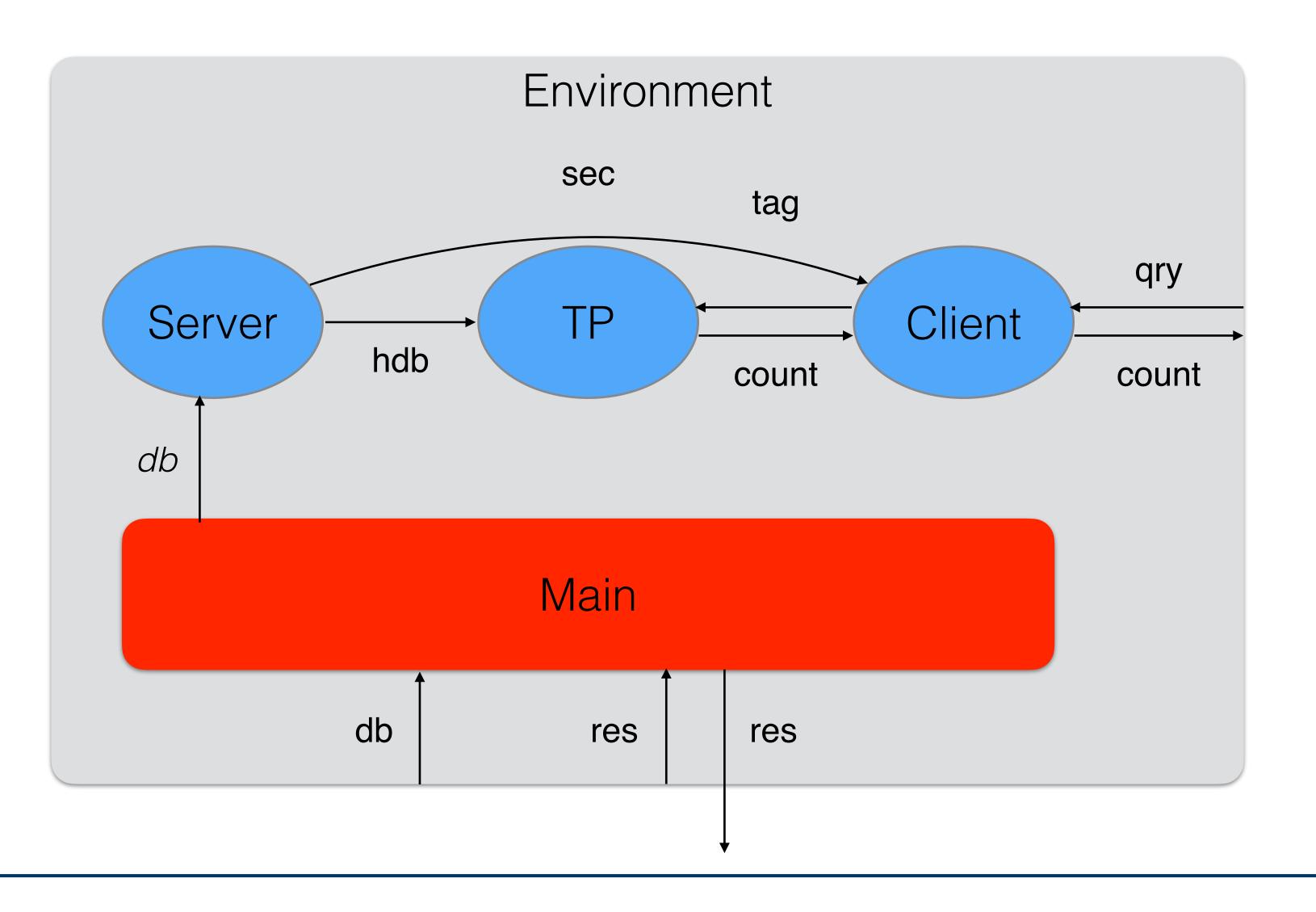


- Informally, the goal is for:
  - Client to only learn the counts for its queries, not anything else about the database (we'll limit how many queries it can make)
  - Server to learn nothing about the queries made by the Client other than the number of queries that were made
  - TP to learn nothing about the database and queries other than certain element *patterns*

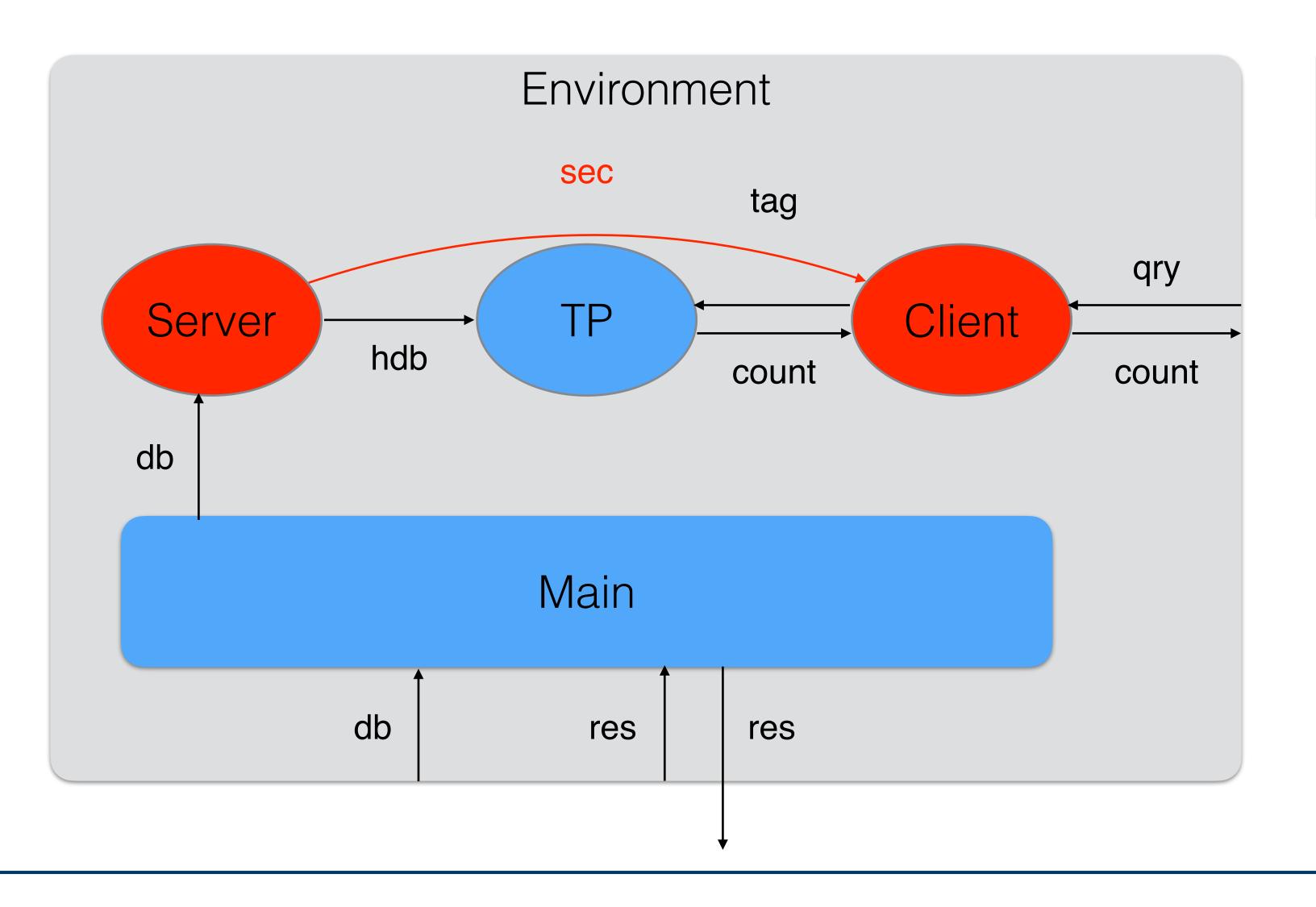








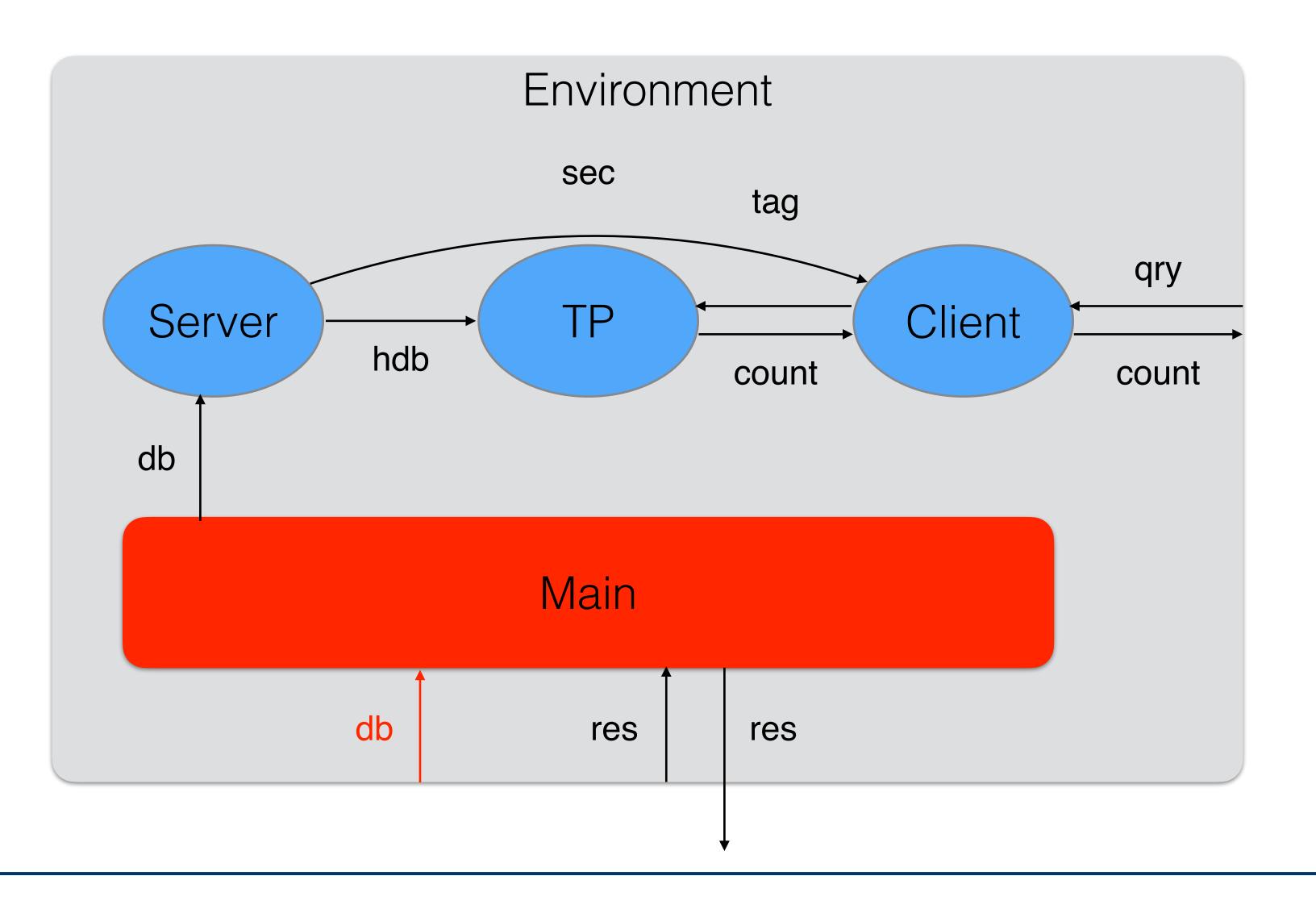




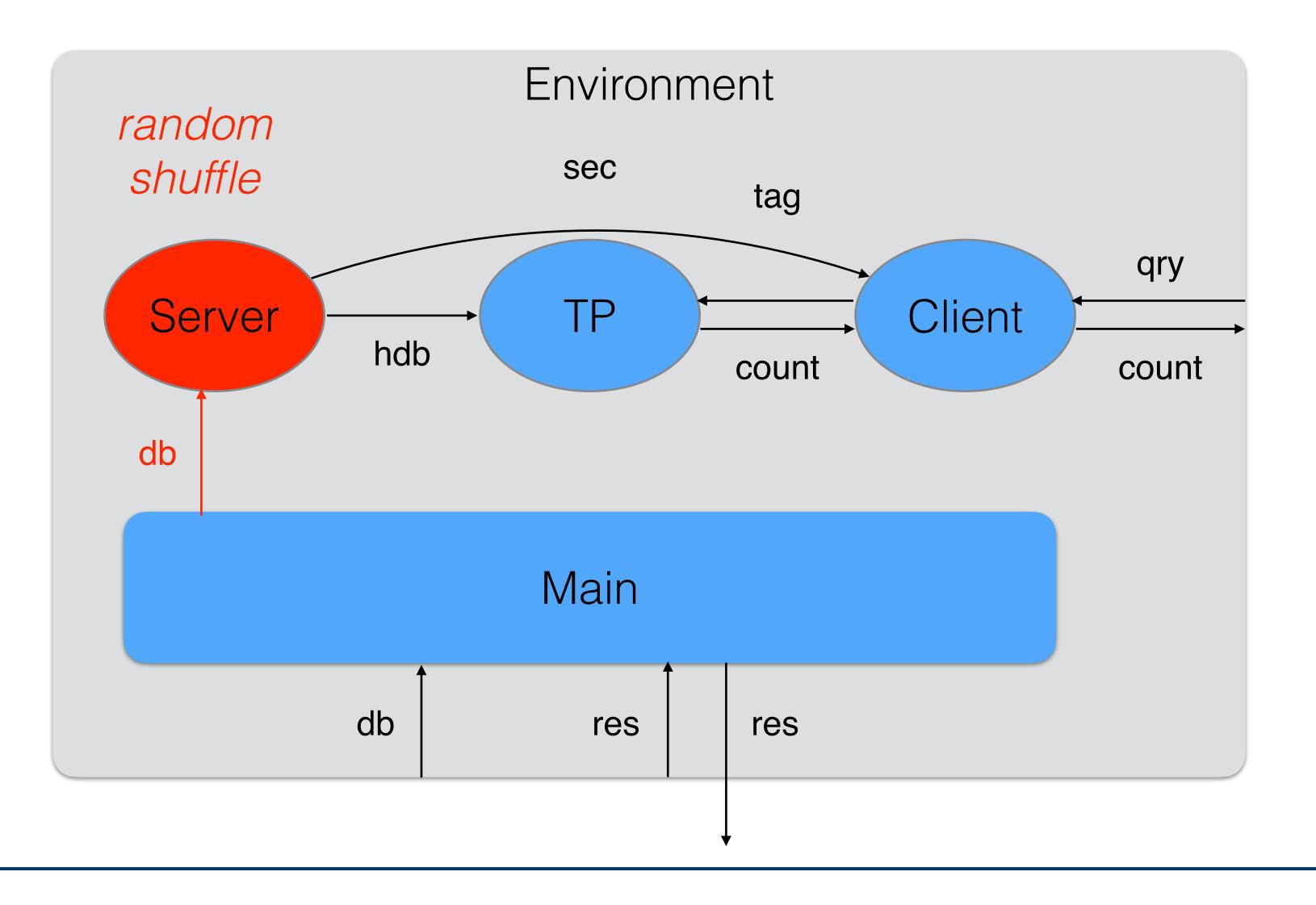
secrets are bit strings of length sec\_len



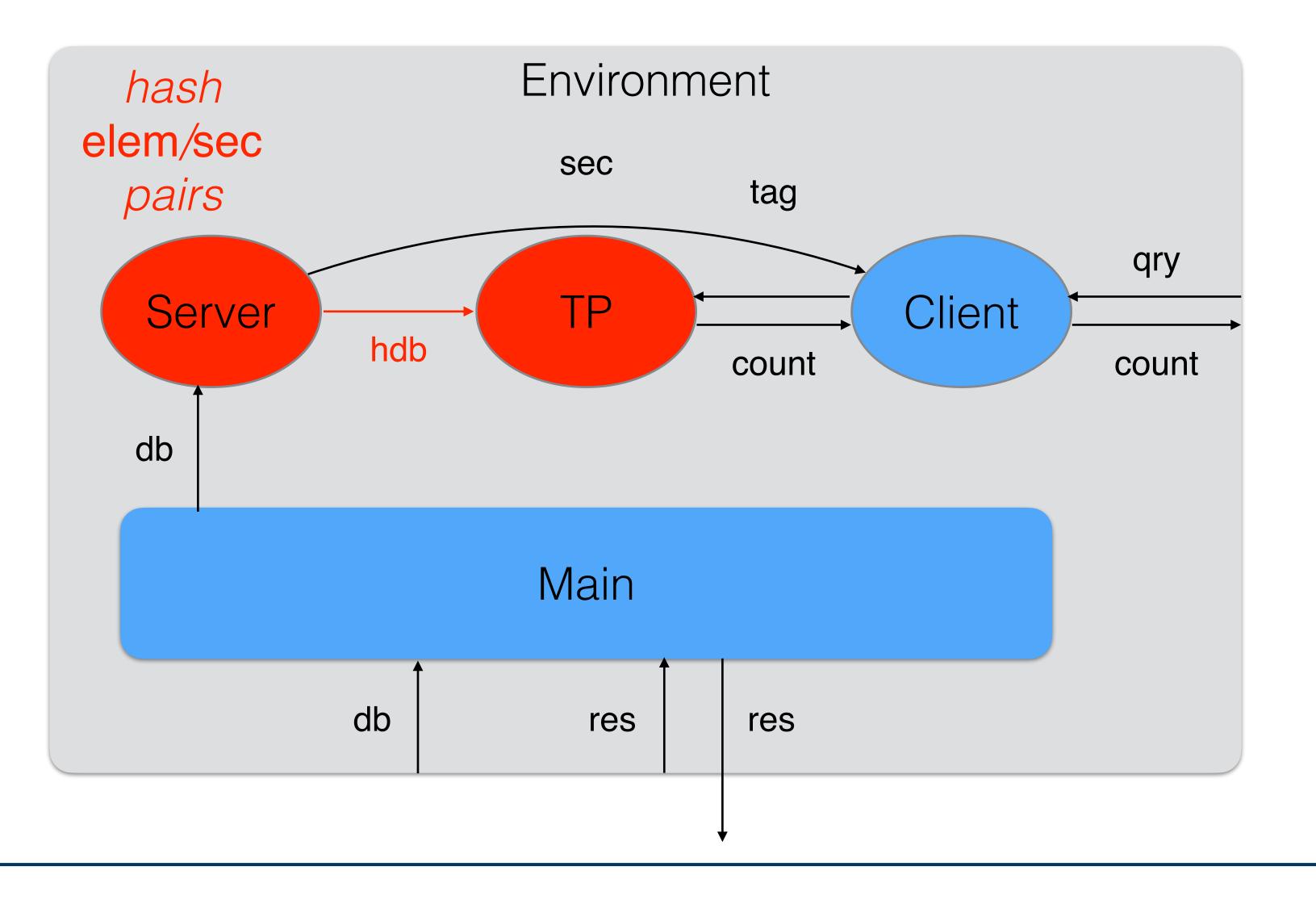








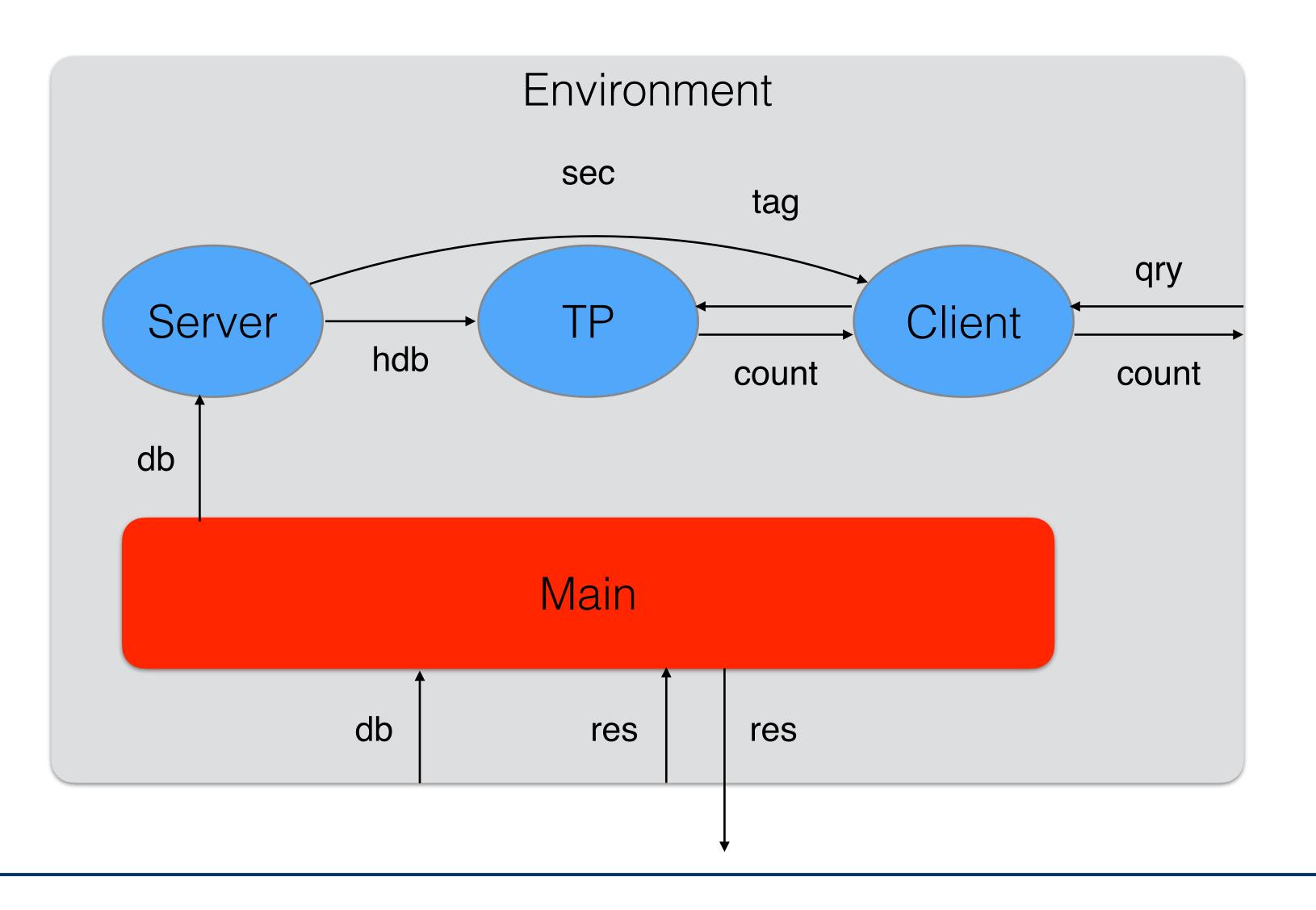




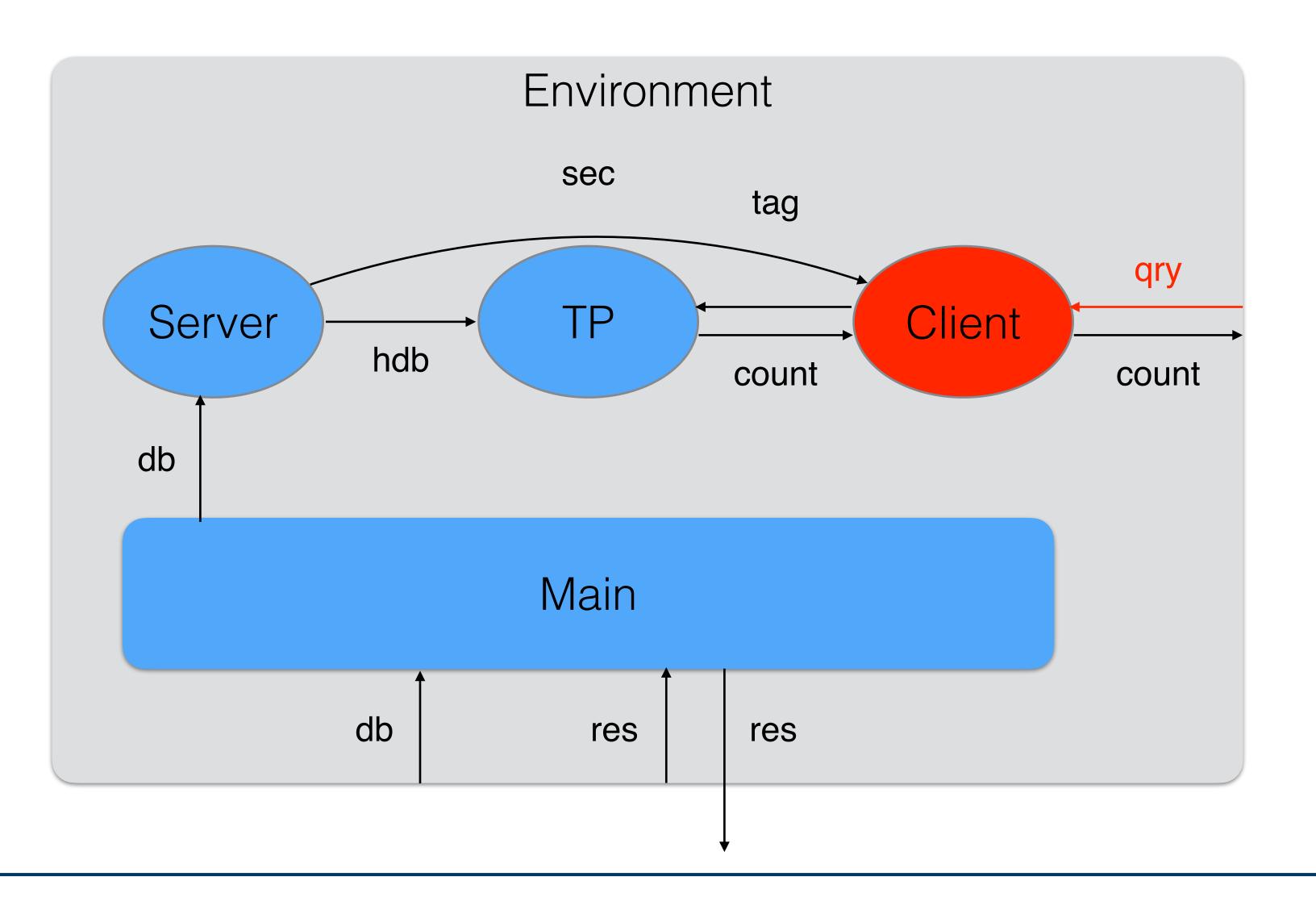
tags are bit strings of length tag\_len



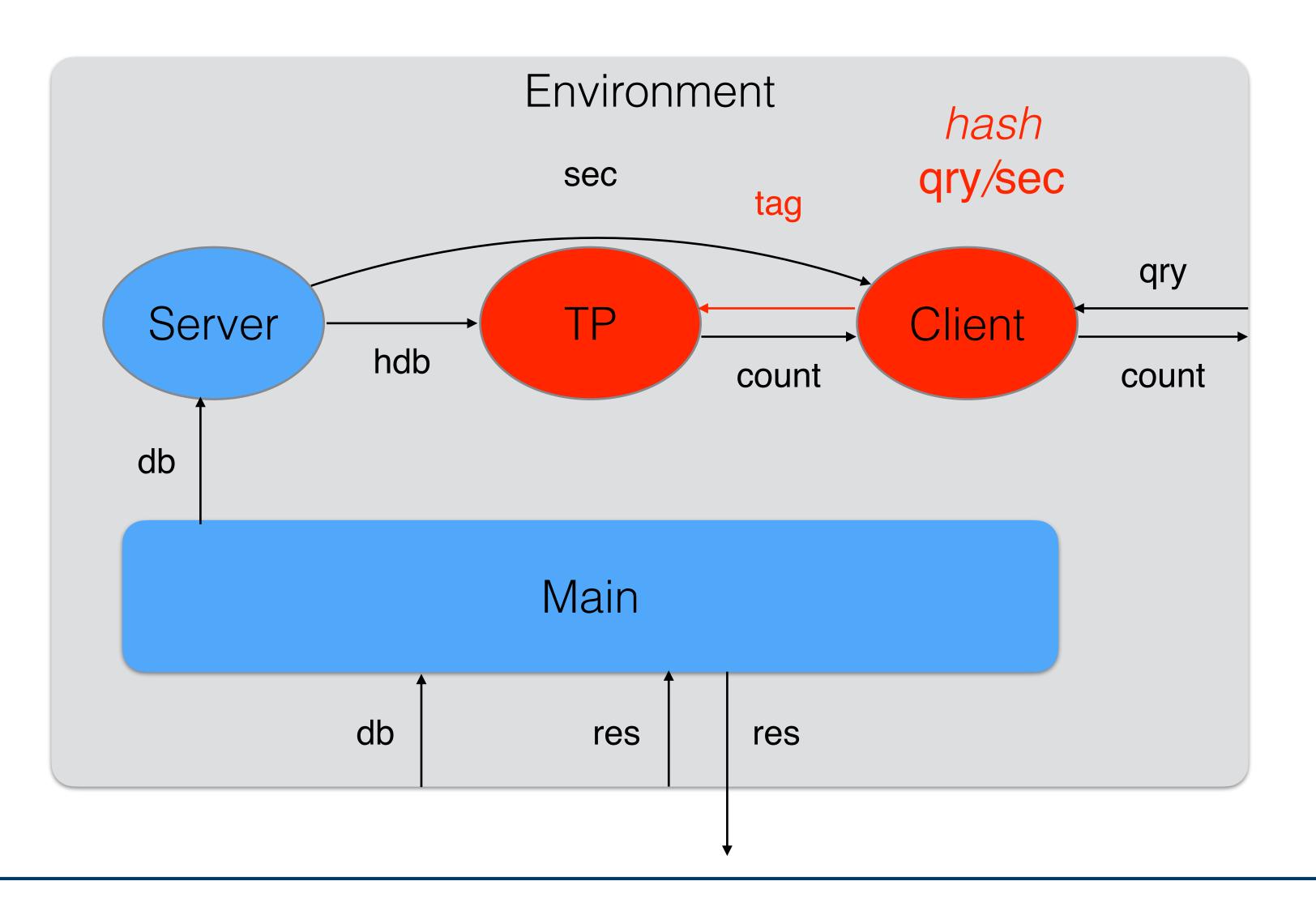




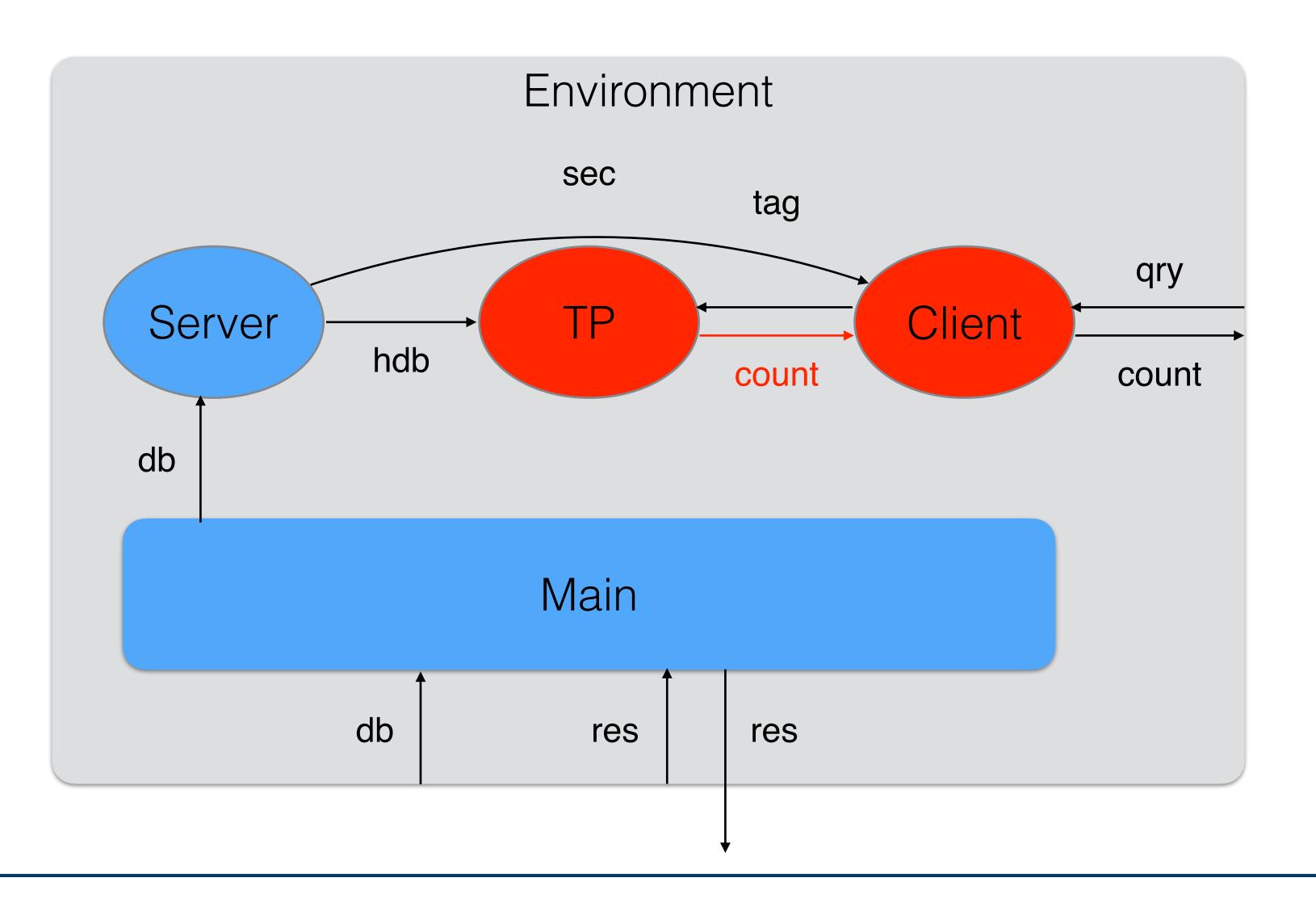
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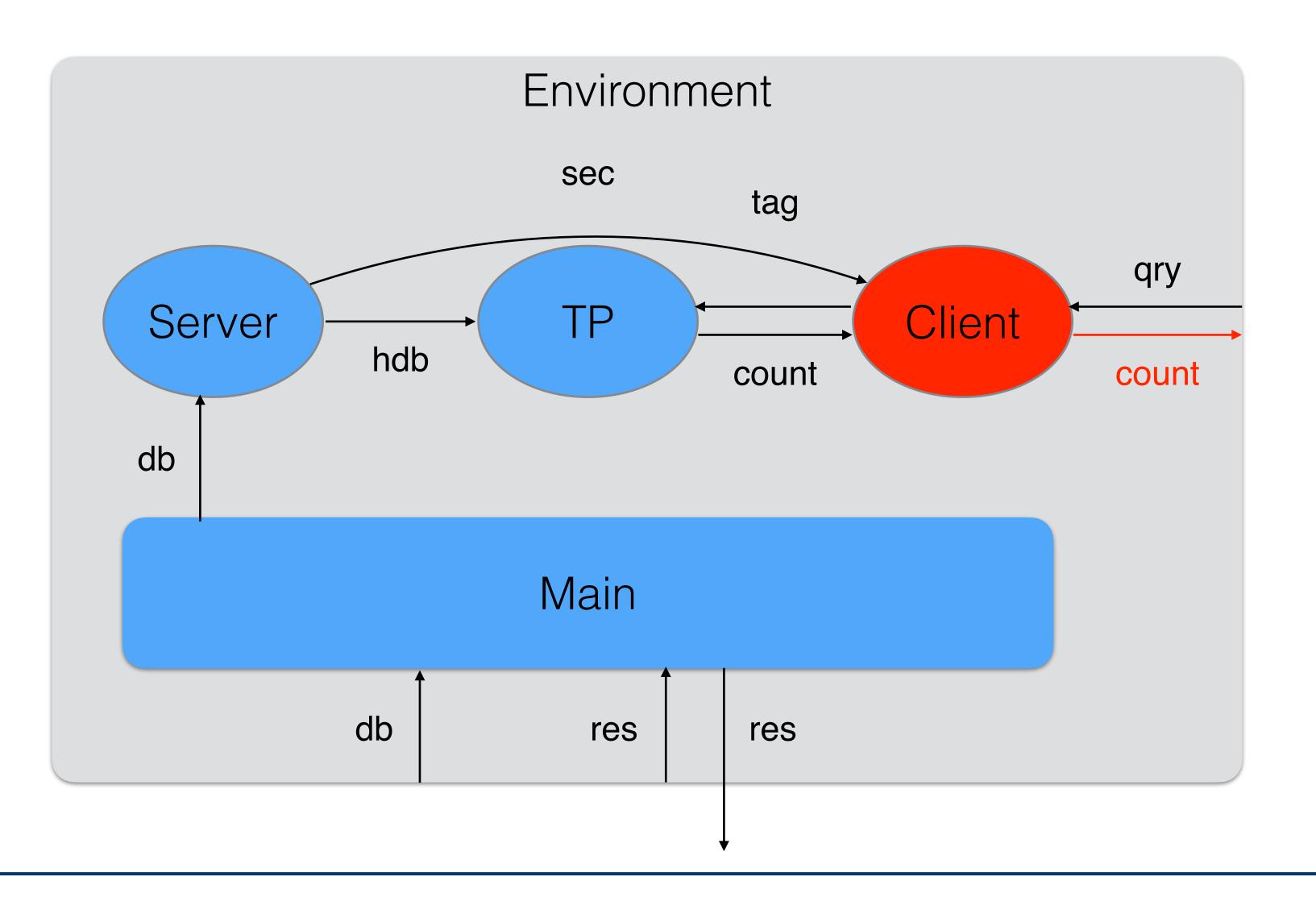




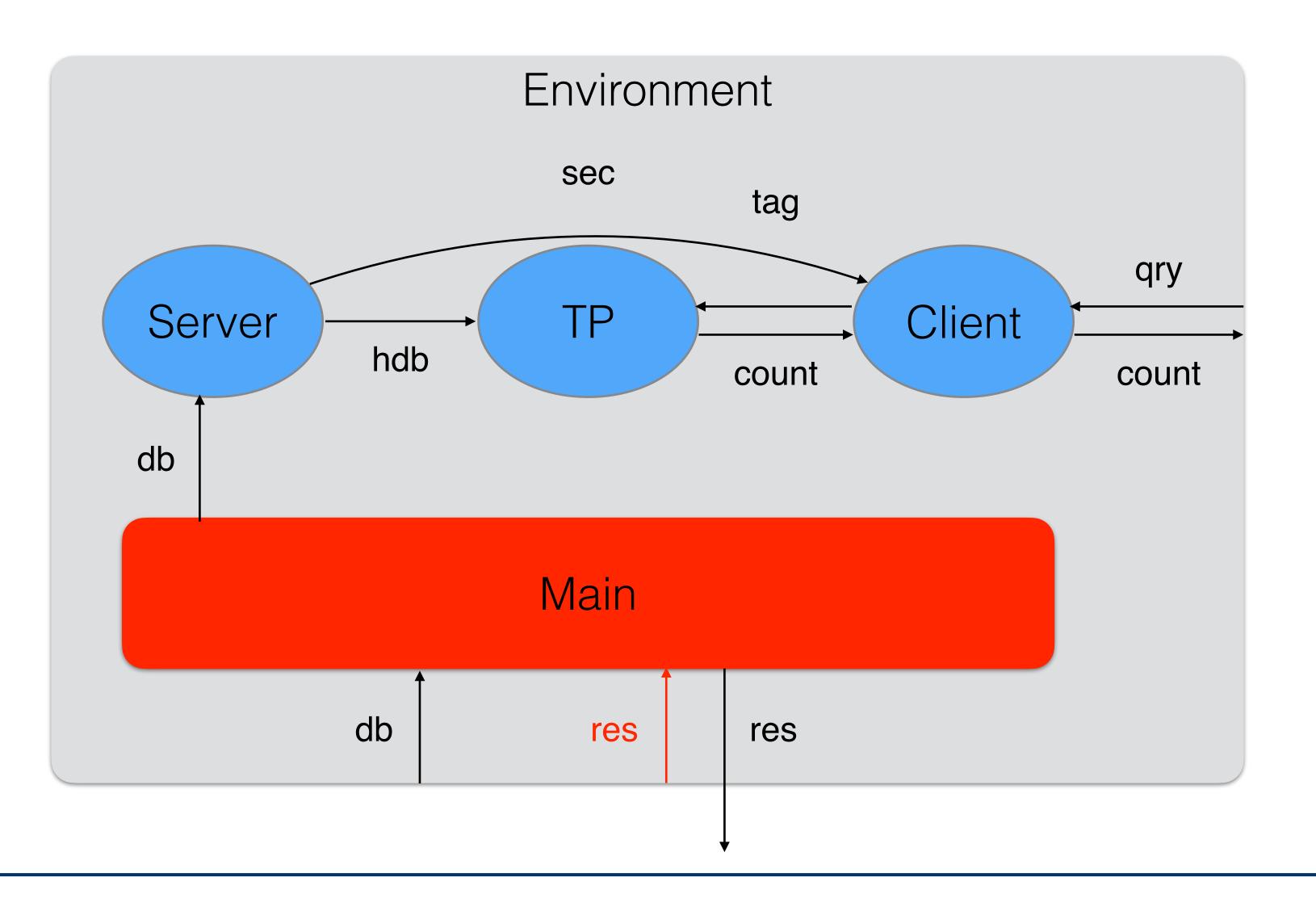




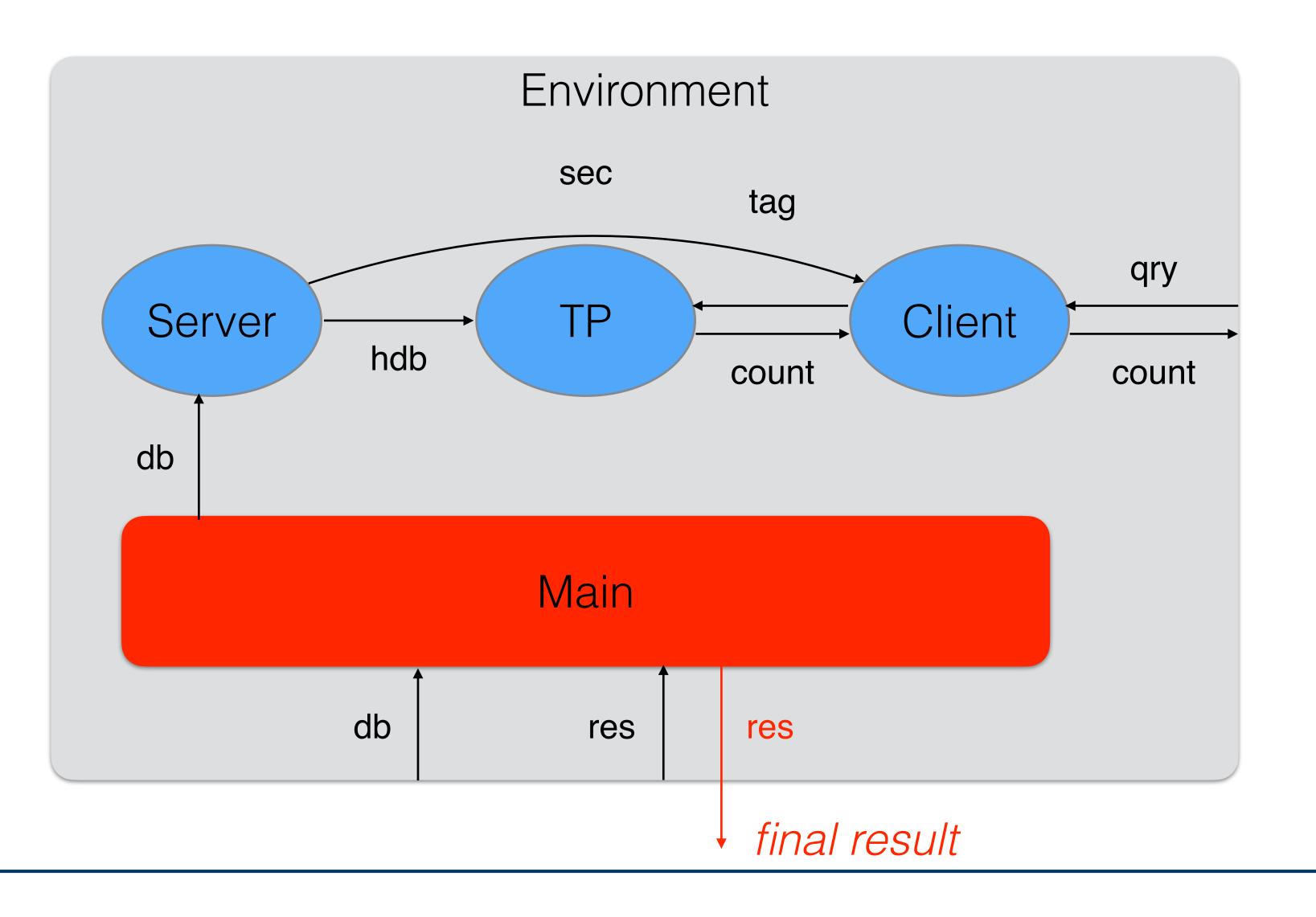
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- E.g., suppose the original database was [0; 1; 1; 2] and the queries are 1, 2 and 3
- The Server's shuffled database might be [1; 0; 2; 1]
- TP will get a hashed database [t<sub>2</sub>; t<sub>1</sub>; t<sub>3</sub>; t<sub>2</sub>] and hash tags t<sub>2</sub>, t<sub>3</sub> and t<sub>4</sub>, and so will return to Client counts 2, 1 and 0 (assuming no hash collisions)



- Next, we'll continue our treatment of Example 2:
  - Considering the EasyCrypt formalization of the protocol and the real and ideal games for each protocol party
  - Giving a high-level sketch of the proof of our security against the three parties

#### **New Material**



- Elements (type elem) may be anything
- Secrets (type sec) are bits strings of length sec\_len
- Hash tags (type tag) are bit strings of length tag\_len
- Hashing is done using a random oracle in which element/secret pairs are hashed to hash tags
  - Like the true random function of Example 1; memoizes answers in a finite map
  - Adversary can query the random oracle, but does not have direct access to its map

# Elements, Secrets and Hashing in EasyCrypt



```
type db = elem list. type hdb = tag list.
type server_view = server_view_elem list.
type tp_view = tp_view_elem list.
type client_view = client_view_elem list.
module type ENV = \{
  proc init_and_get_db() : db option
 proc get_qry() : elem option
 proc put_qry_count(cnt : int) : unit
 proc final() : bool
}.
```

### **PCR Protocol**

Each party has a *view* variable that records everything it sees



```
module Protocol (Env : ENV) = {
  module 0r = R0.0r
  proc main() : bool = {
    var db_opt : db option; var b : bool;
    init_views(); 0r.init();
    server_gen_sec(); client_get_sec();
    db_opt <@ Env.init_and_get_db();</pre>
    if (db_opt <> None) {
      server_hash_db(oget db_opt);
      tp_get_hdb();
      client_loop();
    }
    b <@ Env.final();</pre>
    return b;
```

### **PCR Protocol**

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```
proc client_loop() : unit = {
  var cnt : int; var tag : tag;
  var qry_opt : elem option;
  var not_done : bool <- true;</pre>
  while (not_done) {
    qry_opt <@ Env.get_qry();</pre>
    cv <- cv ++ [cv_got_qry qry_opt];</pre>
    if (qry_opt = None) {
      not_done <- false;</pre>
    } else {
      tag <@ Or.hash((oget qry_opt, client_sec));</pre>
      cnt <@ tp_count_tag(tag);</pre>
      CV <- CV ++
             [cv_query_count(oget qry_opt, tag, cnt)];
      Env.put_qry_count(cnt);
```

### **PCR** Protocol



- We are modeling what is called <u>semi-honest</u> or <u>honest-but curious</u> security
- In this model, the Adversary is given access to a given protocol party's view—the party's data—but it is not allowed to modify that data
- The Adversary is also given access to the hash procedure of the random oracle this is different from having access to its map
- The Real and Ideal games for each protocol party are parameterized by the Adversary
- The Adversary tries to learn more from the protocol's view plus the hash procedure's view of the random oracle than it should
- At the end of the games, the Adversary returns a boolean judgement, trying to make the probability it returns true be as different as possible in the Real and Ideal games



- specializations of Protocol
- party
- In calls to the Adversary, the party's current view is supplied
- The Real Game GReal is
  - parameterized by Adv : ADV

### **Real Games**

The Real Games for the Server, Third Party and Client are formed as

• For a given party, we define the module type ADV of Adversaries for that

defined by giving Protocol an environment Env made out of Adv



```
module type ADV(0 : R0.0R) = \{
  proc init_and_get_db(view : server_view) :
    db option {0.hash}
  proc get_qry(view : server_view) : elem option {0.hash}
  proc qry_done(view : server_view) : unit {0.hash}
 proc final(view : server_view) : bool {0.hash}
}.
```

- choose
- Queries are chosen one by one adaptively
- for the query
- knowledge

Adversary can do hashing when deciding which database and queries to

• qry done is called with server view, which does not include the count

• Each time the Adversary is called, it can do hashing to try to increase its



```
module GReal(Adv : ADV) = {
  module 0r = R0.0r
  module A = Adv(0r)
  module Env : ENV = \{
    proc init_and_get_db() : db option = {
      var db_opt : db option;
      db_opt <@ A.init_and_get_db(Protocol.sv);</pre>
      return db_opt;
    proc get_qry() : elem option = {
      var qry_opt : elem option;
      qry_opt <@ A.get_qry(Protocol.sv);</pre>
      return qry_opt;
    proc put_qry_count(cnt : int) : unit = {
      A.qry_done(Protocol.sv);
```



#### **Real Game for Server**

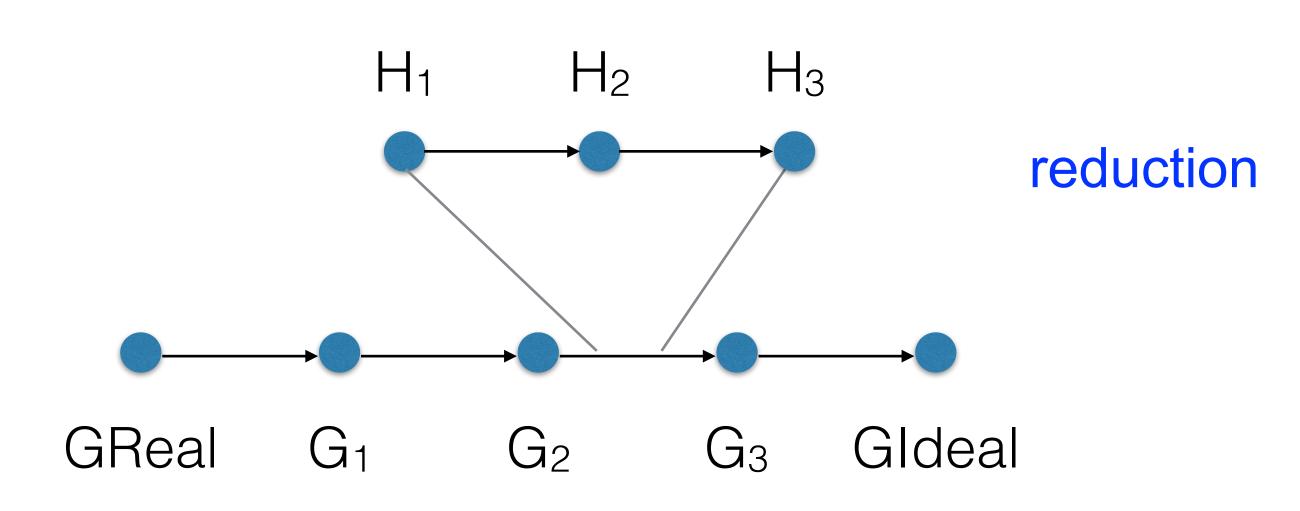
```
proc final() : bool = {
    var b : bool;
    b <@ A.final(Protocol.sv);
    return b;
    }
}
proc main() : bool = {
    var b : bool;
    b <@ Protocol(Env).main();
    return b;
}</pre>
```



- to the Adversary)
- Simulator's job is to convince the Adversary it's interacting with the real game: it must simulate the party's view and the hashing procedure's view of the random oracle state
- Because we are working information-theoretically, when assessing the information leakage from the Ideal Game to the Simulator (and thus Adversary), we don't have to scrutinize its Simulator
  - It can't learn more about the database or queries by brute force computation
- In fact, in our EasyCrypt security theorems, the Simulators are existentially quantified

A party's Ideal Game is also parameterized by a Simulator (in addition)



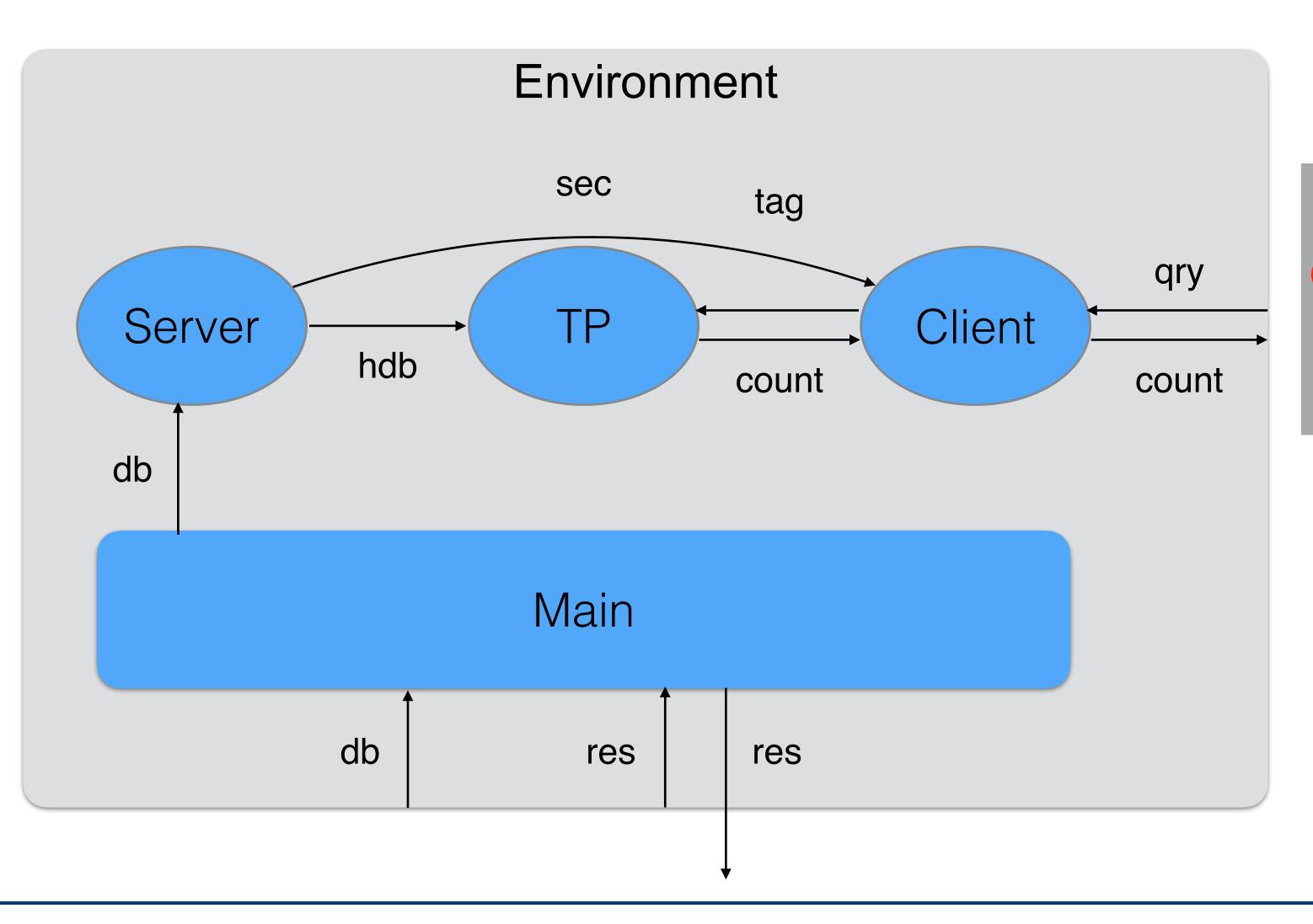


## **Two Dimensional Sequences of Games**

 When proving security against a protocol party, in connecting the real and ideal games we sometimes make use of a reduction, which is itself proved using a sequence of games (perhaps using a reduction, etc.).



### **Reminder: Real Game for Server**



Environment discards count before calling Adversary



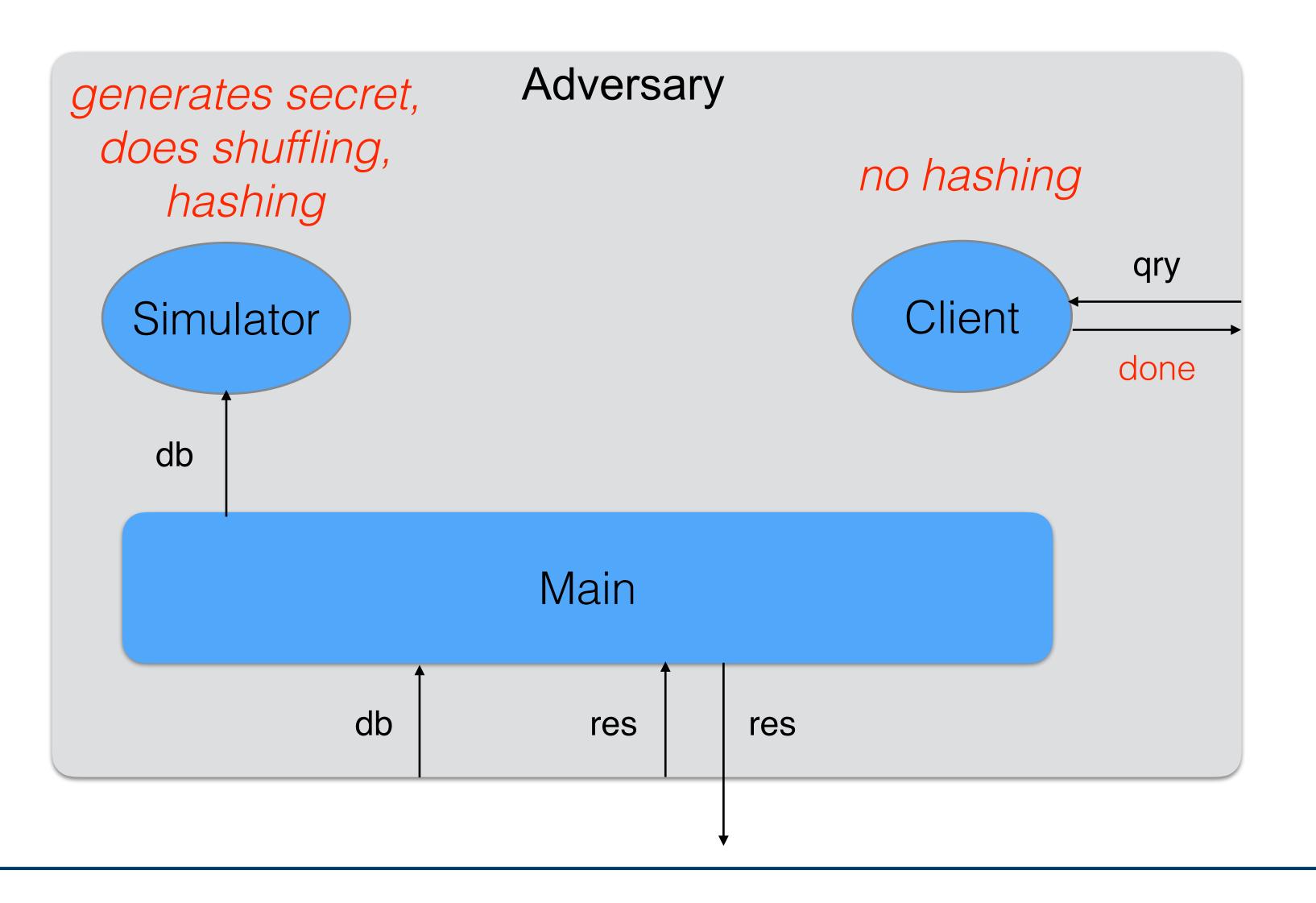


- What (if anything) can the Serve counts?
- We formalize this by asking what can be learned from the Server views that are passed to the Adversary — *plus the ability to run the hash procedure of the random oracle*
  - We need to "forget" that the Adversary is choosing the queries, and so clearly knows them.
  - We can think that each time the Adversary is called, the Server is woken up
- To answer and prove this, we need to formalize an Ideal Game

• What (if anything) can the Server learn about the queries and their



#### Ideal Game for Server





- The Simulator doesn't directly learn anything about the queries, and so the Server views it simulates can't convey anything about them either
- And the query loop doesn't modify the random oracle, so experimentation with the random oracle won't learn anything either
- But because the Server is woken up each iteration of the query loop, the Server does learn the number of queries



return true:

lemma GReal\_GIdeal :

exists (Sim <: SIM{-GReal, -GIdeal}),</pre> forall (Adv <: ADV{-GReal, -GIdeal, -Sim}) &m,</pre> Pr[GReal(Adv).main() @ &m : res] = Pr[GIdeal(Adv, Sim).main() @ &m : res].

- the Client in the Real but not the Ideal Game

• We are able to prove perfect security: Real/Ideal games equally likely to

The only challenge is dealing with the redundant hashing performed by

• We remove it using a variation of a technique due to Benjamin Grégoire



## **Redundant Hashing**

```
module type HASHING = \{
 proc hash(inp : input) : output (* ordinary hashing *)
 proc rhash(inp : input) : unit (* redundant hashing *)
}.
module type HASHING ADV(H : HASHING) = \{
 proc main() : bool {H.hash H.rhash}
```

Two implementations of HASHING, both built from a random oracle 0:

- hashes its input, but discards the result

}.

NonOptHashing (``non optimized hashing"), in which rhash

OptHashing (``optimized hashing"), where rhash does nothing



# **Redundant Hashing**

```
module GNonOptHashing(HashAdv : HASHING_ADV) = {
  module H = NonOptHashing(Or)
  module HA = HashAdv(H)
  proc main() : bool = {
    var b : bool;
    Or.init(); b <@ HA.main();</pre>
    return b;
}.
module GOptHashing(HashAdv : HASHING_ADV) = {
  module H = OptHashing(Or)
  module HA = HashAdv(H)
  proc main() : bool = {
    var b : bool;
    Or.init(); b <@ HA.main();</pre>
    return b;
```



lemma GNonOptHashing\_GOptHashing (HashAdv <: HASHING\_ADV{0r}) &m :</pre> Pr[GNonOptHashing(HashAdv).main() @ &m : res] = Pr[GOptHashing(HashAdv).main() @ &m : res].

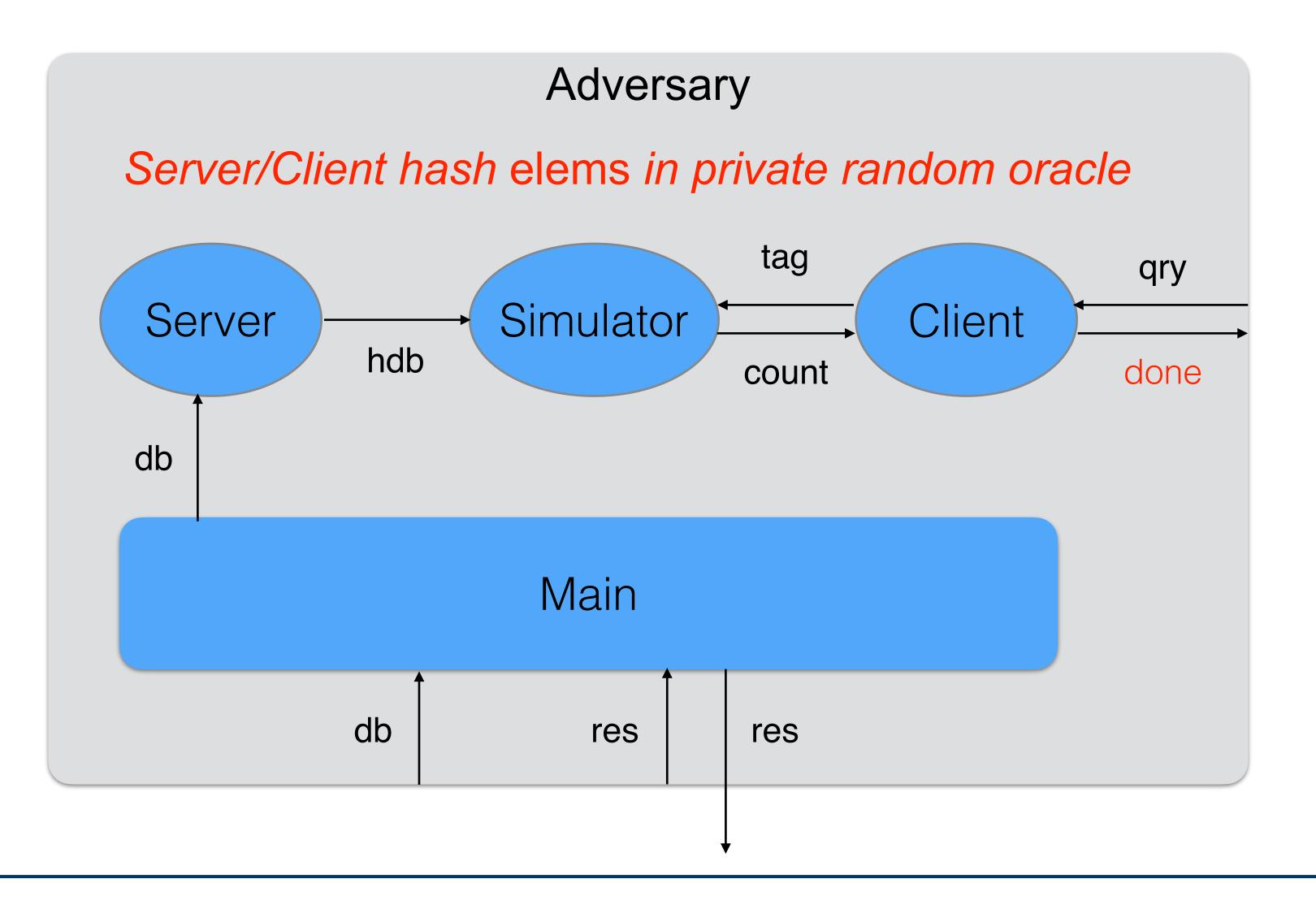
- superseded by hash or no longer necessary
  - Proof uses EasyCrypt's eager tactics
- sequence of games proof can be connected with be connected with the right side of the gap

Proof intuition: redundant hashing can be put off until it's

To use in Server proof, we define a concrete adversary HashAdv in such a way that the left side of the gap in the GNonOptHashing(HashAdv), and GOptHashing(HashAdv) can



# **Ideal Game for Third Party**





- The Adversary is invoked with the TP's view when the database and queries are requested by the game and client loop
- In the Ideal Game, Adversary only learns patterns, not anything more about the database and queries
  - It doesn't have access to the private random oracle used by Server/ Client
  - So even though the database and queries were used to derive the hashed database [t<sub>1</sub>; ...; t<sub>n</sub>] and query tags s<sub>1</sub>, ..., s<sub>m</sub>, these tags were all randomly (but consistently) chosen, and so convey no information about the particular elements
  - And the Server's random shuffling means it doesn't learn anything about the order of the database



- E.g., suppose the original database was [0; 1; 1; 2]
- The Server's shuffled database might be [1; 0; 2; 1]
- In the Real Game, TP will get a hashed database [t<sub>2</sub>, t<sub>1</sub>, t<sub>3</sub>, t<sub>2</sub>], where t1 = hash(0, sec), t2 = hash(1, sec) and t3 = hash(2, sec) for the shared Server/Client sec
- In the Ideal Game, TP will get a hashed database with the same pattern, [s<sub>2</sub>; s<sub>1</sub>; s<sub>3</sub>; s<sub>2</sub>], but where the s<sub>i</sub> have no connection with hash or sec
- In order to tell the games apart, we can prove it has to guess sec, i.e., call hash with a pair whose second component is sec



- different number of times (e.g., [0; 1; 1; 2; 2; 2; ...]).
- tags t with their elements e.
- Given a particular (e, t) pair, it can search for a sec' such that another choice of sec'.

• To try to differentiate the games, the Adversary can pick a database with a large number of distinct elements, where each element appears a

 When given (in TP's view) the hashed database that was created in the Real or Ideal Game from shuffling the database and then hashing its elements (either paired with sec in the random oracle, or in the private random oracle), it can (assuming no hash collisions) match the resulting

hashing (e, sec') results in t. When it finds one, it can check that the rest of the hashed database is consistent with sec'. Otherwise it can try



- This process is guaranteed to succeed in the Real Game, it's highly unlikely to succeed in the Ideal Game
- In any event, if the Adversary never calls the random oracle with a pair whose second component is sec, we can prove it will fail to distinguish the Real and Ideal Games



- To obtain a security theorem, we must limit (limit) the number of distinct inputs the Adversary may hash
  - The Server and Client are unrestricted
- We use a reduction to bridge the Real and Ideal Games one proved with up-to-bad reasoning — and so that makes us assume the Adversary's procedures are lossless (always terminating), and prove that the Client Loop always terminates
- When we form GReal and Gldeal, we terminate the Client Loop after qrys\_max steps (in GReal, by returning None from the environment's get\_gry procedure)

# **Proof of Security Against Third Party**



```
    Here is the relevant part of the Environment for GReal:

  module Env : ENV = \{
    var qrys_ctr : int
    proc get_qry() : elem option = {
      var qry_opt : elem option;
      qry_opt <@ A.get_qry(Protocol.tpv);</pre>
      if (qry_opt <> None) {
        if (qrys_ctr < qrys_max) { qrys_ctr <- qrys_ctr + 1; }</pre>
        else { qry_opt <- None; }</pre>
      }
      return qry_opt;
```

# **Proof of Security Against Third Party**



- We reduce security against TP to t Random Oracles"
- They offer *limited* (limit) hashing of element/secret pairs (what Adversary does), as well as *unlimited* hashing of elements (what Server and Client do)
- "Dependent" implementation with single map, where hashing an element is same as hashing pair of it and sec — connection with Real Game
- "Independent" implementation with separate maps connection with Ideal Game
- We prove that a Secrecy Adversary can only tell the games involving the two implementations apart if it does limited hashing of a pair whose second component is sec

We reduce security against TP to the security of a new abstraction, "Secrecy



- The Secrecy Random Oracles proof is carried out using up-to-bad reasoning
- As long as the Secrecy Adversary doesn't do limited hashing with a pair with right side sec (the "bad" event), we can maintain an invariant:
  - keeping the non-sec-part of the map of the dependent implementation in sync with the non-sec-part of the elem \* sec map of the independent implementation; and
  - keeping the sec-part of the map of the dependent implementation in sync with the elem map of the independent implementation



- We reduce the upper-bounding of the probability of the bad event holding to a lemma about another new abstraction, "Secret Guessing Oracles"
  - It gives the adversary limited (limit) number of chances to guess sec — but it doesn't get any feedback during the guessing
  - EasyCrypt's pHL is used to upper bound the probability of the adversary winning by

 Both the Secrecy Random Oracles and Secret Guessing Oracles definitions and proofs are packaged up into reusable theories

#### limit / 2sec\_len



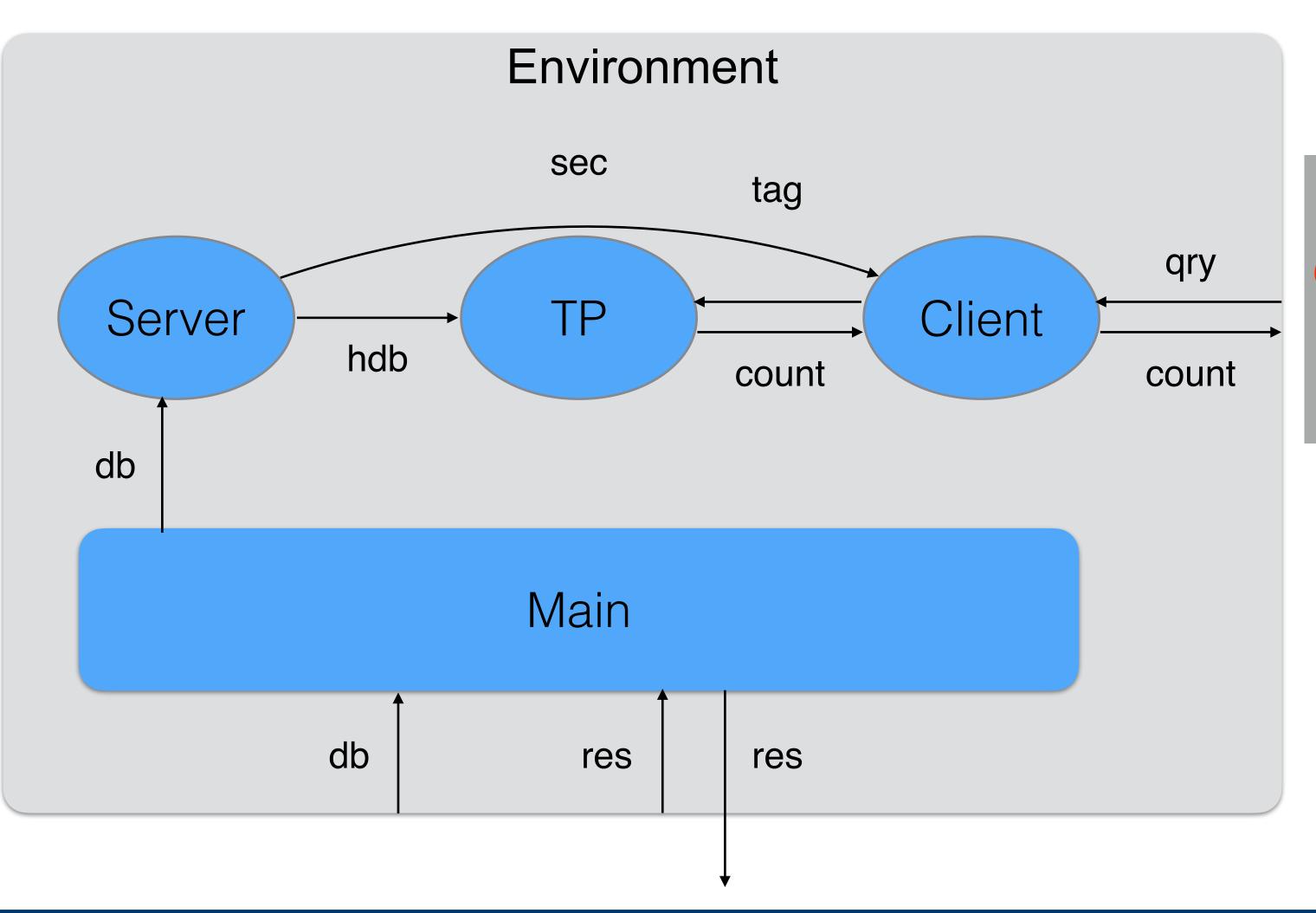
# **Third Party Proof**

limit / 2sec\_len

• The theorem for security against the TP upper-bounds the distance between the probabilities of the Real and Ideal Games returning true by



# **Reminder: Real Game for Client**

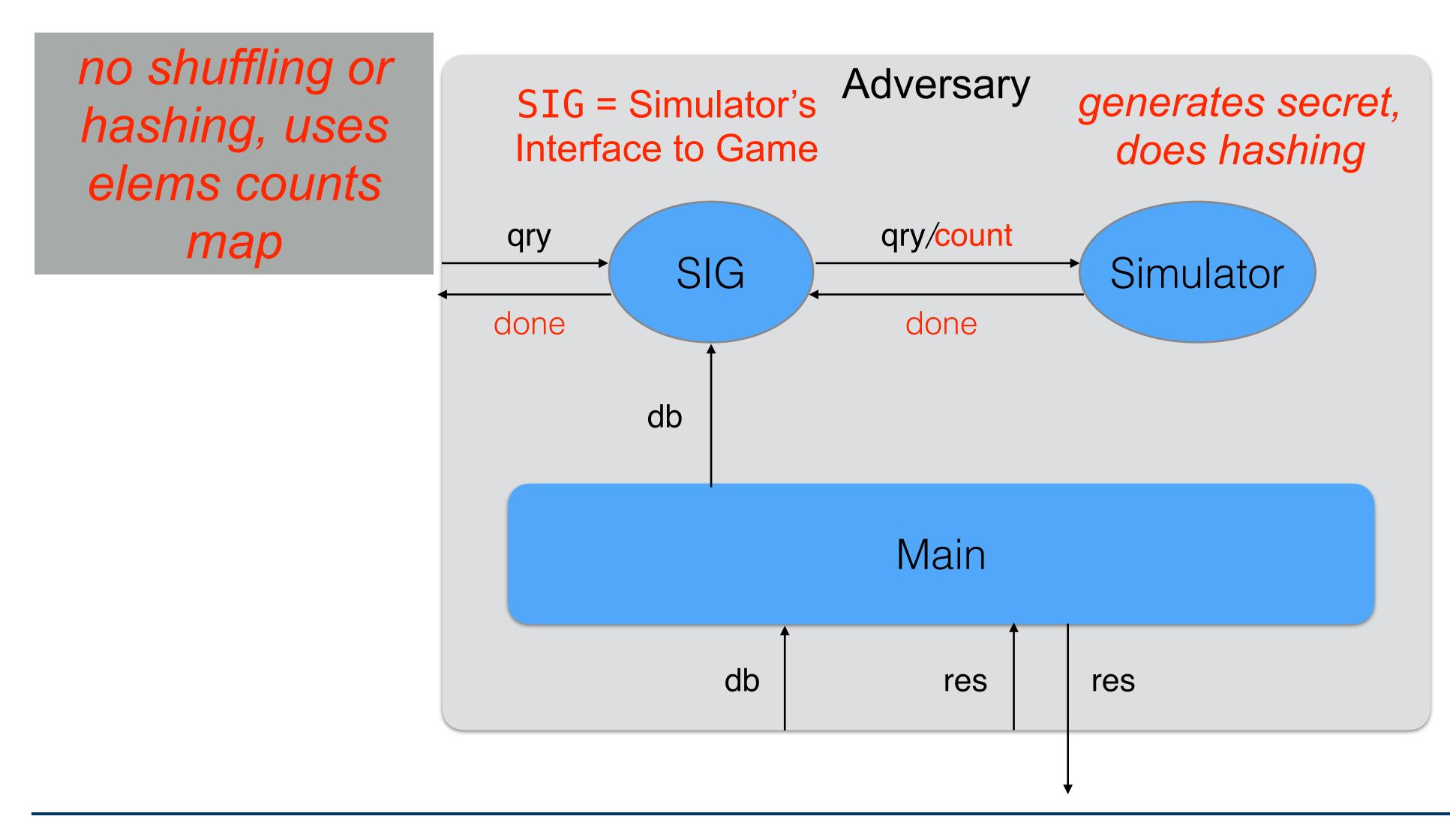


Environment discards count before calling Adversary





## Ideal Game for Client





- forcing a hash collision
- [elem] and the only query be elem'
  - In Real Game, count will be
  - In Ideal Game, count will be 0
- queries

The Adversary can distinguish the Real and Ideal Games by causing or

 If it can find distinct elem and elem' such that (elem, sec) and (elem', sec) hash to the same hash tag, tag, then it can let db =

 It can let db be a list of distinct elements of greater length than number of distinct hash tags, and work through that same list of elements as



- Thus we must impose a hashing budget on the Adversary not just on the hashing it does directly, but also on the hashing it makes Server and Client do:
  - adv\_budget distinct hashing done by Adversary
  - db\_uniqs\_max maximum number of distinct elements in database
  - qrys\_max maximum number of queries
- budget = adv\_budget + db\_uniqs\_max + qrys\_max
- If Adversary doesn't respect budget, we terminate game early (we terminate the Client Loop after qrys\_max steps)
- Because the proof uses up-to-bad reasoning, we need that Adversary is always terminating and Client Loop terminates

# **Proof of Security Against Client**



- We have Budgeted Random Oracles, which provide: separate budgeted hashing procedures for the Adversary, Server and
  - Client
  - set a flag when over budget, but keep working
  - for Adversary and Server, only distinct inputs matter, but for Client its the number of hashes
  - ordinary (unrestricted) hashing (which the Adversary uses before making its final judgement)
- There are two implementations of budgeted random oracles:
  - a "collision-possible" one in which hash collisions may occur
  - a "collision-free-while-within-budget" one in which hash collisions don't happen if only budgeted hashing is done and all budgets respected



- Each move back and forth between the collision-possible and collisionfree-while-within-budget versions incurs a penalty of (budget \* (budget - 1)) / 2tag\_len + 1
- This is proved using up-to-bad reasoning, where the "bad" event is when a collision occurs
- EasyCrypt's failure event lemma and pHL are used to bound the probability that failure occurs
- The proof is packaged into a reusable theory

# **Proof of Security Against Client**



- Move to collision-possible budgeted random oracle
- Move to collision-free-while-within-budget random oracle
- Use complex relational invariant to switch to Server, TP and Client using an elements counts map instead of hashed database (but Server still does hashing)
- Switch back to collision-possible budgeted random oracle • Switch back to ordinary random oracle (Adversary still subjected to budget)
- Get rid of Server's hashing, which is now seen to be redundant Show that computing elements counts map works out same without first shuffling database
- Final refactoring

# **Client Proof**



 Theorem for security against the Client upper bounds the distance between the probabilities of the Real and Ideal Games returning true by (budget \* (budget - 1)) / 2tag\_len which is two times (budget \* (budget - 1)) / 2tag\_len + 1

# **Client Proof**



- Size of EasyCrypt formalization:
  - About 380 lines of theorem statements and relevant definitions (random oracles, protocol definition, etc.)
  - About 5,275 lines of proof (which one can trust EasyCrypt to check)
- Formalizing Protocol once parameterized by Environment and then specializing to Real Games works well
- Because we work information-theoretically, Simulators are existentially quantified (so part of proof, not specification)
- Removing redundant hashing was crucial, and our version of Grégoire's technique was proved once and used twice



- Use of budgeted random oracles in Client proof let us do the hard step of the proof without worrying about hash collisions
- EasyCrypt made it easy to obtain concrete upper bounds in terms of game parameters on the distances between real and ideal games



- queries?
- A: Not in the highly unlikely event of hash collisions
- Q: Why do we let the Adversary choose the database and queries?
  - A: This models how it may have inside information about what elements (e.g., people's names) are likely to appear in the database or in queries
    - appearing numerous times corresponds to "Alice", based on guess.

• Q: In the PCR Protocol, does the Client always get correct counts for its

• E.g., TP, when analyzing the tags it sees, might guess that a tag knowledge of an organization. But it won't be able to confirm that



- other one eavesdropping?
- special access to the network

#### Discussion

• Q: Is it realistic to assume two parties can communicate, without the

• A: Yes. The Adversary works on behalf of a given party, and has no



- Q: Are the restrictions we place on the Adversary realistic?
  - A: Server:
    - No restrictions
  - A: TP:
    - Limit on distinct hashes
  - A: Client:
    - Budget for Adversary's distinct hashing
    - Budget on number of distinct elements in database
    - Budget on number of queries

#### Discussion

in reality, the Adversary doesn't choose the database or queries



### **Example 2: Private Count Retrieval**

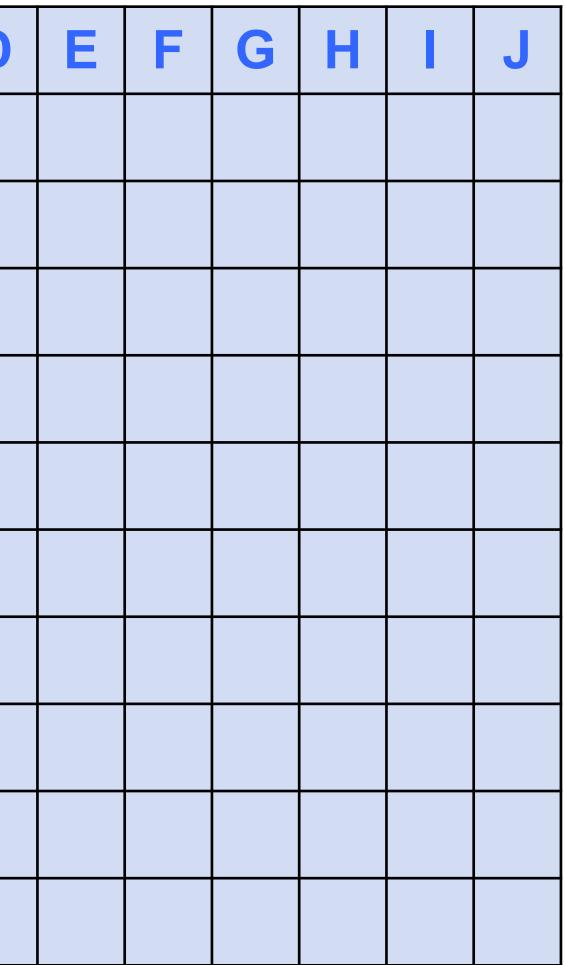
# Questions about Example 2?



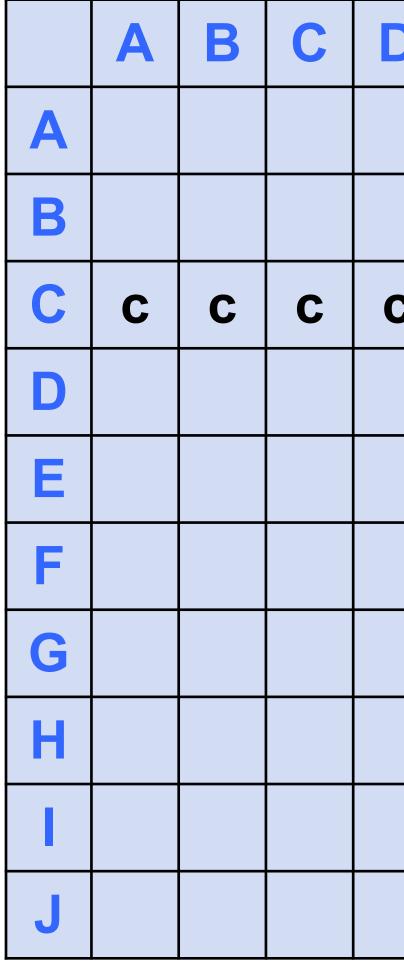
- In our final example, we'll apply the Real/Ideal Paradigm to the security of the two-player board game Battleship
- Information Flow Control) Library, and Concurrent ML with home-grown access control — both of which are implemented using data abstraction
- We'll be looking at program security in Haskell with the LIO (Labeled IO) • We'll define security in this non-probabilistic (but possibilistic, due to thread scheduling) setting.
- And we'll explain how we used the definition of security to audit our **Battleship implementations**
- Joint work with former colleagues at MIT Lincoln Laboratory



	Α	В	С	D
Α				
В				
С				
D				
Ε				
F				
G				
Η				
J				







#### Carrier

Ε	F	G	Н	J
С				



	Α	В	С	D	Ε	F	G	Н	J
Α									
В						b			
С	С	С	С	С	С	b			
D						b			
Ε						b			
F									
G									
Η									
J									

#### Battleship



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	Α	В	С	D
Α				
В				
С	С	С	С	С
D				
Ε				
F				
G				
Η				
J				

Ε	F	G	н	I	J
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С	b				
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#### Submarine



	Α	В	С	D
Α				
В				
С	С	С	С	С
D				
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J				

Ε	F	G	Н	J
	b			
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	b			
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		d		
		d		





	Α	В	С	D
Α				
В				
С	С	С	С	С
D				
Ε				
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G			р	
H			р	
J				

#### Patrol Boat

Ε	F	G	н	I	J
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С	b				
	b				
	b				
S	S	S			
		d			
		d			
		d			





#### **Player's Board**

	Α	В	С	D	Ε	F	G	Η	J
Α									
В						b			
С	С	С	С	С	С	b			
D						b			
Е						b			
F									
G			р		S	S	S		
н			р				d		
1							d		
J							d		

# Battleship Rules Shooting

#### **Opponent's Shooting Record**

	Α	В	С	D	Ε	F	G	Η	J
Α									
В									
С									
D									
Ε									
F									
G									
Н									
1									
J									



#### **Player's Board**

	Α	В	С	D	Ε	F	G	Η	J
Α									
В						b			
С	С	С	С	С	С	b			
D						b			
Е						b			
F									
G			р		S	S	S		
н			р				d		
1							d		
J							d		

#### **Battleship Rules** Shooting

#### **Opponent's Shooting Record**

	Α	В	С	D	Ε	F	G	Η	I	J
Α										
В										
С										
D										
Е										
F										
G										
н										
J										

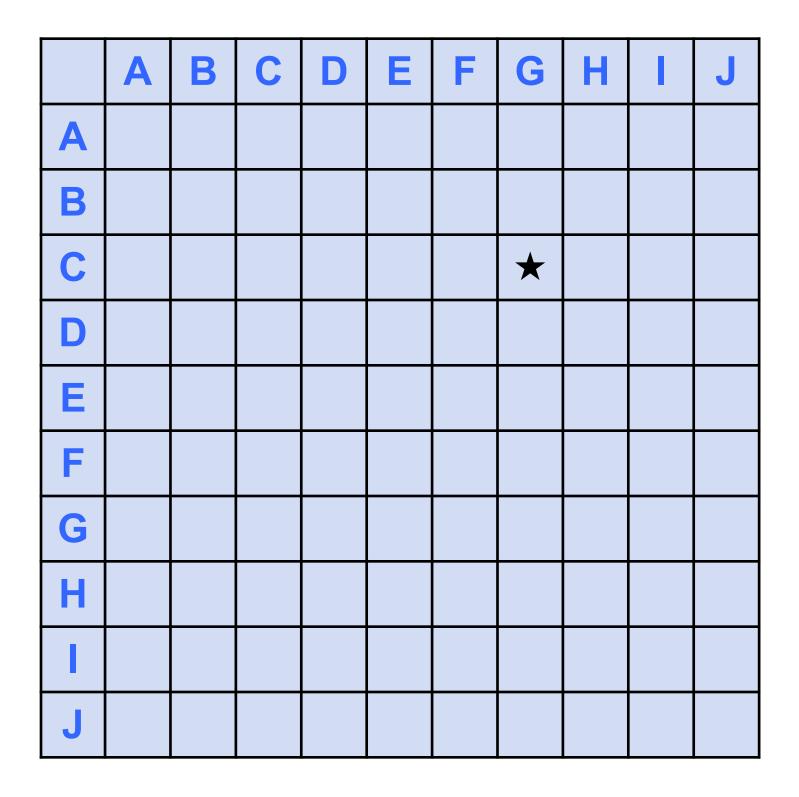
Shoot CG –



	Α	В	С	D	Ε	F	G	Η	T	J
Α										
В						b				
С	С	С	С	С	С	b	$\star$			
D						b				
Е						b				
F										
G			р		S	S	S			
н			р				d			
1							d			
J							d			

## **Battleship Rules** Shooting

#### **Opponent's Shooting Record**



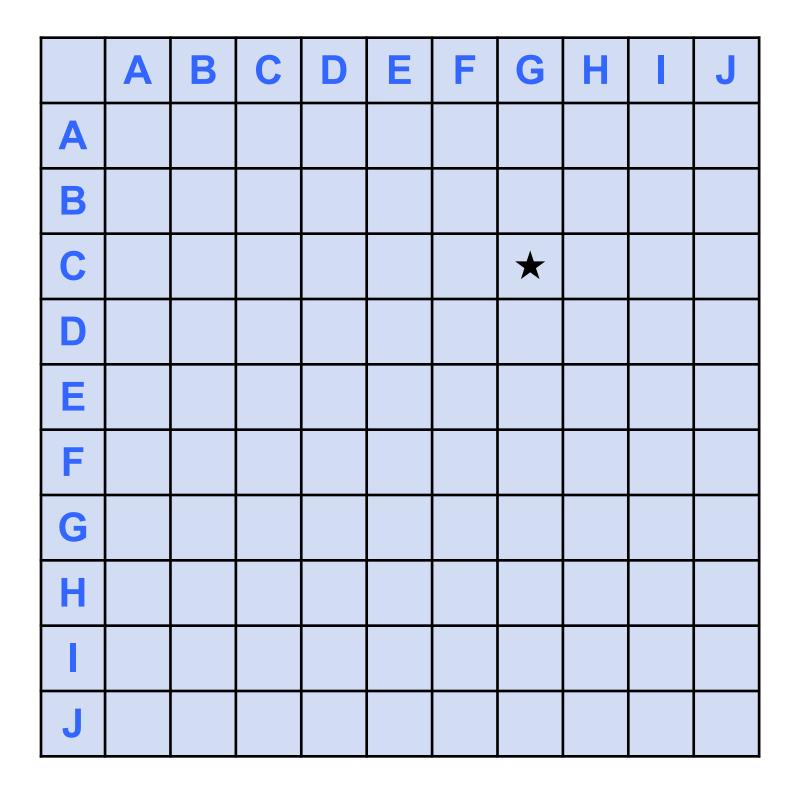
Shoot CG – "Miss"



	Α	В	С	D	Ε	F	G	Η	T	J
Α										
В						b				
С	С	С	С	С	С	b	$\star$			
D						b				
Е						b				
F										
G			р		S	S	S			
н			р				d			
1							d			
J							d			

## Battleship Rules Shooting

#### **Opponent's Shooting Record**



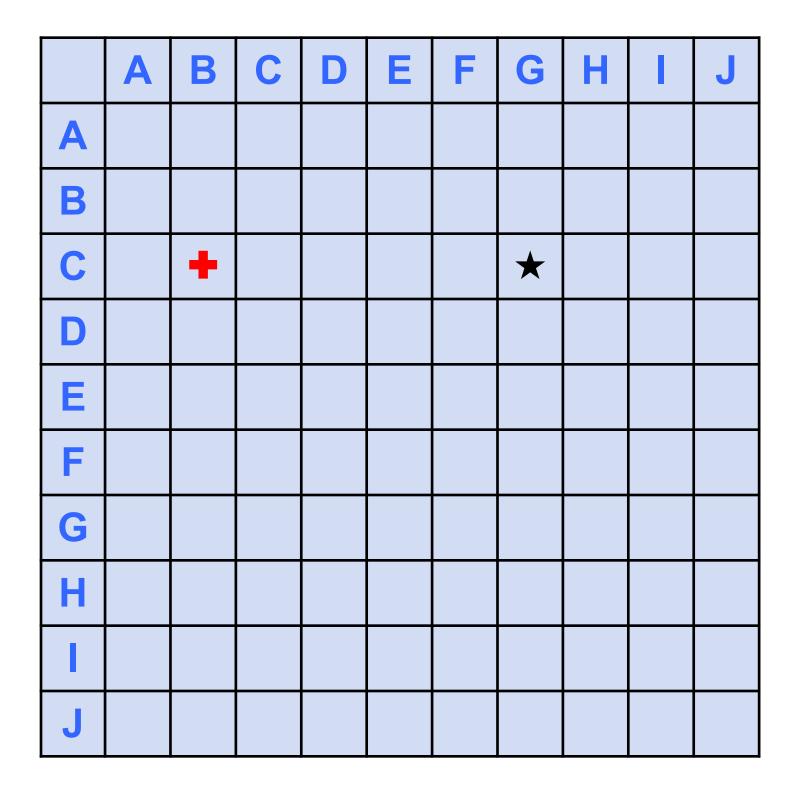
Shoot CB –



	Α	В	С	D	Ε	F	G	Η	T	J
Α										
В						b				
С	С	С	С	С	С	b	$\star$			
D						b				
Е						b				
F										
G			р		S	S	S			
н			р				d			
1							d			
J							d			

## **Battleship Rules** Shooting

#### **Opponent's Shooting Record**



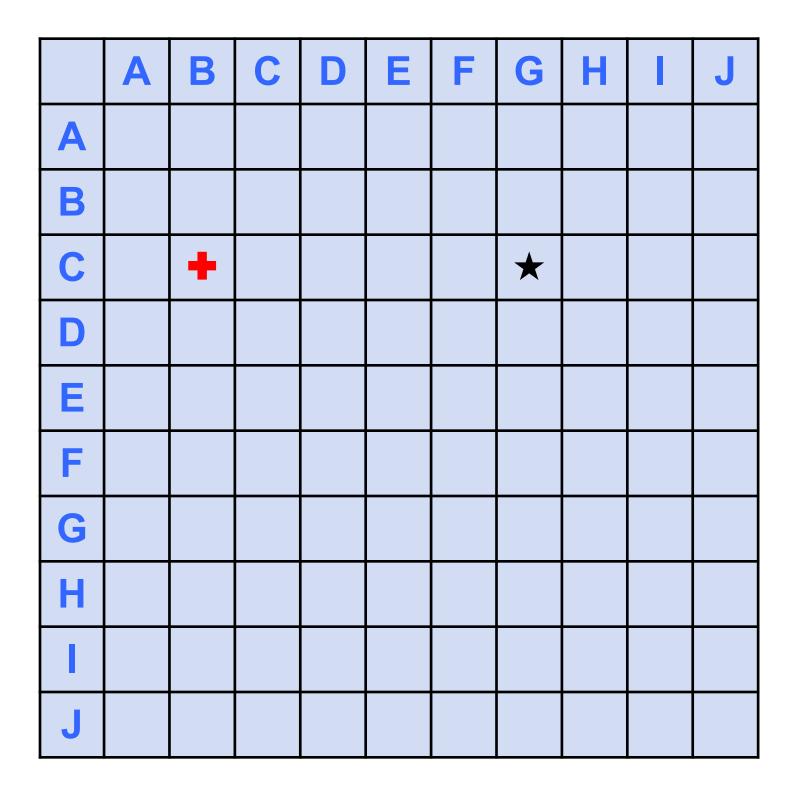
Shoot CB – "Hit"

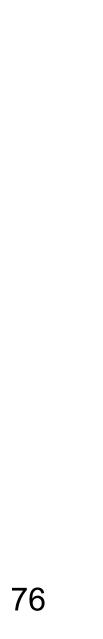


	Α	В	С	D	Ε	F	G	Η	I.	J
Α										
В						b				
С	С	С	С	С	С	b	*			
D						b				
Е						b				
F										
G			р		S	S	S			
н			р				d			
							d			
J							d			

Shoot DB –

## **Battleship Rules** Shooting

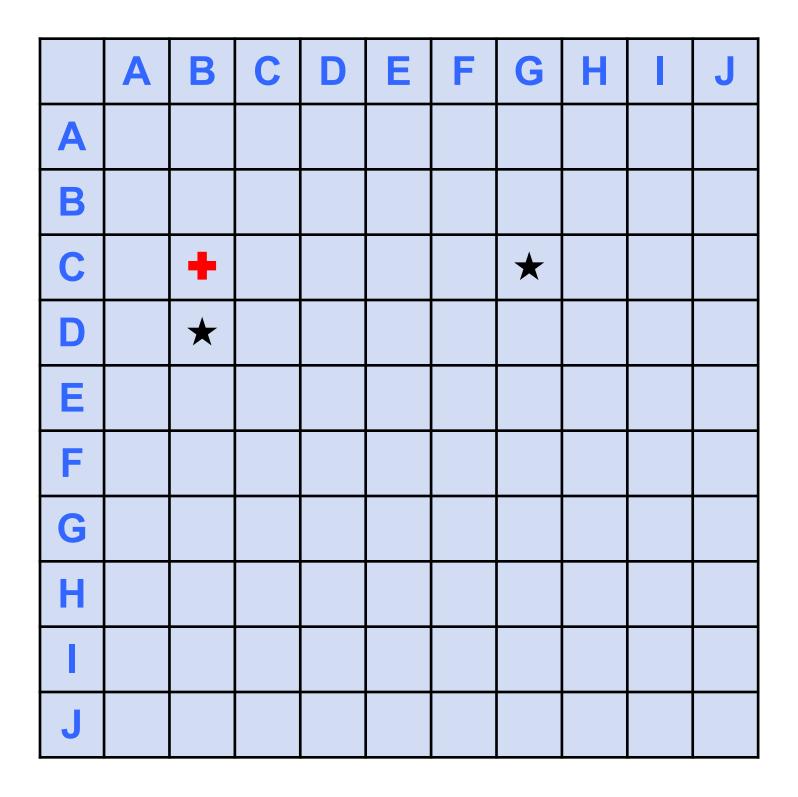




	Α	В	С	D	Ε	F	G	Η	I.	J
Α										
В						b				
С	С	С	С	С	С	b	*			
D		$\star$				b				
Е						b				
F										
G			р		S	S	S			
н			р				d			
1							d			
J							d			

## **Battleship Rules** Shooting

#### **Opponent's Shooting Record**



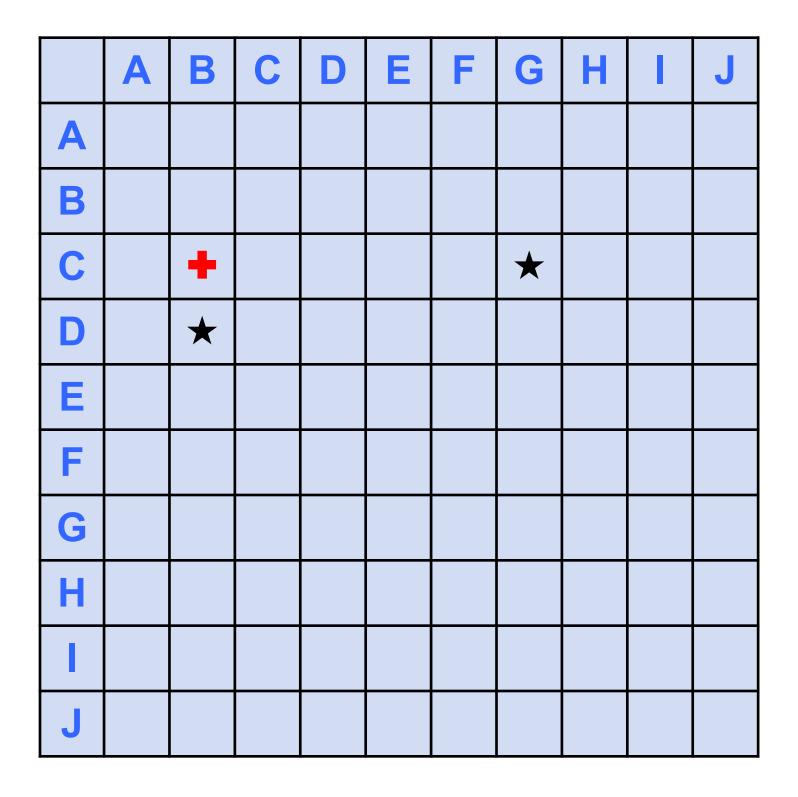
Shoot DB – "Miss"



	Α	В	С	D	Ε	F	G	Η	T	J
Α										
В						b				
С	С	С	С	С	С	b	$\star$			
D		$\star$				b				
Е						b				
F										
G			р		S	S	S			
н			р				d			
							d			
J							d			

## Battleship Rules Shooting

#### **Opponent's Shooting Record**



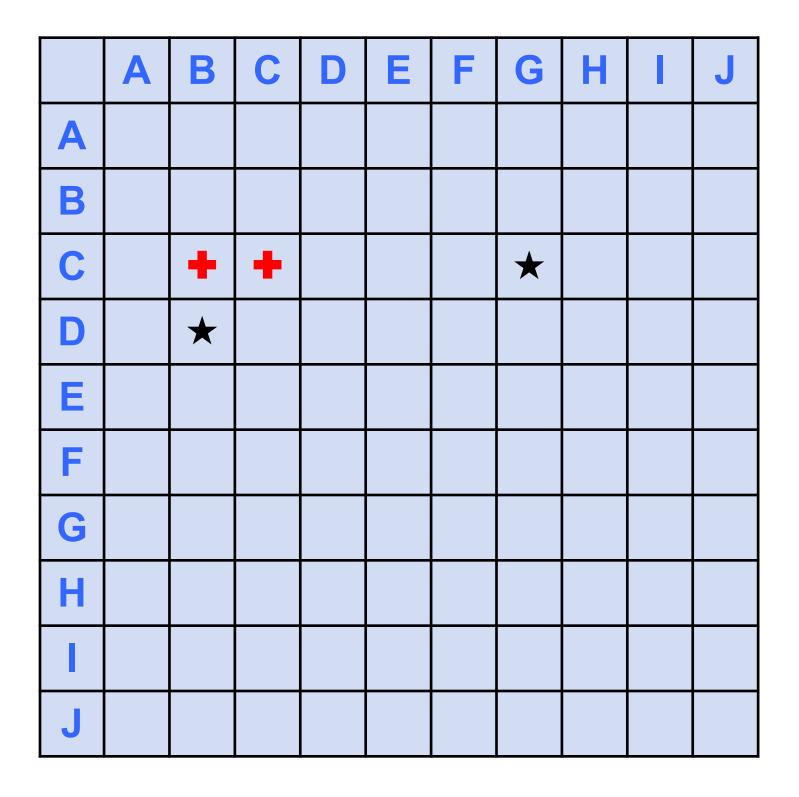
Shoot CC –



	Α	В	С	D	Ε	F	G	Η	I.	J
Α										
В						b				
С	С	С	С	С	С	b	*			
D		$\star$				b				
Е						b				
F										
G			р		S	S	S			
н			р				d			
1							d			
J							d			

## **Battleship Rules** Shooting

#### **Opponent's Shooting Record**



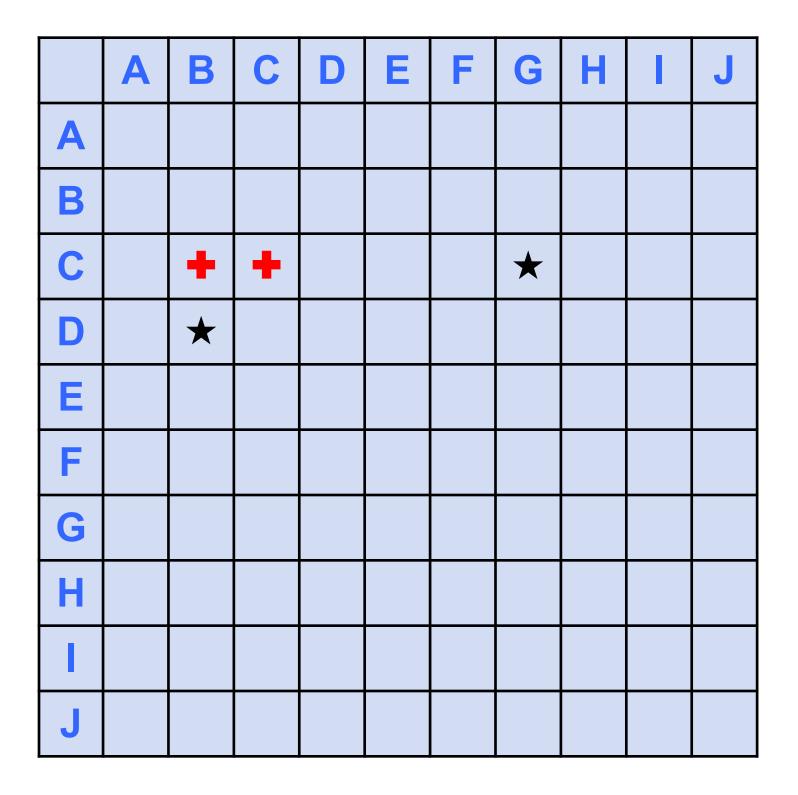
Shoot CC – "Hit"



	Α	В	С	D	Е	F	G	Η	I.	J
Α										
В						b				
С	С	С	С	С	С	b	*			
D		*				b				
Е						b				
F										
G			р		S	S	S			
н			р				d			
							d			
J							d			

Skipping Ahead ...

## **Battleship Rules** Shooting

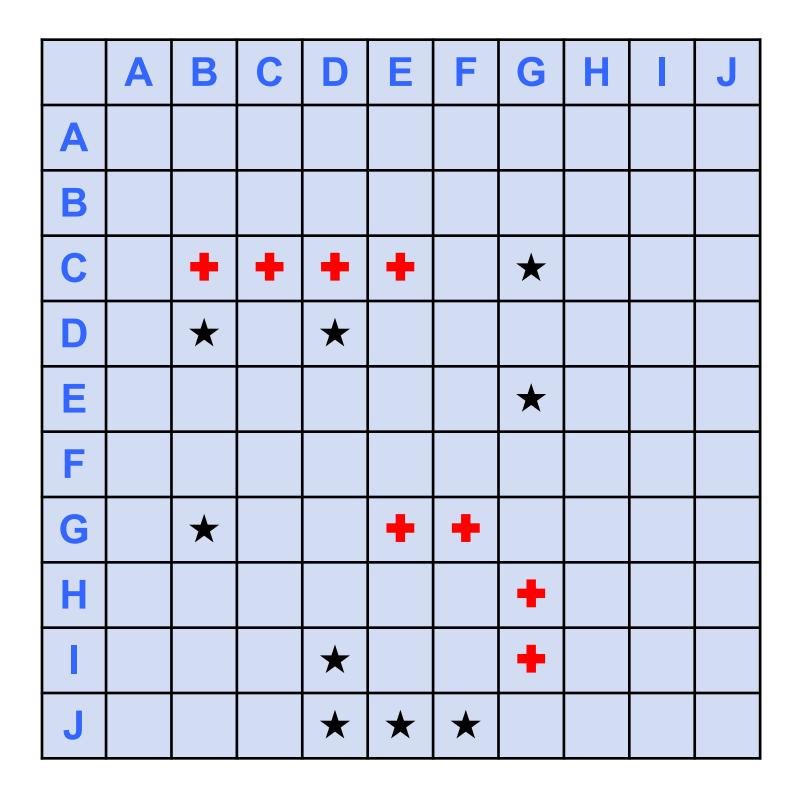




	Α	В	С	D	Ε	F	G	Η	Т	J
Α										
В						b				
С	С	С	С	С	С	b	*			
D		*		*		b				
Е						b	$\star$			
F										
G		$\star$	р		S	S	S			
н			р				D			
				*			D			
J				$\star$	$\star$	$\star$	d			

Shoot CA –

## **Battleship Rules** Shooting

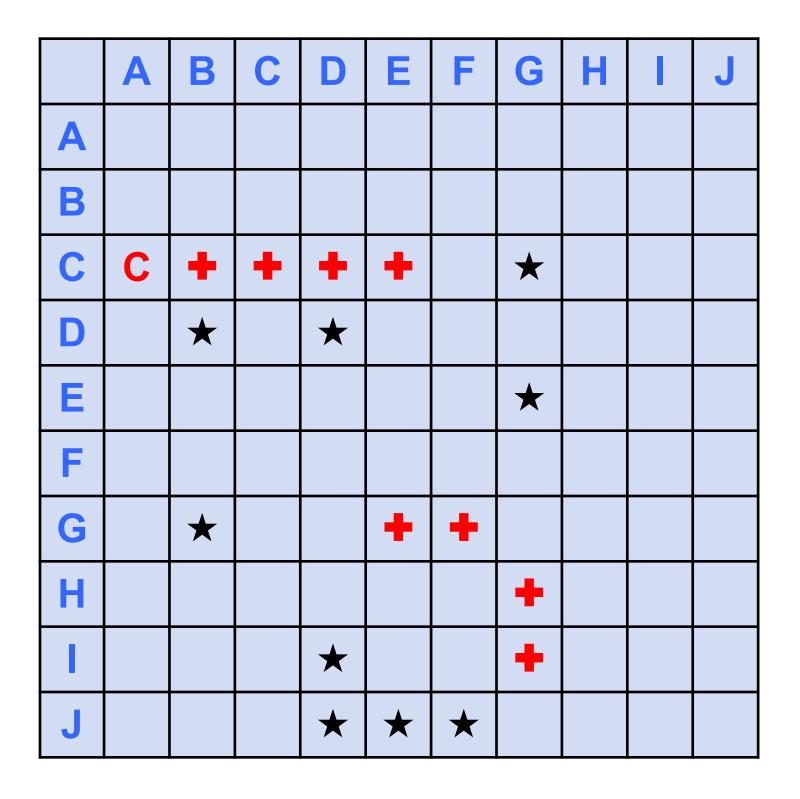




	Α	В	С	D	Ε	F	G	Η	I.	J
Α										
В						b				
С	С	С	С	С	С	b	*			
D		$\star$		$\star$		b				
Е						b	$\star$			
F										
G		*	р		S	S	S			
н			р				D			
				$\star$			D			
J				*	$\star$	$\star$	d			

## **Battleship Rules** Shooting

#### **Opponent's Shooting Record**



Shoot CA – "Sank Carrier"

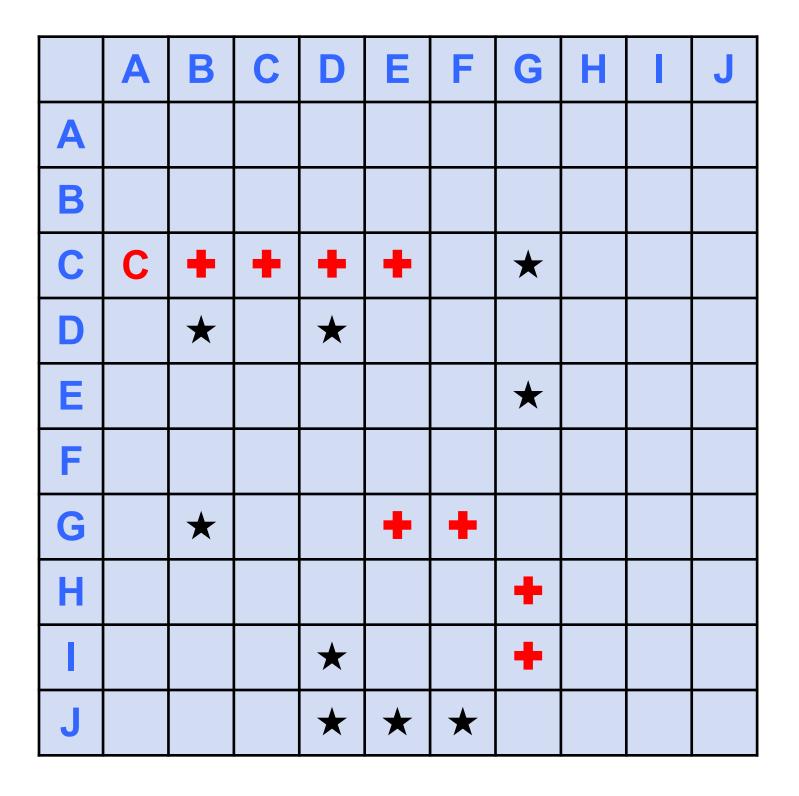


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	Α	В	С	D	Ε	F	G	Η	Т	J
Α										
В						b				
С	С	С	С	С	С	b	$\star$			
D		$\star$		$\star$		b				
Е						b	$\star$			
F										
G		$\star$	р		S	S	S			
н			р				D			
				$\star$			D			
J				*	$\star$	$\star$	d			

**Position Inference – Carrier** 

## **Battleship Rules** Shooting

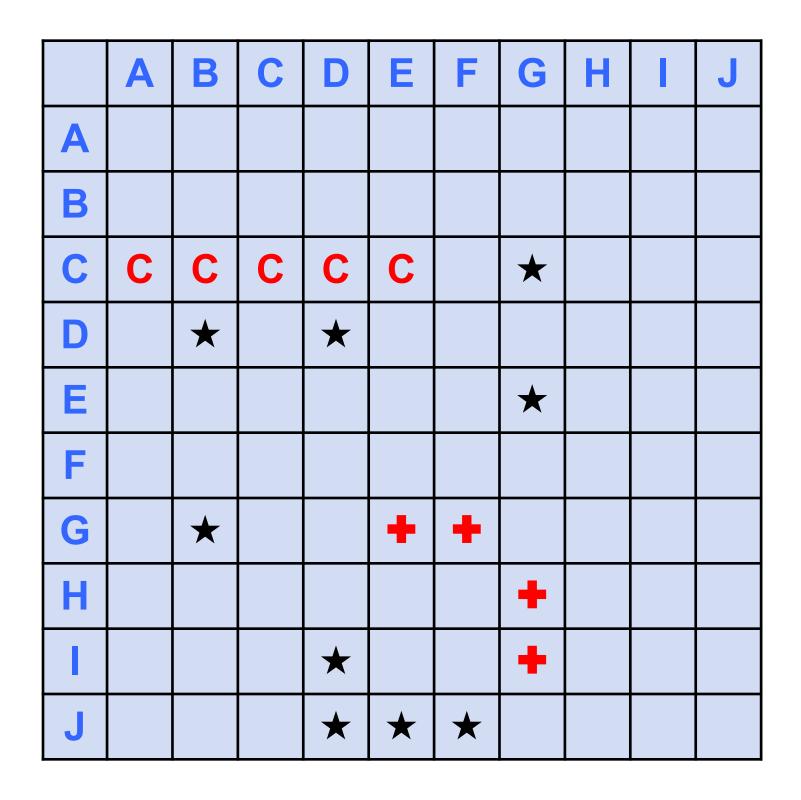




	Α	В	С	D	Ε	F	G	Η	T	J
Α										
В						b				
С	С	С	С	С	С	b	$\star$			
D		*		*		b				
Е						b	$\star$			
F										
G		*	р		S	S	S			
н			р				D			
				$\star$			D			
J				$\star$	$\star$	$\star$	d			

Shoot GG –

## **Battleship Rules** Shooting

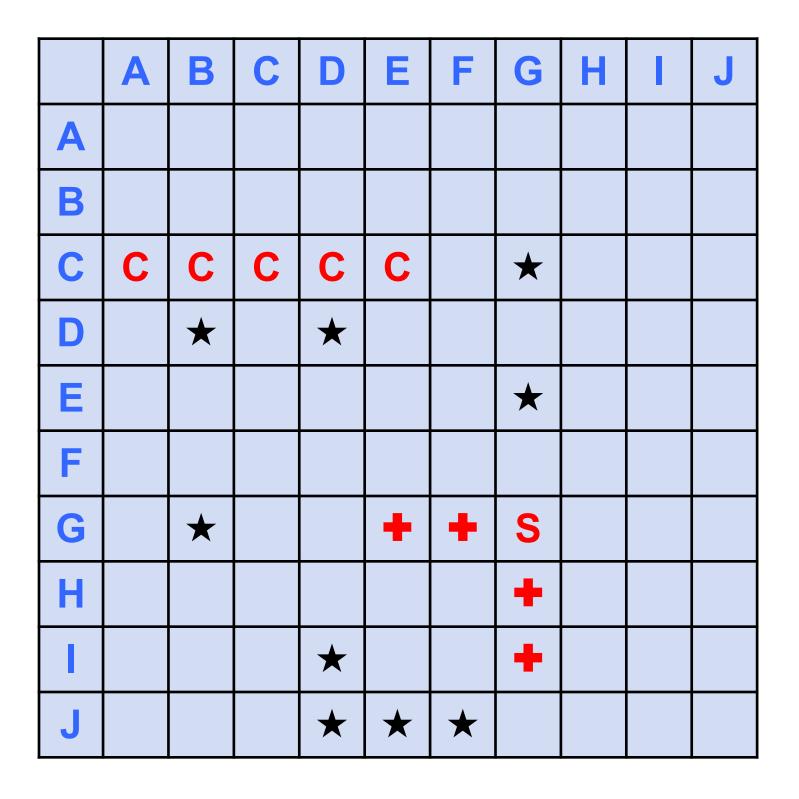




	Α	В	С	D	Ε	F	G	Η	T	J
Α										
В						b				
С	С	С	С	С	С	b	$\star$			
D		$\star$		$\star$		b				
Е						b	*			
F										
G		*	р		S	S	S			
н			р				D			
				*			D			
J				$\star$	*	$\star$	d			

## **Battleship Rules** Shooting

#### **Opponent's Shooting Record**



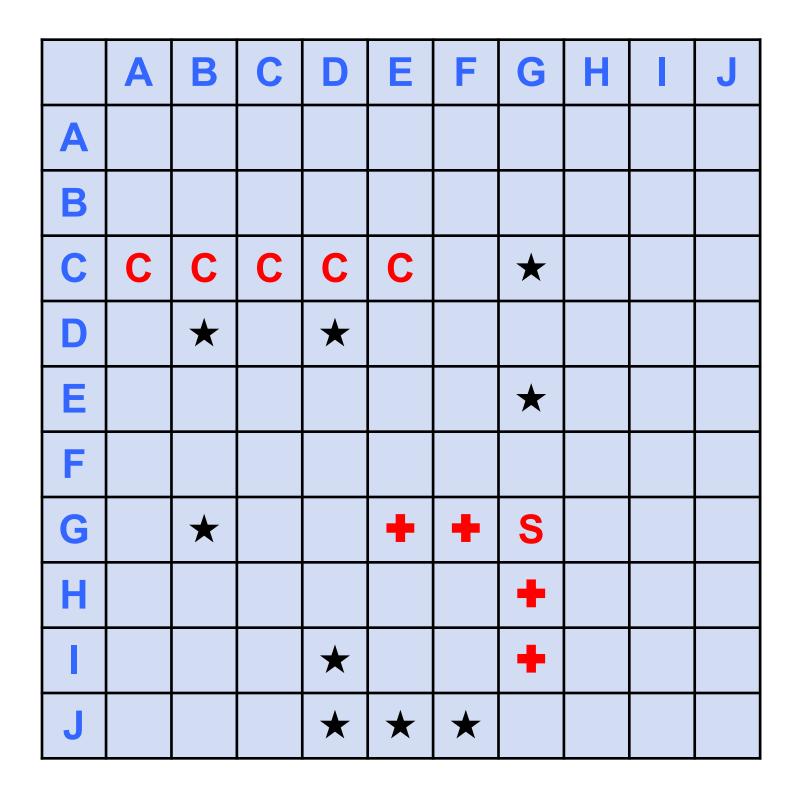
Shoot GG – "Sank Submarine"



	Α	В	С	D	Ε	F	G	Η	T	J
Α										
В						b				
С	С	С	С	С	С	b	$\star$			
D		$\star$		$\star$		b				
Е						b	*			
F										
G		*	р		S	S	S			
н			р				D			
				$\star$			D			
J				$\star$	*	$\star$	d			

Shoot JG –

## **Battleship Rules** Shooting

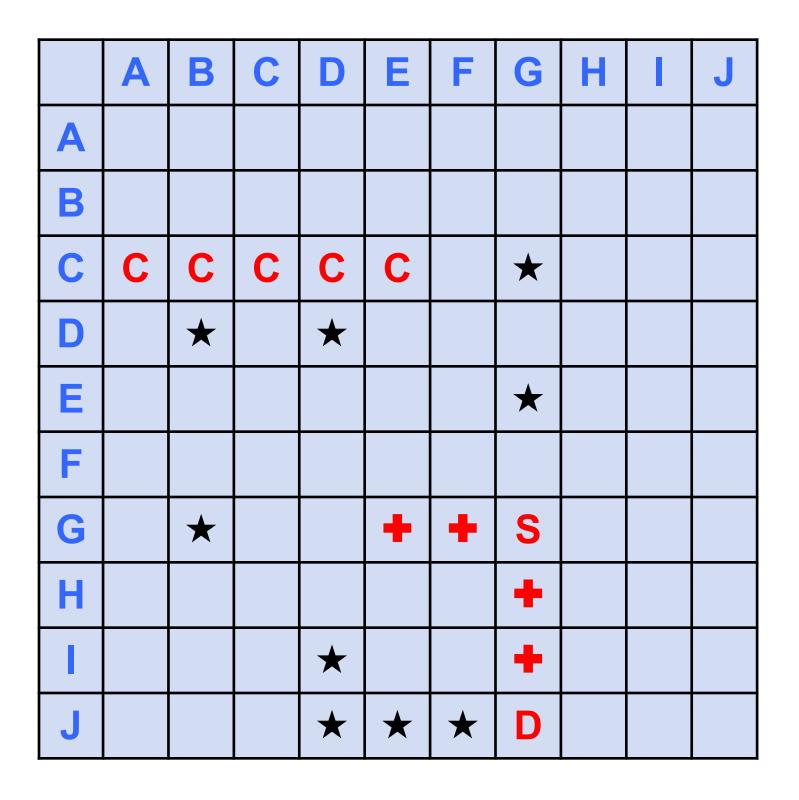




	Α	В	С	D	Ε	F	G	Η	T	J
Α										
В						b				
С	С	С	С	С	С	b	*			
D		$\star$		$\star$		b				
Е						b	$\star$			
F										
G		*	р		S	S	S			
н			р				D			
				$\star$			D			
J				$\star$	$\star$	$\star$	D			

Shoot JG – "Sank Destroyer"

## **Battleship Rules** Shooting



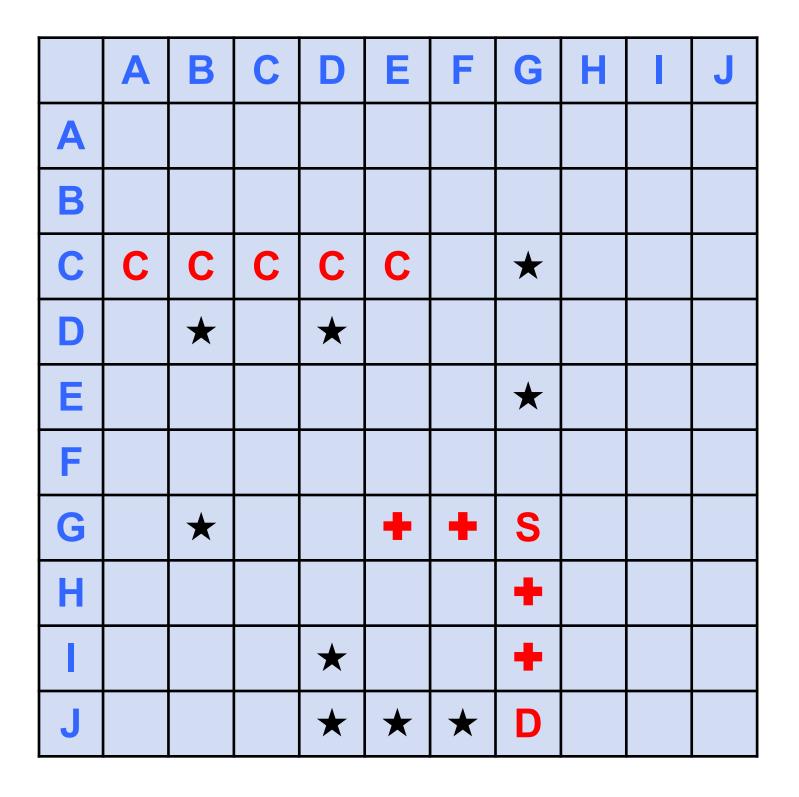




	Α	В	С	D	Ε	F	G	Η	I.	J
Α										
В						b				
С	С	С	С	С	С	b	*			
D		*		*		b				
Е						b	$\star$			
F										
G		$\star$	р		S	S	S			
н			р				D			
				*			D			
J				$\star$	*	$\star$	D			

**Position Inference – Destroyer** 

## **Battleship Rules** Shooting

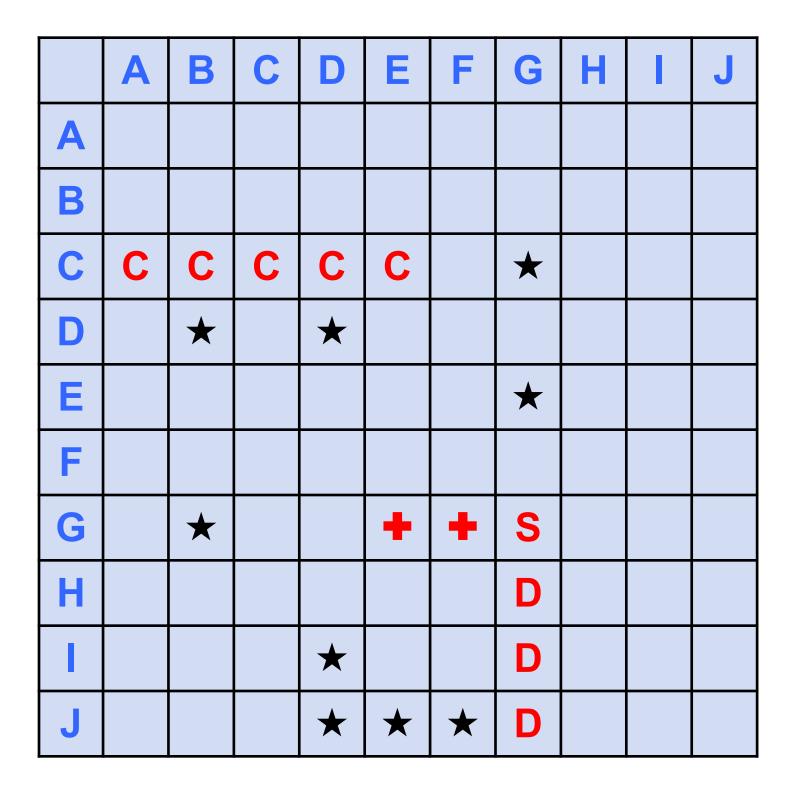




	Α	В	С	D	Ε	F	G	Η	I.	J
Α										
В						b				
С	С	С	С	С	С	b	*			
D		*		*		b				
Е						b	$\star$			
F										
G		$\star$	р		S	S	S			
н			р				D			
				$\star$			D			
J				$\star$	$\star$	$\star$	D			

**Position Inference – Submarine** 

## **Battleship Rules** Shooting





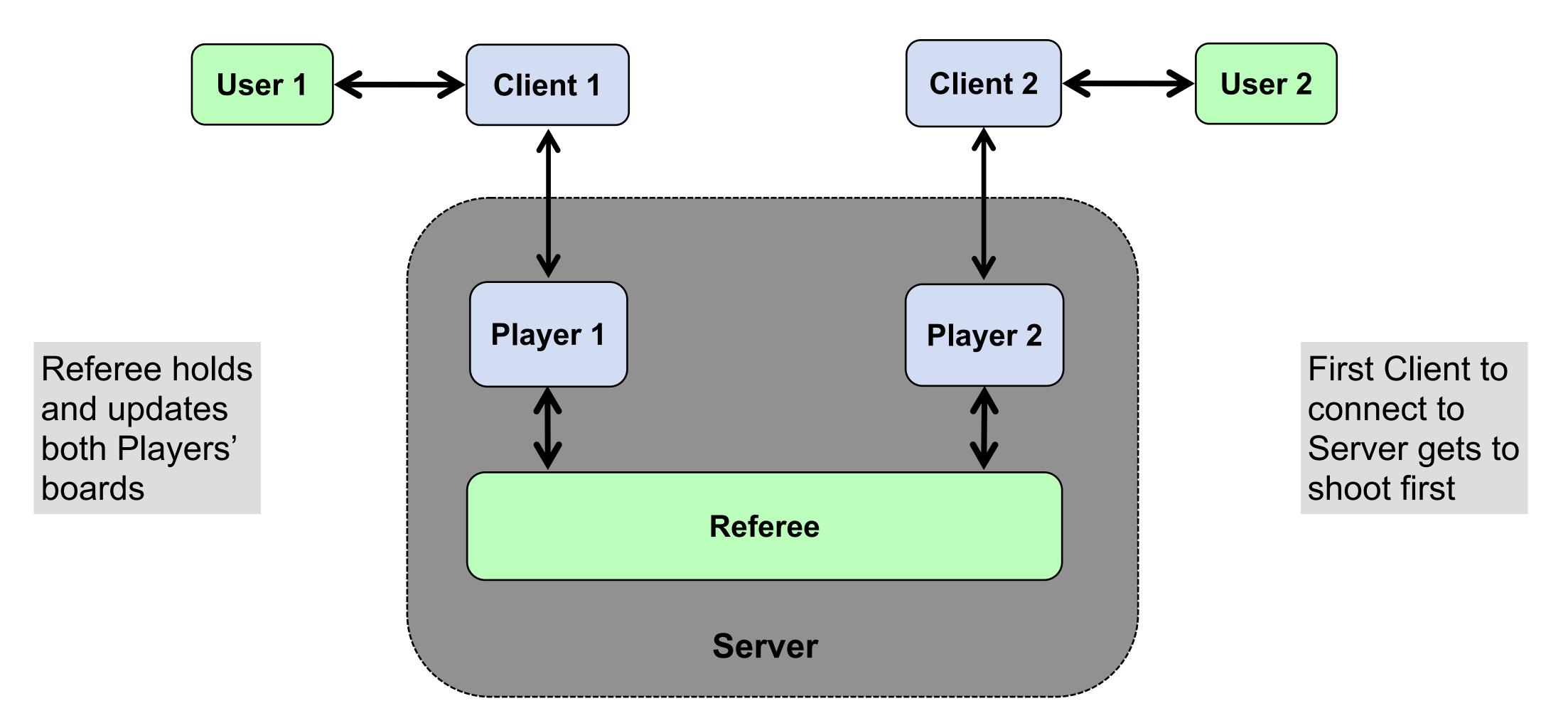
	Α	В	С	D	Ε	F	G	Η	T	J
Α										
В						b				
С	С	С	С	С	С	b	$\star$			
D		$\star$		$\star$		b				
Е						b	$\star$			
F										
G		*	р		S	S	S			
н			р				D			
				$\star$			D			
J				*	$\star$	$\star$	D			

# Battleship Rules Shooting

	Α	В	С	D	Ε	F	G	Η	T	J
Α										
В										
С	С	С	С	С	С		$\star$			
D		*		*						
Е							$\star$			
F										
G		$\star$			S	S	S			
н							D			
				$\star$			D			
J				*	*	*	D			



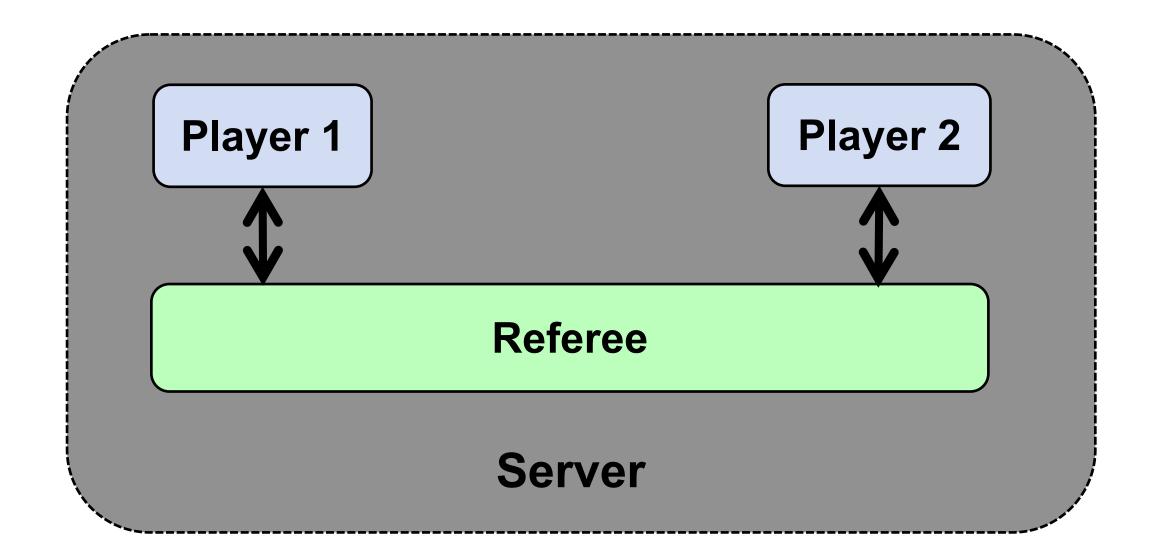
## **Program Architecture and Behavior**





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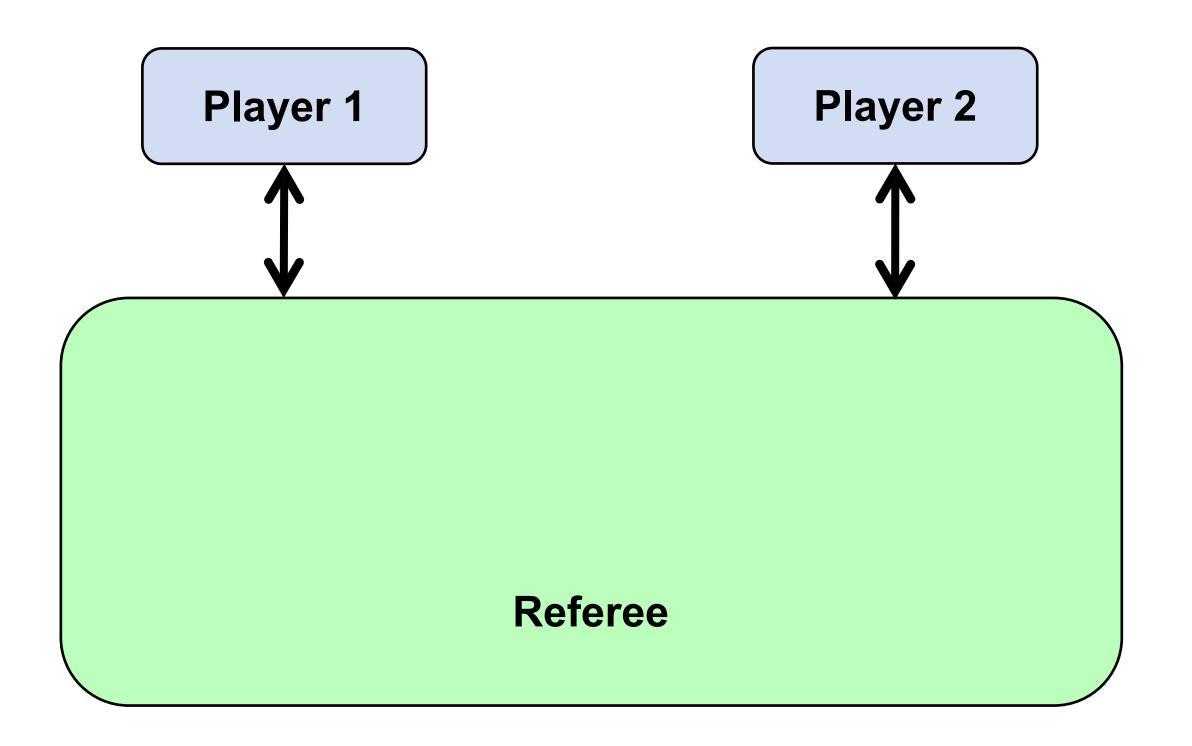
- We implemented in Concurrent ML a trusted referee that holds and updates both player's boards, enforcing the rules of the game
- But we were also interested in reducing the trusted computing base (TCB), by splitting the referee into mutually distrustful player interfaces



## **Trusted Referee**

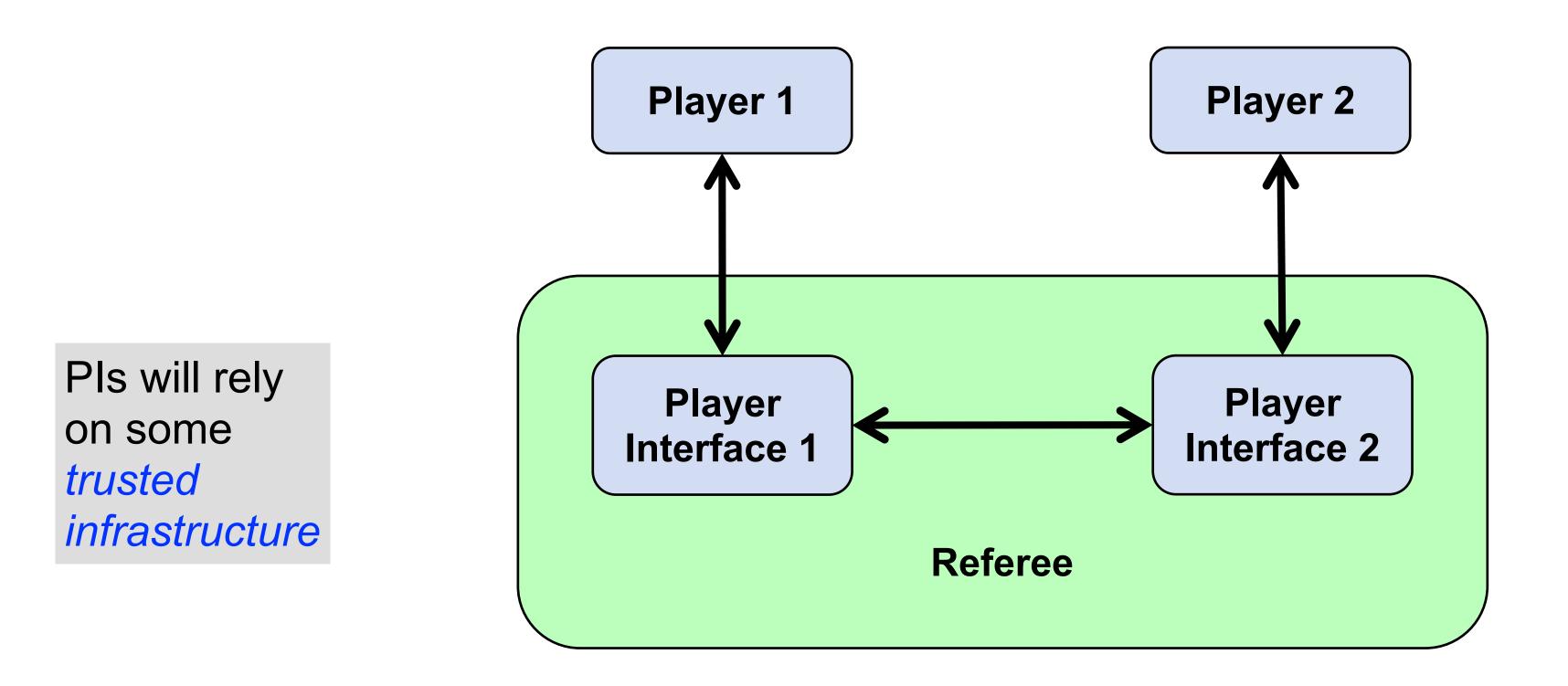


## Splitting Referee into Mutually Distrustful Player Interfaces (Pls)





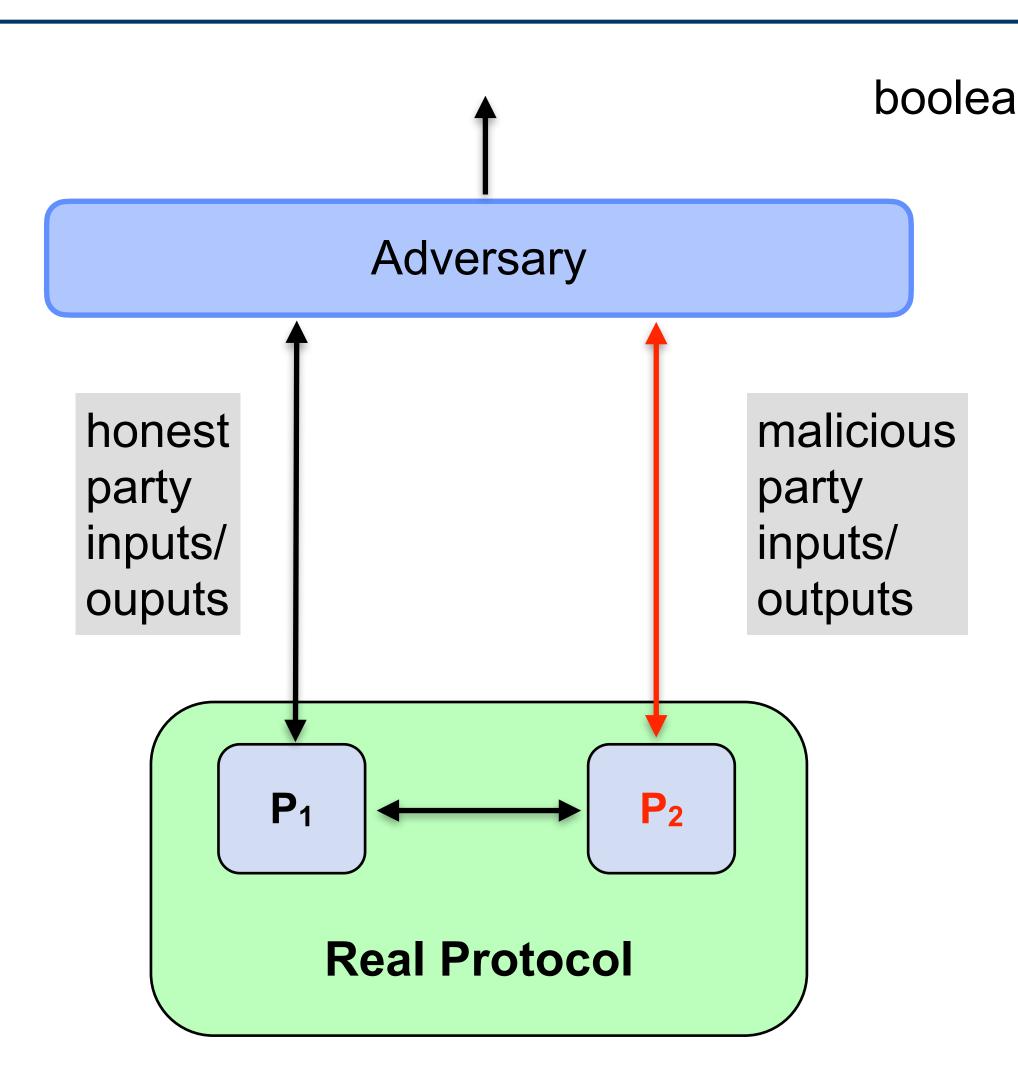
## Splitting Referee into Mutually Distrustful Player Interfaces (Pls)

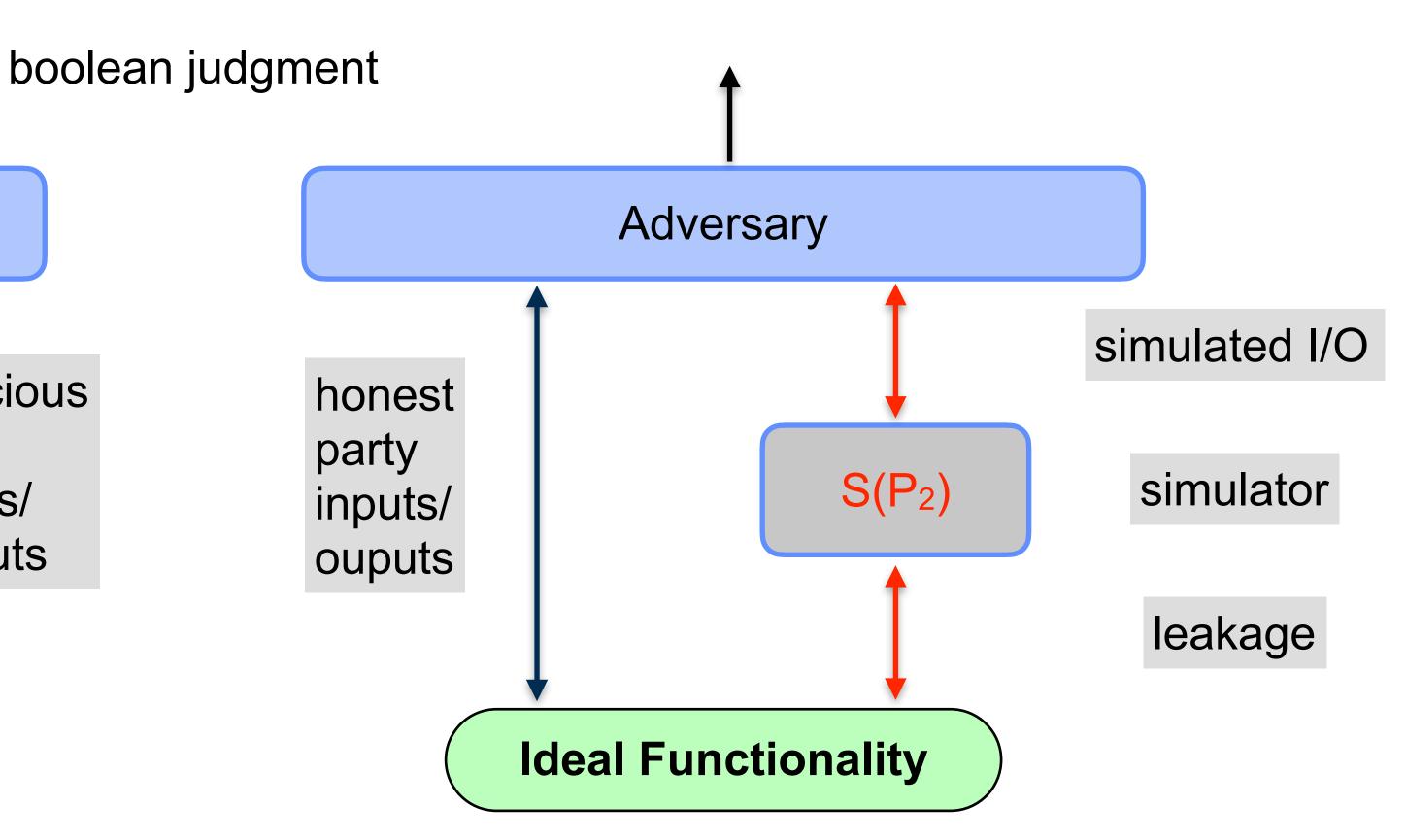


### How do we define security against a malicious opponent PI?



## **Theoretical Cryptography's Real/Ideal Paradigm**



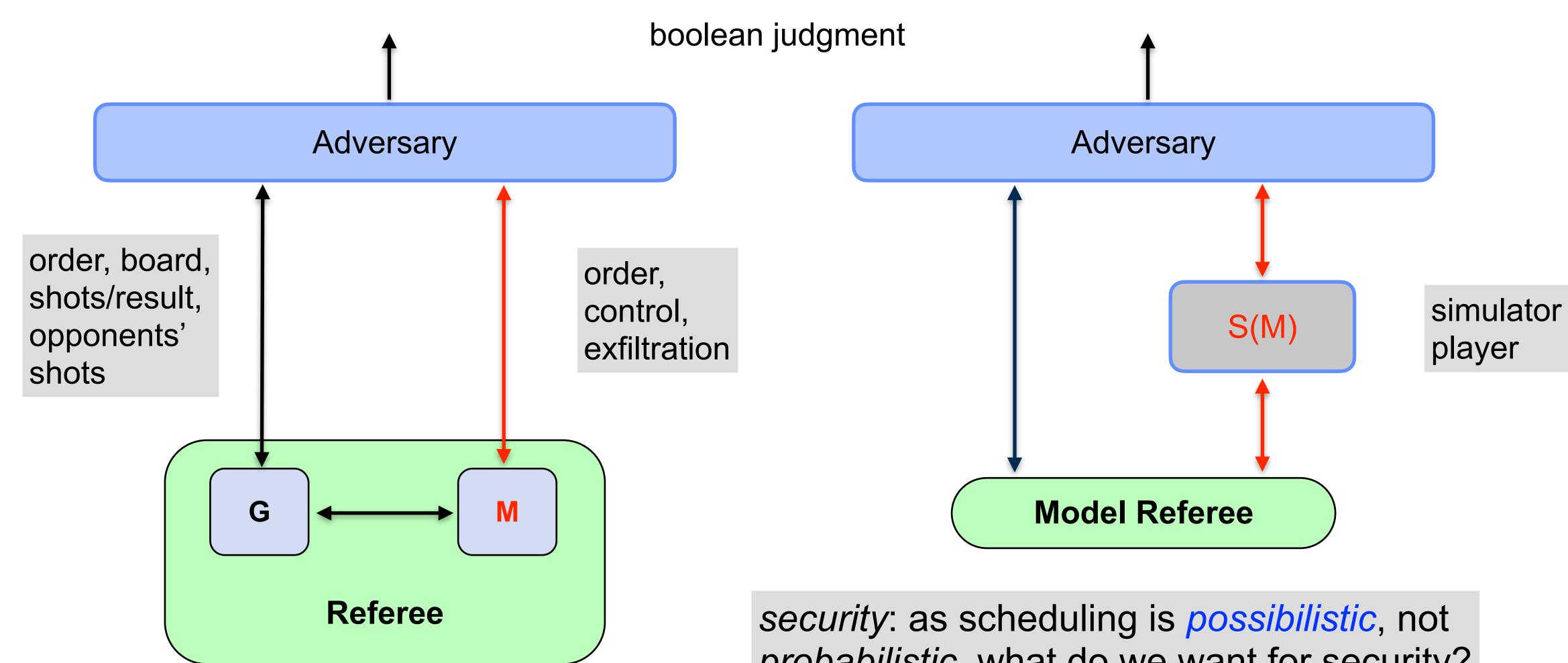


security: real and ideal games have close to same probability of returning true, for all adversaries





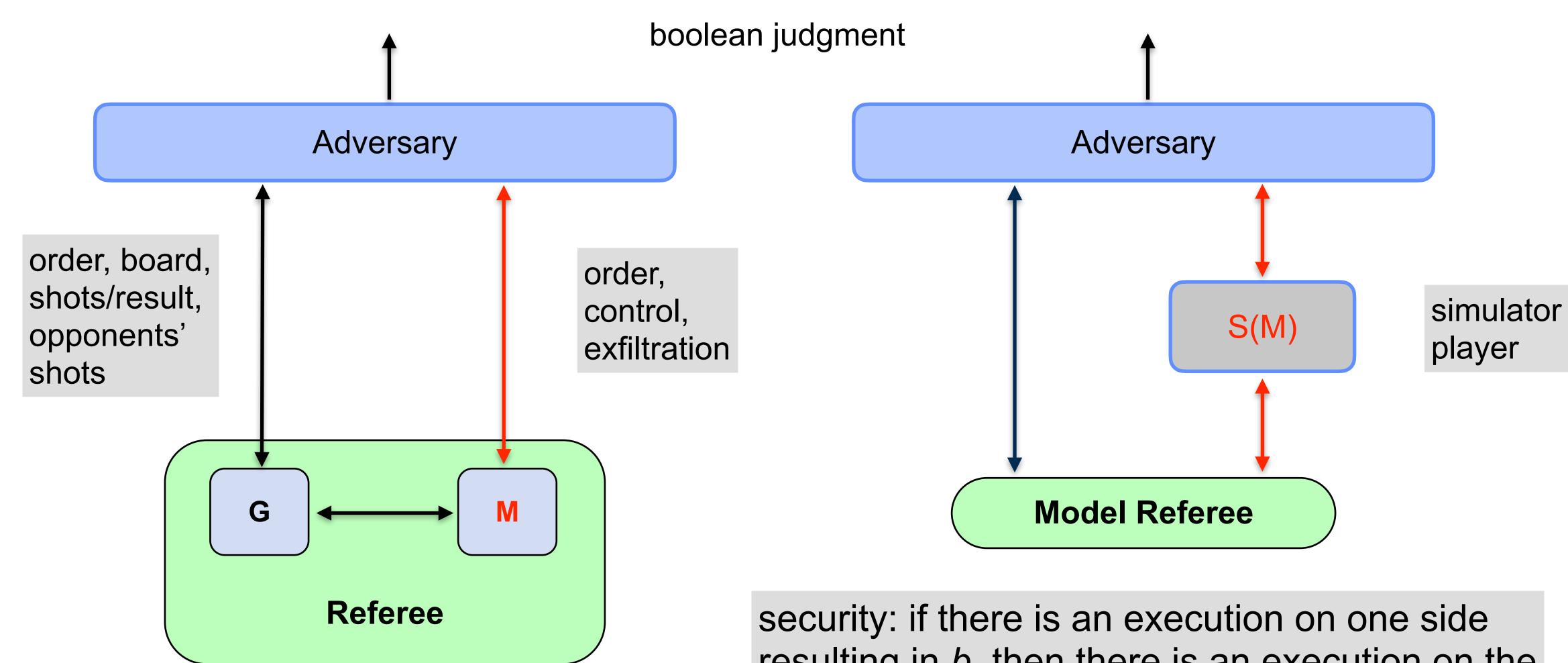
## **Security Against Malicious PI (Tentative)**



probabilistic, what do we want for security?



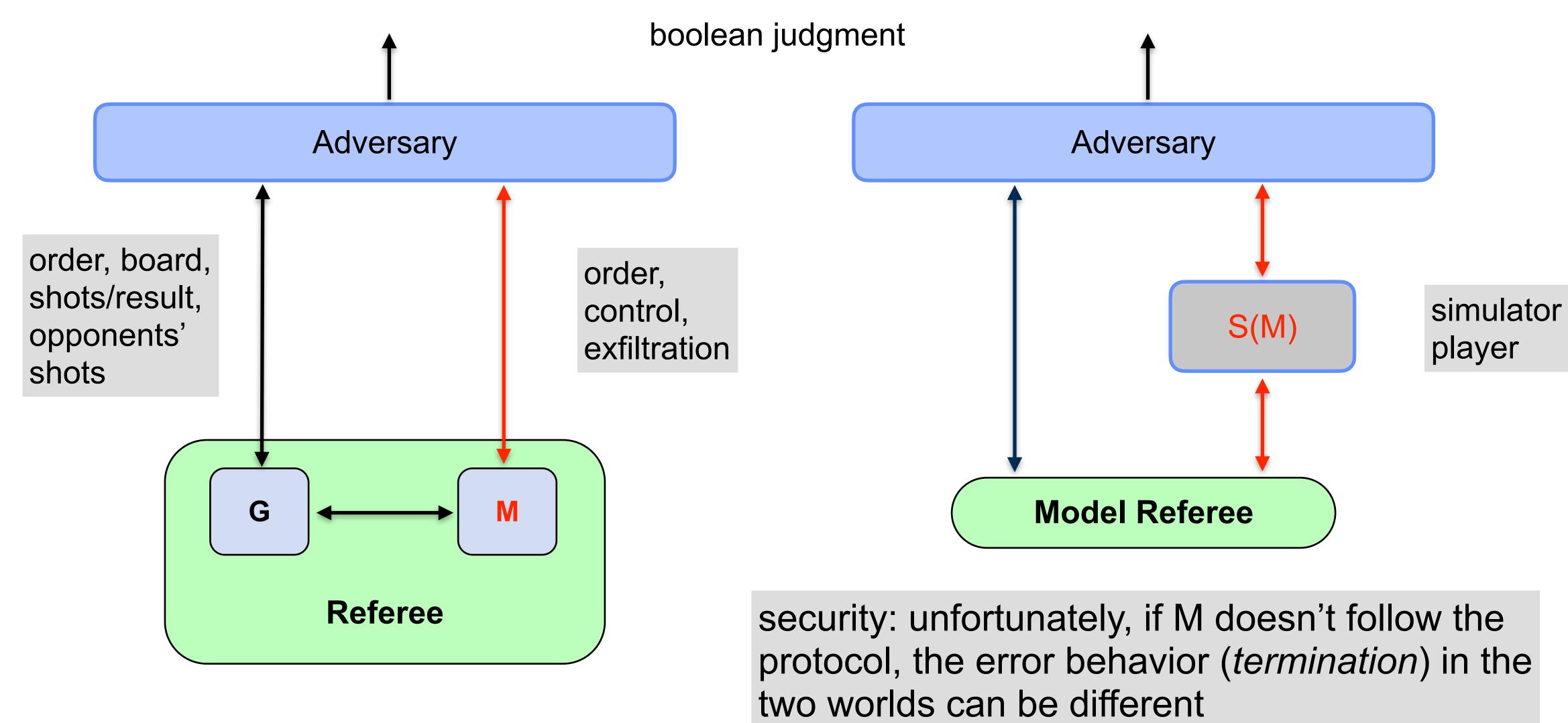
## **Security Against Malicious PI (Tentative)**



resulting in b, then there is an execution on the other side also resulting in *b* 

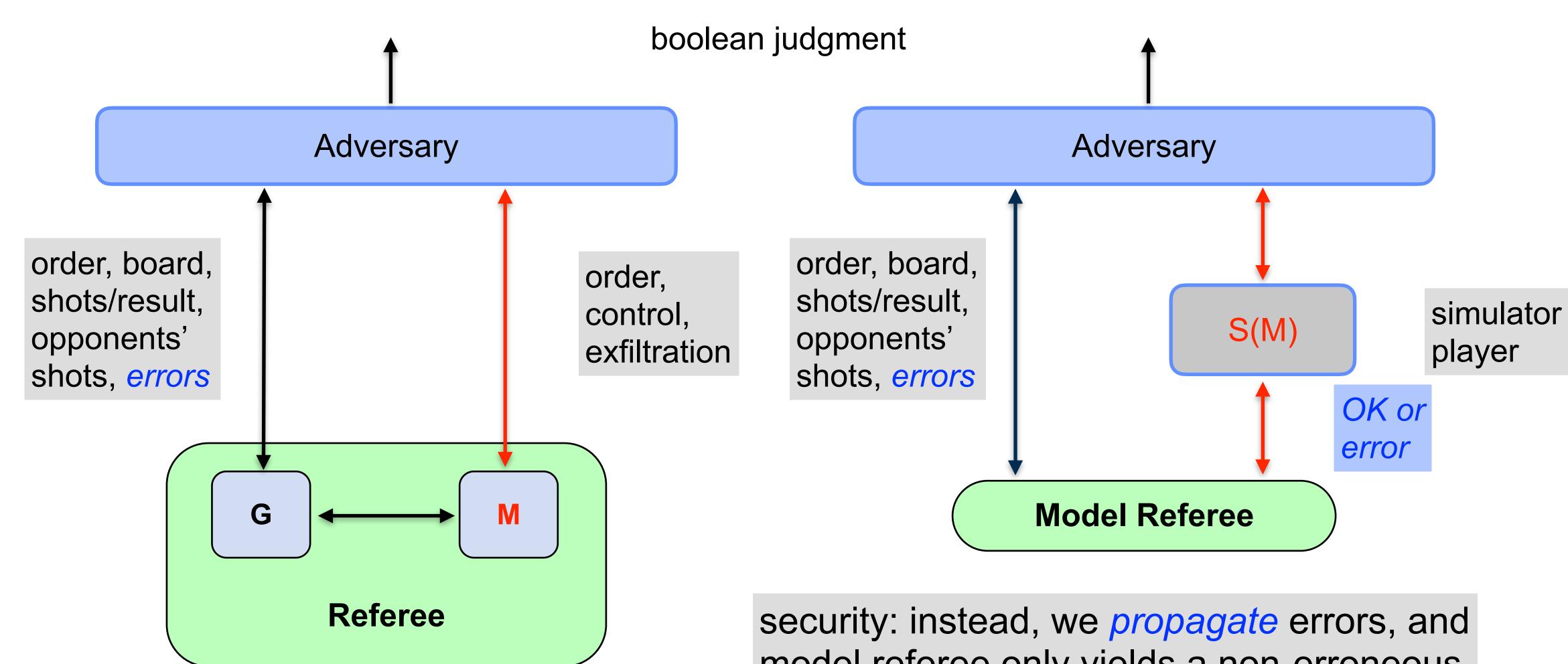


## **Security Against Malicious PI (Tentative)**





## Security Against Malicious Pl



security: instead, we *propagate* errors, and model referee only yields a non-erroneous result if simulator player says OK



- In the next lecture with we'll start with review of: the program architecture of our secure battleship implementations in
  - Haskell/LIO and Concurrent ML
  - our Real/Ideal Paradigm definition of security against a malicious player interface
- Then we'll survey the two implementations and consider how we used our security definition to audit them

